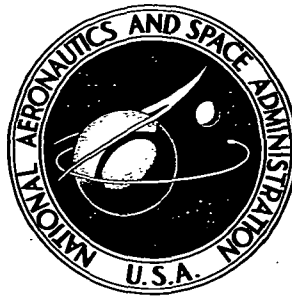


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**CASE FILE
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**NUMERICAL ANALYSIS OF
STIFFENED SHELLS OF REVOLUTION**

Volume V of VII

by V. Svalbonas and P. Ogilvie

Prepared by

GRUMMAN AEROSPACE CORPORATION

Bethpage, N.Y. 11714

for George C. Marshall Space Flight Center

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16. ABSTRACT This manual contains engineering programming information for the STARS-2B (Shell Theory Automated for Rotational Structures -2B (Buckling)) digital computer program. The report is written for the engineer who will need to make small alterations to the program, such as incorporating a new geometry, or altering a table size, to fit his specific needs. The sections of the manual each cover one major subroutine. These sections are further subdivided in the following manner where applicable: A. Subroutine description. B. A list of pertinent engineering symbols and their FORTRAN coded counterparts. C. Subroutine flow chart. D. Subroutine FORTRAN listing.			
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- VOLUME III. Users' Manual for STARS-2B, 2V - Shell Theory Automated for Rotational Structures - 2 (Buckling, Vibrations), Digital Computer Programs
- VOLUME IV. Engineer's Program Manual for STARS-2S - Shell Theory Automated for Rotational Structures - 2 (Statics), Digital Computer Program
- VOLUME V. Engineer's Program Manual for STARS-2B - Shell Theory Automated for Rotational Structures -2 (Buckling), Digital Computer Program
- VOLUME VI. Engineer's Program Manual for STARS-2V - Shell Theory Automated for Rotational Structures -2 (Vibration), Digital Computer Program
- VOLUME VII. Satellite Programs for the STARS System

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INTRODUCTION

This manual presents a general description of the STARS-2B digital computer program. FORTRAN IV is used exclusively in writing the various subroutines. The execution of this program requires the use of eleven temporary storage units.

The program was initially written and debugged on the IBM 370-165 computer and then converted to the UNIVAC 1108 computer, where it utilizes approximately 46,000 words of core. Only basic FORTRAN Library routines are required by the program, these being: sine, cosine, absolute value, square root, min 0, max 0, amax 1, amin 1, and random.

For ease and speed in usage, the Table of Contents on the following page has also been laid out to present the call sequence of the program.

CONTENTS

CALL SEQUENCE	CALLING ROUTINE	PAGE
MAIN		1
RIEMAN	MAIN	9
SETUP	RIEMAN	23
MAGIC	RIEMAN	23
ROBOT	RIEMAN	27
GEOMET	ROBOT	27
PLICO	GEOMET	27
PLINE	GEOMET	27
DIF1	RIEMAN	44
DIFF2	RIEMAN	44
SEGMAT	MAIN	59
SREVN2	SEGMAT	59
REGMAT	MAIN	68
RINGER	REGMAT	85
SWITCH	REGMAT	68
CHASE	REGMAT	68
FUTILE	CHASE	68
TRIEQ	CHASE	68
STRMAT	MAIN	91
RINGER	STRMAT	85
FLEX	STRMAT	91
INITAL	MAIN	102
LEBEGE	MAIN	109
FIXEM	LEBEGE	109
WAND	LEBEGE	109
TOBAR	LEBEGE	109
TEMOEG	TOBAR	109
PLYCO	TEMOEG	109
PLYNE	TEMOEG	109

CALL SEQUENCE	CALLING ROUTINE	PAGE
ODE1	LEBEGE	135
ODE2	LEBEGE	135
EIGVAL	MAIN	147
COMPAK	EIGVAL	147
EIGEN	EIGVAL	151
FUTILE	EIGEN	68
DAGGER	EIGEN	151
SWITCH	EIGEN	68
SYMEIG	EIGEN	151
TFORM	SYMEIG	151
STURM	SYMEIG	151
PREP	STURM	151
DET	STURM	151
SYMVEC	EIGEN	151
QSVEC	SYMVEC	151
QWIEL	SYMVEC	151
RANDOM	QWIEL	151
ANDD	QWIEL	151
DOTPRO	QWIEL	151
TRIEQ	EIGEN	68
DETERM	MAIN	165
DET2	DETERM	165
DCOMP2	DET2	165
SUPER	DCOMP2	165
BCVECT	MAIN	172
ETRAP	MAIN	175

SUBROUTINE MAIN

MAIN is the control link for the entire program. Sizing values are read into the program, as well as information for eigenvalue or determinant accuracy calculations, and the material property tables. Calls are made to subroutines RIEMAN and SEGEMAT once for each segment in a region; then subroutine REGMAT is called. This procedure is executed once for every region in the structure. Finally a call to subroutine STRMAT is made. If the clues are set for the program to calculate the prestress state, subroutines INITAL and LEBEGE are called. Otherwise the control link loops back and resets the clues for the calculation of nonlinear stiffness matrices.

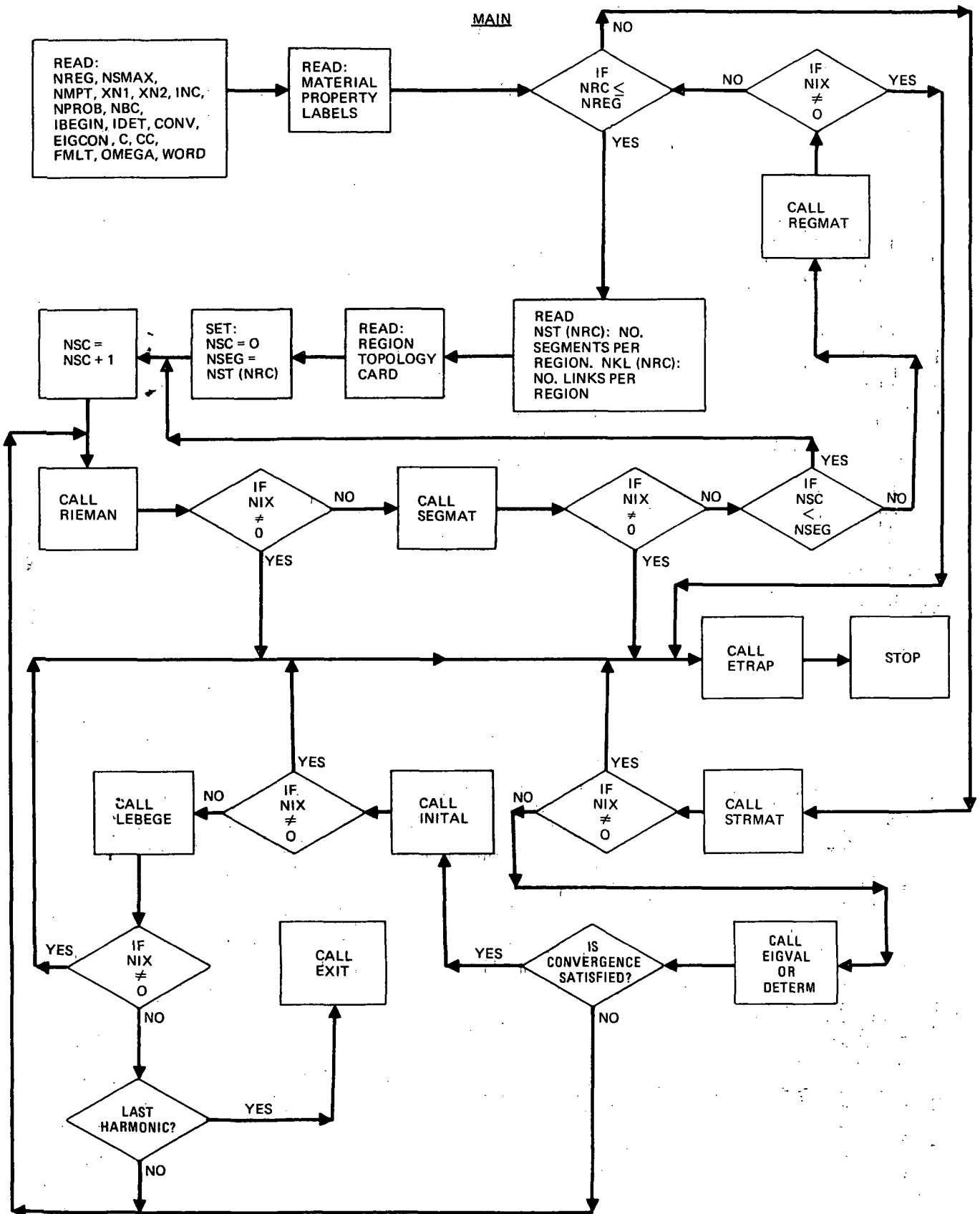
In the calculation loop for the nonlinear stiffness matrices the program proceeds as above to STRMAT. Next EIGVAL or DETERM are called to calculate eigenvalues or evaluate a determinant as per user input. If these calculations satisfy convergence criteria, subroutines BCVECT, INITAL, and LEBEGE are called. If convergence criteria are not satisfied the program will loop until satisfaction is obtained.

In a multi-harmonic eigenvalue search the whole procedure loops on the harmonic number.

There are also several counters in this control link. These are defined as follows:

- NSC - Counts the calls to subroutines RIEMAN and SEGEMAT, from 1 to the number of segments within a region.
- NRC - Counts the calls to subroutine REGMAT, from 1 to the number of regions in the structure.
- ICYC - Cycle counter (counts harmonics).
- NPASS - Pass counter (counts passes necessary to converge in a single harmonic).

The block data and overlay listings are included in this section.



```

C ..... ROUTINE **D1      ** ABACUS UPDATED 07/01/72 .....
HLØCK DATA
COMMON /NAME1/ FACE(4),STRGØ(7),THERM(4),MATER(3),SEGTAB(12)
DATA STRGØ /11.0,13.0,21.0,31.0,12.0,14.0,15.0/
DATA THERM /4HTHST,4HNØTH,4HTHCN,4HTHIN/
DATA MATER /4HISØ1,4HØRTH,4HSTIF/
DATA SEGTAB/4HST1Ø,4HTHIC,4HRWAF,4HRWAL,4HRWA2,4HRWA3,4HISG1,
1 4HISG2,4HISG3,4HST11,4HST12,4HST13/
DATA FACE /4HSING,4HEQUA,4HUNEQ,4HBLAN/
COMMON /HINTER/INDIC8
COMMON /RØND/M,L
END
100000
100010
100020
100030
100040
100050
100060
100070
100080

100090

```

```

C ..... ROUTINE **D2 ** ABACUS UPDATED 07/25/72 .....
INTEGER SAVJTC, SAVSTP, SEGTA, 0, THICK, TYPE
INTEGER XN1, XN2, XN
DOUBLE PRECISION SAVTIC, TIC, PHI, ST0P, REST0P, RTICK
DOUBLE PRECISION YC0RR
COMMON ST0RY(16), XMAT(110,10), STD(10), SADUS(30), RADIUS(30)
COMMON TADUS(30), UADUS(30), SAVTIC(900)
COMMON XN, TEFREE, TIC, PHI, ST0P, REST0P, RTICK, G1, XNL(2), NH
COMMON NST(30), NKL(30), NXMAT(20), SAVJTC(30), SAVSTP(30), JRTIC(30)
COMMON JRST0P(30), NREG, NMPT, NRC, NSC, NIX, IERR0R, KGE0M, IGE0M, ISTATB
COMMON KELVIN, IBEGIN, NPR0B, NSEG, NERR0R, Q, THICK, N0JS, NLINKS, NLCASE
COMMON NTSKL, NZ, NBCT, LINPUT, NTRKL, NPASS, XN1, KBC, NRINGS
COMMON /NAME/, FACE(4), STRG0(7), THERM(4), MATER(3), SEGTAB(12)
COMMON /LYC0RR/ YC0RR(80)
COMMON /RING/ RRING(28), AMAT(30,4), IRLC(28)
DIMENSION QVEC(128,2)
1 WRITE(6,1726)
1726 FORMAT(1H1)
REWIND 1
REWIND 2
REWIND 3
REWIND 4
REWIND 8
REWIND 9
REWIND 10
REWIND 11
REWIND 12
REWIND 13
REWIND 14
NIX = 0
O=5
READ(5,1001,END=555) (STORY(I),I=1,16)
1001 FORMAT (16A4)
READ(5,1002) NREG, NSMAX, NMPT, XN1, XN2, INC, NPR0B, NBC, KBC, IBEGIN,
1 IDET, C0NV, EIGC0N, C, CC
1002 FORMAT(12,13,9I2,4F7.0)
XN = XN1
WRITE(6,602) NSMAX, NREG, NMPT, NPR0B, NBC, XN1, XN2, INC
602 FORMAT(///19X,93HUNSMMETRIC, 0RTH0TR0PIC, REINF0RCED SHELL ANALY
1SIS WITH COUPLING 0F AT M0ST 29 SHELL REGIONS/762X,-STARTS-2B-//
2 56X,-AS 0F N0VEMBER 1, 1972-///8X,21HN0MBER 0F SEGMENTS = ,13,
321H NUMBER 0F REGIONS = ,12,43H NUMBER 0F MATERIAL PR0PERTY TABLES
4 USED = ,12,22H NUMBER 0F PR0BLEMS = ,12//8X,-NUMBER 0F B0UNDARY C
50NDIT10N-MATRICES = -,12///40X,-STABILITY HARMONICS (N) = -,12,
6 - 10 - ,12,- INCREMENTED BY -,12)
IF (KBC.NE.0) G0 T0 502
WRITE(6,604)
604 FORMAT(///31X,-THE GIVEN INPUT INDICATES THAT THE PREBUCKLING STAT
1E WILL BE CALCULATED-)
G0 T0 503
502 WRITE(6,608)
608 FORMAT(///31X,-THE GIVEN INPUT INDICATES THAT THE PREBUCKLING STAT
1E WILL BE PR0VIDED-)
503 CONTINUE
WRITE(6,605) (STORY(I),I=1,16)
605 FORMAT(18(//),8X,16A4,18(//),80X,35H0R INF0RMATION CALL V. SVALB0N
1AS/117X,14H(516) 575-7701/103X,10HP. 0GILVIE)
IF (C0NV.EQ.0.0) C0NV = 0.01
C0NVER = C0NV
IF (C.EQ.0.0) C = 0.05

```

```

IF (CC.EQ.0.0) CC = 1.0
D = CC*C
F = C
MDET = 0
KDET = 0
XNL(1) = 0.0
XNL(2) = 0.0
NLCASE = NPR0B
NH = 0
XN = 0
ICYC = 1
MPASS = 0
MPAS = 0
KNBC = 2
LINPUT = 1
JNBC = IABS(NBC)
FIGCON = ABS (EIGCON)
NR0W=0
KK=-1
NSAVE=0
D0 13 I=1,NMPT
KK=KK+2
NXMAT(KK)=NR0W+1
II=NR0W+1
READ(5,1004) STD(1),TYPE
1004 FORMAT (A4,6X,A4,6X)
NR0W = 11
D0 11 L=1,3
G0 T0 8000
11 IF (TYPE.EQ.MATER(L)) G0T0 12
12 CONTINUE
IF (L.EQ.1) NR0W=4
IF (L.EQ.2) NR0W=7
LL=NSAVE+NR0W
READ(5,1005) ((XMAT(M,J),J=1,10),M=II,LLL)
1005 FORMAT (5E14.7)
NR0W=NSAVE+NR0W
NXMAT(KK+1)=LLL
13 NSAVE=NR0W
READ(5,2000)
2000 FORMAT(1X)
100 NPASS = NPASS+1
REWIND 13
REWIND 4
IF (KBC.NE.0) NPR0B = 0
IF (NH.EQ.0) G0 T0 618
IF ((ICYC.GT.1.AND.NPASS.EQ.1) G0 T0 618
IF (NPASS.LT.3.AND.XN.EQ.XNL.AND.(XN.NE.0.0R.NLCASE.NE.1))
1 G0 T0 618
NPAS = NPAS+1
WRITE(6,1726)
WRITE(6,607) XN
WRITE(6,611) NPAS
618 REWIND 10
D0 99 NRC=1,NREG
IF (NH.EQ.0.0R.IBEGIN.EQ.1) WRITE(6,1726)
IF (Q.EQ.5) READ(5,1003) NST(NRC),NKL(NRC),NRING(NRC),STORY
1003 FORMAT(3I2,16A4)
IF (NH.NE.0) G0 T0 613
WRITE(6,606)NRC,NST(NRC),NKL(NRC)
606 FORMAT(//////////58X,13HREGION NUMBER,13//35X,10HTH
200630
200640
200650
200660
200670
200680
200690
200700
200710
200720
200730
200740
200750
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201100
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201120
201130
201140
201160
201170
201160
201161
201200
201210
201220
201230
201240
201250

```

```

HERE ARE ,I2,14H SEGMENTS AND ,I2,35H KINEMATIC LINKS WITHIN THIS R
REGION)
G0 T0 610
613 IF (IBEGIN.EQ.0) G0 T0 610
WRITE(6,612) NRC,NST(NRC),NKL(NRC)
612 FORMAT(//58X,13HREGION NUMBER,13//35X,10HTHERE ARE ,I2,14H SEGMENT
ITS AND ,I2,35H KINEMATIC LINKS WITHIN THIS REGION)
WRITE(6,607) XN
607 FORMAT(//57X,-HARMONIC (N) =-,I3)
IF (NPAS.NE.0) WRITE(6,611) NPAS
611 FORMAT(//61X,-ESTIMATE=,I3)
610 CONTINUE
IF (O.EQ.5) READ(5,1006) JRTIC(NRC),JRST0P(NRC),STORY
1006 FORMAT(5X,2I5,16A4)
NSEG = NST(NRC)
201 NSC=0
101 NSC=NSC+1
IF (NH.EQ.0-0R.IBEGIN.EQ.1) WRITE(6,1726)
CALL RIEMAN
IF (NIX.NE.0) G0T0 8888
CALL SEGMA
IF (NIX.NE.0) G0T0 8888
IF (NSC.LT.NSEG) G0 T0 101
NSC=0
102 CALL REGMAT
IF (NIX.LT.0) G0 T0 8888
NIX = 0
REWIND 2
REWIND 3
99 CONTINUE
REWIND 11
CALL STRMAT
IF (NIX.NE.0) G0T0 8888
IF (NH.EQ.0) G0 T0 200
IF (NPASS-2) 71,72,198
72 LINPUT = 0
IF (XN.NE.XN1) G0 T0 198
IF (XN.EQ.0-AND.NLCASE.EQ.1) G0 T0 198
71 XNL(NLCASE) = 1
LINPUT = 0
REWIND 1
G0 T0 100
198 IF (IDET.EQ.1-AND.NPAS.GT.1) G0 T0 707
520 CALL EIGVAL (CONVER,EIG,NZ,IBEGIN,QVEC)
IF (NPAS.EQ.1) G0 T0 710
A = XNL(NLCASE)*(12.0*EIG+1.0)/3.0
IF (ABS(ABS(EIG)-1.0).LE.CONVER) A = XNL(NLCASE)*EIG
IF (ABS(ABS(EIG)-1.0).LE.CONVER-AND.IDET.EQ.1) G0 T0 711
XNL(NLCASE) = A
G0 T0 711
710 XNL(NLCASE) = EIG
KFLAG = XNL(NLCASE)/ABS(XNL(NLCASE))
G0 T0 711
707 CALL DETERM (NZ,MDET)
IF (MDET.EQ.KDET-OR.KDET.EQ.0) G0 T0 709
XNL(NLCASE) = XNL(NLCASE)/(1.0-KFLAG*F)
IF (F.GT.0) G0 T0 521
CONVER = 1.E8
G0 T0 520
521 F = F*0.1
MDET = -MDET

```

```

709 XNL(NLCASE) = (1.0-KFLAG*F)*XNL(NLCASE)
KDET = MDET
711 CONTINUE
WRITE(6,700) XNL(NLCASE)
700 FORMAT(/5X,-THE CURRENT LOAD MULTIPLICATION FACTOR =-,1PE14.6)
IF (ABS(XNL(NLCASE)).LT.EIGCON*NR.EIGCON.EQ.0.0) GO TO 510
WRITE(6,511)
511 FORMAT(/ 4X,-EIGENVALUE UPPER LIMIT EXCEEDED IN THIS HARMONIC.-/)
GO TO 500
510 CONTINUE
IF (ABS(ABS(EIG)-1.0).LE.CONVER) GO TO 199
REWIND 1
GO TO 100
199 NPROR=2
CALL BCVECT (NZ,QVEC,NQJS,JRTIC,JRSTOP,NREG)
200 CONTINUE
IF (KBC.NE.0.AND.NH.EQ.0) GO TO 500
CALL INITIAL
REWIND 1
CALL LEBEGE
500 CONTINUE
CONVER = CONV
REWIND 1
NPROR = 0
IF (NH.EQ.0) GO TO 55
ICYC = ICYC+1
IPASS = 0
NPAS = 0
MDET = 0
KDET = 0
F = C
KNBC = KNBC+1
LINPUT = 0
IF (KNBC.LE.JNBC) LINPUT = 1
XN=XN+INC
IF (XN.GT.XN2) GO TO 1
XNL(NLCASE) = 0.0
GO TO 100
55 XNL(1)=1.0
Q = 1
NH = 1
LINPUT = 0
IF (NBC.LT.0) LINPUT = 1
IF (XN.NE.XNL.AND.NBC.GE.2.AND.KBC.EQ.0) LINPUT=1
IF (LINPUT.EQ.0) JNBC = JNBC+1
XN=XN1
IF (NLCASE.EQ.1.AND.XN.NE.0) XNL(1)=0.0
GO TO 100
555 CALL EXIT
8000 TERROR=8000
NERROR=1
8888 CONTINUE
CALL ETRAP
STOP
END

```

201730
201740
201750

201810
201770
201780

201800
201810
201820

201830
201791
201840

201850
201911
201860

201870
201880
201890

201900
201910
201971

201972
201973
201920

201930
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201960

201970
201980
202020

202040
202050
202060

202080
202090
202100

202110
202120
202140

202150
202160

OVERLAY

```

SEG R00T
IN NBF245
IN MAIN,RLDATA
SEG RIF*,(R00T)
IN RIEMAN,SETUP,R00T,GEOMET,PLINE,PLIC0
SEG DF1*,(RIE)
IN DIF1
SEG DF2*,(RIE)
IN DIF2
SEG SGMAT*,(R00T)
IN SGMAT,SREVN2
SEG SWCH*,(R00T)
IN SWITCH,TRIEQ,FUTILE
SEG RING*,(SWCH)
IN RINGER
SEG REG*,(RING)
IN REGMAT,CHASE
SEG STR*,(RING)
IN STRMAT,FLEX
SEG EIG*,(SWCH)
IN EIGVAL,COMPAK,EIGEN,D0TPR0,SYMLEIG,TF0RM,STURM,PREP,QSVEC,DAGGER,ANDD
SEG DET*,(SWCH)
IN DETFRM,DET2,DC0MP2,SUPER
SEG BCV*,(SWCH)
IN BCVECT
SEG INI*,(R00T)
IN INITIAL
SEG LEB*,(R00T)
IN LEBEG,FIXEM,T0BAR,TEM0EG,PLYNE,PLYC0
SEG 0D1*,(LED)
IN 0DE1
SEG 0D2*,(LEB)
IN 0DE2
SEG TRAP*,(R00T)
IN ETRAP

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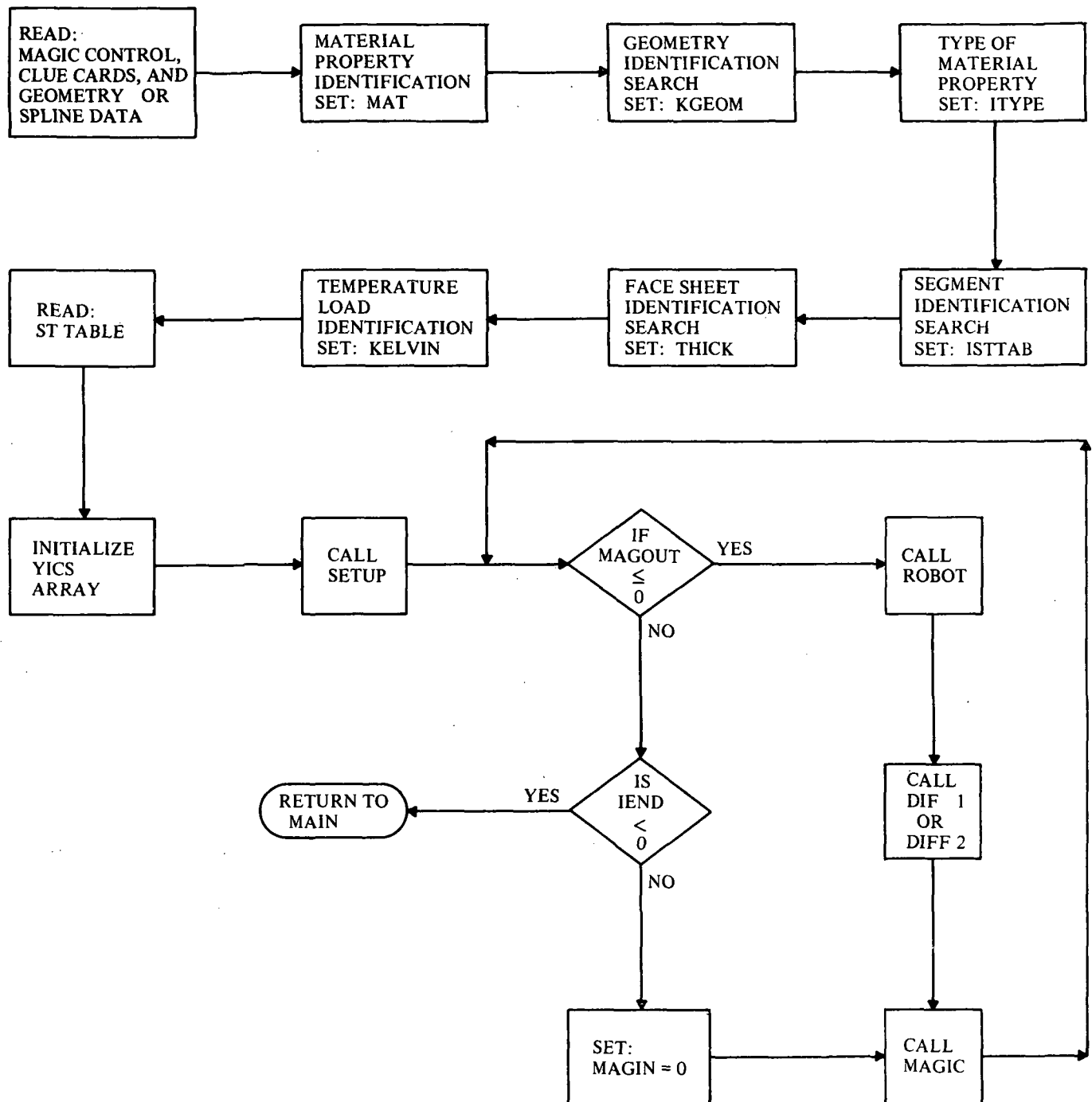
SUBROUTINE RIEMAN

This subroutine link assembles the data tables for use in the integration procedure. The program has the capability of handling 2 loading conditions (dead and live). Temperature load can be included in either one, but not both.

The subprogram link, RIEMAN, utilizes the subroutines SETUP, ROBOT, DIF1 or DIFF2, to integrate the differential equations of each segment independently, under arbitrary load conditions. The results of the integrations of each segment are stored in the YCORR array in RIEMAN, and represent the stiffness and deflection coefficients of each segment.

FORTRAN CODE	ENGINEERING SYMBOLS (REF. 1)
XFTHLD	f_{θ}
XFPHLD	f_{ϕ}
XFZELD	f_{ζ}
XMTHLD	m_{θ}
XMPHLD	m_{ϕ}
ETHET	E_{θ}
EPHI	E_{ϕ}
XGPT	$G_{\phi\theta}$
XNUTP	$\nu_{\theta\phi}$
XNUPT	$\nu_{\phi\theta}$
ALPHTH	α_{θ}
ALPHPH	α_{ϕ}
XNTTH	$N_{T\theta}$
XNTPH	$N_{T\phi}$
XMTTH	$M_{T\theta}$
XMTPH	$M_{T\phi}$
XK11	K_{11}
XK22	K_{22}
XD11	D_{11}
XD22	D_{22}
XK33	K_{33}
XD33	D_{33}

RIEMAN




```

180 READ(5,198) NRZIN,(ZI(J),RI(J),J=1,NRZIN)
198 FORMAT(12,7F10.0/7F10.0)
WRITE(1) NRZIN,(ZI(J),RI(J),J=1,NRZIN)
481 CONTINUE
1003 READ(5,1003) TYPE,HLAYR,SHEET,INTERP,RANKIN,TEFREE,NP
1003 FORMAT(5(A4,6X),E10.1,10X,I2)
IF(NP.LT.-2.0R.NP.GT.30) GO TO 8787
WRITE(1) TYPE,HLAYR,SHEET,INTERP,RANKIN,TEFREE,NP
GO TO 192
191 READ(1) RG0,ANG,STORY
READ(1) DTAU,DIFF,STEP,DELTA
IF (RG0.EQ.14.0) GO TO 182
READ (1) G1,G2,G3
GO TO 183
182 READ(1) NRZIN,(ZI(J),RI(J),J=1,NRZIN)
183 CONTINUE
184 READ(1) TYPE,HLAYR,SHEET,INTERP,RANKIN,TEFREE,NP
192 EPSIL = 1.0E-05
DIFF = 1.0E-04
ERR = 1.0E-07
I = RG0
IF (NH.NE.0) GO TO 920
WRITE(6,651) NSC,I,STORY,DTAU,DIFF,STEP,DELTA
651 FORMAT(/,13X,15HSEGMENT NUMBER ,I2,5X,13HSEGMENT CODE ,I2,5X,
1 16A4//22X,4HDTAU,15X,4HDIFF
2,15X,4HSTEP,10X,5HDELTA//16X,5(E14.7,5X),2X,F2.0)
IF (RG0.EQ.14.0) GO TO 185
WRITE(6,652) G1,G2,G3
652 FORMAT(/,54X,24HGEOMETRY INPUT VARIABLES,//38X,3(E14.7,5X))
GO TO 645
185 WRITE(6,186) (ZI(I),RI(I),I=1,NRZIN)
186 FORMAT(/,57X,24HGEOMETRY INPUT VARIABLES//42X,16HAXIAL COORDINATE,
1 9X,6HRADIUS/50X,1HZ,20X,1HR/(43X,1PIE15.8,5X,1PIE15.8))
645 WRITE(6,653) TYPE,HLAYR,SHEET,INTERP,RANKIN,TEFREE,NP
653 FORMAT(/,12X,5(A4,6X),9H FREE = ,E10.3,12X,
1 26HNUMBER OF TABLE COLUMNS = ,I2)
920 CONTINUE
C MATERIAL PROPERTY IDENTIFICATION
DO 501 I=1,NMPT
IF (HLAYR-STD(I)) 501,502,501
502 MAT=I
501 CONTINUE
C GEOMETRY IDENTIFICATION SEARCH
DO 503 I=1,7
503 DO 504 I=1,7
504 CONTINUE
IF (RG0-STRG(I)) 504,505,504
505 KGEOM=I
DO 506 I=1,3
IF (TYPE-MATER(I)) 506,507,506
507 ITYPE=I
DO 510 I=1,12
IF (INTERP-SEGTab(I)) 510,511,510
510 CONTINUE
GO TO 8088
511 ISTATB=I
DO 508 I=1,4

```

```

508 CONTINUE
509 GOTO 8089
509 THICK=I
KLUE2=I
GOTO (430,430,420,420,420,420,425,425,425,430,430,430),ISTTAB
420 KLUE2=2
GOTO 430
425 KLUE2=3
430 KLUEL=THICK
C TEMPERATURE LOAD IDENTIFICATION
DO 401 I=1,4
IFRANKIN.EQ.THERM(I)GOTO 402
401 CONTINUE
GOTO 8090
402 KELVIN=I
C LINEAR ANALYSIS IDENTIFICATION
IANLYZ = I
NR0W = THICK + 1
IF (.ISTTAB.EQ.1) NR0W = 11
IF (.ISTTAB.EQ.3) NR0W = 13
IF (.ISTTAB.EQ.4) NR0W = 8
IF (.ISTTAB.EQ.5) NR0W = 9
IF (.ISTTAB.EQ.6) NR0W = 10
IF (.ISTTAB.EQ.7) NR0W = 7
IF (.ISTTAB.EQ.8) NR0W = 8
IF (.ISTTAB.EQ.9) NR0W = 9
IF (.ISTTAB.EQ.10) NR0W = 12
IF (.ISTTAB.EQ.11) NR0W = 13
IF (.ISTTAB.EQ.12) NR0W = 14
IF (KBC.NE.0) NR0W = NR0W+2*NLCASE
L= 2*(MAT-1)+1
II=NXMAT(L)
II=NXMAT(L+1)
IF (NH.NE.0) GOTO 921
WRITE(6,654) ((XMAT(I,J),J=1,10),I=1,III)
654 FORMAT(/51X,28H MATERIAL PROPERTY TABLE USED,/(10(IH ,E12.5)))
655 WRITE(6,655)
655 FORMAT(/42X, 47HTABLE ORDER PHI OR S VS. CROSSSECTION PROPERTIES,)
921 CONTINUE
DO 901 I=1,NR0W
IF(IQ.EQ.1) GOTO 193
READ (5,1005) (ST(I,J),J=1,NP)
1005 FORMAT (5E14.7)
WRITE(1) (ST(I,J),J=1,NP)
IF (NH.NE.0) GOTO 901
IF (KBC.EQ.0) GOTO 194
IF (I.EQ.NR0W-2*NLCASE+1) WRITE(6,298)
298 FORMAT(/42X,48HTABLE ORDER PHI OR S VS. INPUT STRESS RESULTANTS)
194 WRITE(6,600) (ST(I,J),J=1,NP)
600 FORMAT(1H ,8(E14.7,2X)/(3X,8(E14.7,2X)))
GOTO 901
193 READ (1) (ST(I,J),J=1,NP)
901 CONTINUE
DO 750 JJ=1,12
750 LST(JJ) = 0
IF (KBC.NE.0) GOTO 590
K=NR0W+1
JJ=1
JJJ=6
MM=1

```

```

NRW = NRW
DØ 17 NLC=1,NLCASE
JT = JJ
JTT= JJJ
L=C
IF(Q.EQ.1) GØ TØ 195
READ(5,1004) (LST(J),J=JJ,JJJ)
1004 FORMAT(611)
WRITE(1) (LST(J),J=JJ,JJJ)
GØ TØ 196
195 READ(1) (LST(J),J=JJ,JJJ)
196 CONTINUE
IF(LST(JJ))8031,19,20
20 L = LST(JJ)
IF (NLC.GT.1.AND.LST(1).NE.0.AND.LST(JT).NE.0) GØ TØ 8008
19 JJ=JJ+1
23 IF(LST(JJ))8031,22,21
21 L=L+1
22 IF(JJ.EQ.JJJ) GØ TØ 24
JJ=JJ+1
GØ TØ 23
24 IF(L.EQ.0) GØ TØ 71
KK = K + L - 1
GØ 72 M=K, KK
IF(Q.EQ.1) GØ TØ 197
READ (5,1005) (STM,J),J=1,NP)
WRITE(1) (STM,J),J=1,NP)
GØ TØ 72
197 READ (1) (STM,J),J=1,NP)
72 CONTINUE
IF (LST(JT).EQ.0) GØ TØ 660
LY = K
KY = K
KZ = K+LST(1)-1
K = KZ+1
IF (NH.NE.0) GØ TØ 665
WRITE(6,656)
656 FORMAT(/745X,42HTABLE ORDER PHI ØR S VS. TEMPERATURE LOADS, )
DØ 657 N=KY,KZ
WRITE(6,600) (ST(N,J),J=1,NP)
657 CONTINUE
660 IF (L-LST(JT)).EQ.0) GØ TØ 665
IF (NH.NE.0) GØ TØ 665
WRITE(6,661) NLC
661 FORMAT(/16X,8HPRØBLEM ,12,5X,84HTABLE ØRDER PHI ØR S VS. DISTRIB
UTED LOADS (F THETA, F PHI, F ZETA, M THETA, M PHI),)
WRITE(6,1968) (LST(J),J=JT,JTT)
1968 FORMAT(27H LOAD IDENTIFICATION CLUES ,611/)
DØ 662 N = K, KK
WRITE(6,600) (ST(N,J),J=1,NP)
662 CONTINUE
665 CONTINUE
71 K = K + L - LST(JT)
IF (NLC.EQ.1.AND.LST(1).EQ.0) NRW = K-1
JJ=JJ+1
JJJ=JJ+5
17 MM=MN+1
590 CONTINUE
IF (Q.EQ.1) GØ TØ 2004
READ (5,591) IS,SAVJTC(IS),SAVSTP(IS),(STØRY(I),I=1,16)
591 FORMAT (315,16A4)

```

```

2000 2000 READ(5,2000)
      F0RMAT(1X)
      WRITE(1) IS,SAVJTC(1S),SAVSTP(1S),ST0RY
      GO TO 2005
2004 READ(1) IS,SAVJTC(1S),SAVSTP(1S),ST0RY
2005 CONTINUE
      ITIC = SAVJTC(1S)
      IST0P = SAVSTP(1S)
      JTIC = JRTIC(NRC)
      JST0P = JRST0P(NRC)
      TIC = ST(1,1)
      ST0P = ST(1,NP)
      NEQNS=64+8*NPR08
      DO 73 I=1,NEQNS
73   YICS(1)=0.0
      YICS(5)=1.0
      YICS(14)=1.0
      YICS(23)=1.0
      YICS(32)=1.0
      YICS(42)=1.0
      YICS(51)=1.0
      YICS(60)=1.0
      NCYC=0
      NSAVE=NR0W
      IEND=0
      PRINT=TIC
      DTA=DTAU
      DTAU = 0.00
      IF (NH.NE.O.AND.KBC.EQ.O) READ(13) SAVY
2001 F0RMAT(1X,1P1E16.7,15,1P6E16.7)
      59 CALL SETUP (MAGIN,MAG0UT,TIC,STEP,NEQNS,DTAU,EPSIL,DELTA,ERR,TIME,
      10TIME,YICS,YPRD,YC0RR,YD0T,YNEH,YDEV,FMDEL,TBDEL)
      GO TO 61
60 CONTINUE
      CALL MAGIC (MAGIN,MAG0UT,TIC,STEP,NEQNS,DTAU,EPSIL,DELTA,ERR,TIME,
      1 10TIME,YICS,YPRD,YC0RR,YD0T,YNEH,YDEV,FMDEL,TBDEL)
61 IF(MAG0UT.LE.O) GO TO 25
      IF(TIME.GT.ST0P) GO TO 62
      IF(TIME.LT.ST0P) GO TO 63
64 IEND=-1
      GO TO 67
62 IF(TIME.LE.(ST0P+DIFF)) GO TO 64
      GO TO 8001
63 IF((ST0P-DIFF).LE.TIME) GO TO 64
      IF(11TIME+DTIME).GT.ST0P) GO TO 65
      IF(PRINT.GT.TIME) GO TO 66
      PRINT=TIME+DTA
67 CONTINUE
      IF(IEND.GT.O) GO TO 8002
      IF(IEND.LT.O) GO TO 150
66 CONTINUE
      MAGIN = 0
      GO TO 60
65 DTIME=ST0P-TIME
      DELTA = 0.00
      GO TO 67
75 NCYC=NCYC+1
      MAGIN=-1
      GO TO 60
      25 LT=0

```

```

303070 IF (NH-NE.0.AND.KKNT.EQ.4.AND.KBC.EQ.0) READ(13) SAVY
303080 JJ = NLCASE*6
303090 DO 15 J=1,JJ
303100 15 LT=LT+ST(J)
303110 296 NTOTAL = LT+NSAVE
303120 PHI=TIME
303130 ARG=PHI
303140 LL=NP+1
303150 DO 51 I=1,NP
303160 IF(ARG-ST(1,1)) 52,55,51
303170 52 IF(I-1) 55,55,54
303180 51 CONTINUE
303190 I=NP
303200 GO TO 55
303210 54 GO 57 IK=2,NTOTAL
303220 57 ST(IK,LL)=ST(IK,I-1)+(ST(IK,I)-ST(IK,I-1))*(ARG-ST(1,1-1))/(ST(1,1-1)-ST(1,1-1))
303230 1)-ST(1,1-1))
303240 GO TO 80
303250 55 DO 58 IK=2,NTOTAL
303260 58 ST(IK,LL)=ST(IK,I)
303270 80 CONTINUE
303280 C THE UPDATED INTERPOLATED VALUES OF THE MATERIAL PROPERTY COEFFIC
303290 C IENTS ARE FOUND IN THE XMAT TABLE AND STORED IN THE XLAYER ARRAY
303300 L = (MAT-1)*2+1
303310 II=NXMAT(L)
303320 III=NXMAT(L+1)
303330 LL=NP+1
303340 L=NR0W + 1
303350 IF(KELVIN.NE.1)GO TO 81
303360 IF(THICK.NE.1)GO TO 83
303370 81 LOOP=1
303380 IL0W=1
303390 IHIGH = 1
303400 IF(KELVIN.NE.1)GO TO 85
303410 82 CONTINUE
303420 TMPAV(IL0W)=(ST(L,LL)+ ST(L+1,LL)+ ST(L+2,LL) + ST(L+3,LL))/4.0
303430 GO TO 85
303440 83 LOOP = 2
303450 IL0W = 1
303460 IHIGH = 2
303470 TMPAV(IL0W)= (ST(L,LL)+ ST(L+1,LL))/2.0
303480 TMPAV(IHIGH)=(ST(L+2,LL) + ST(L+3,LL))/2.0
303490 85 DO 105 IL=IL0W,IHIGH
303500 M=1
303510 GO TO (91,92,93),KELVIN
303520 91 ARG= TMPAV(IL)
303530 GO TO 94
303540 93 CONTINUE
303550 ARG = ST(NR0W+1,LL)
303560 TMPAV(I) = ARG
303570 DO 104 I = 2,10
303580 IF (ARG-XMAT(I,I)) 121,123,104
303590 121 IF (I-2) 8007,8007,124
303600 104 CONTINUE
303610 GO TO 8067
303620 123 L=I+1
303630 DO 122 J=L,III
303640 XLAYER(M)=XMAT(J,I)
303650 122 M=M+1
303660 GO TO 111
303670 124 L=I+1

```



```

D0 125 J=L,III
XPLAYER(M)=XMAT(J,I-1)+(XMAT(J,I)-XMAT(J,I-1))*(ARG-XMAT(III,I-1))/
1 (XMAT(III,I)-XMAT(III,I-1))
125 M=M+1
92 G0 T0 111
92 L = II + 1
D0 922 J=L,III
XPLAYER(M)= XMAT(J,I)
922 M=M+1
111 G0 T0 (115,115,112,113,114),L00P
112 XNUTP= XPLAYER(2)
IFI(ITYPE,NE, 1)G0 T0 131
XNUTP= XNUTP
XGPT(1) = ETHET(1)/(2*(1+ XNUTP))
XGPT(2) = ETHET(2)/(2*(1+ XNUTP))
G0 T0 106
131 XNUTP = XPLAYER(3)
XNUTP = ETHET(1)*XNUTP/EPHI(1)
G0 T0 106
113 ES= XPLAYER(8)
ALPHS=XPLAYER(10)
G0 T0 106
114 ALPHR = XPLAYER(9)
ER = XPLAYER(7)
G0 T0 118
115 G0 T0(101,102,103),ITYPE
101 ETHET(1L)= XPLAYER(1)
XNUTP = XPLAYER(2)
ALPHTH(1L)= XPLAYER(3)
EPHI(1L) = ETHET(1L)
XNUTP= XNUTP
ALPHPH(1L)= ALPHTH(1L)
XGPT(1L)= ETHET(1L)/(2.0*(1.0+ XNUTP))
G0 T0 105
102 ETHET(1L)= XPLAYER(1)
EPHI(1L) = XPLAYER(2)
XNUTP= XPLAYER(3)
ALPHTH(1L)= XPLAYER(4)
ALPHPH(1L)= XPLAYER(5)
XGPT(1L) = XPLAYER(6)
XNUTP= ETHET(1L)* XNUTP/EPHI(1L)
G0 T0 105
103 ETHET(1L)= XPLAYER(1)
EPHI(1L)= XPLAYER(2)
XNUTP= XPLAYER(3)
ALPHTH(1L) = XPLAYER(4)
ALPHPH(1L) = XPLAYER(5)
XGPT(1L) = XPLAYER(6)
ER= XPLAYER(7)
ES= XPLAYER(8)
ALPHR = XPLAYER(9)
ALPHS = XPLAYER(10)
XNUTP = ETHET(1L) * XNUTP/EPHI(1L)
105 CONTINUE
106 L = NR0W+1
G0 T0 (117,107,108,119,118),L00P
107 L00P= 3
IL0W = 3
HIGH= 3
G0 T0 82
108 IF(ITYPE .EQ.3 .AND. ISTATB .GE. 3)G0 T0 109

```



```

C
C
C
XFEZEL1 = 0.0
XFPHL2 = 0.0
XFEZEL2 = 0.0
ANALYS=LINE
ANALYS=DMTH
ANALYS=NPH
XNPH1= 0.0
DØ 77 M=1, JF
I = (M-1)*8 + 1
IF (I.EQ.1.AND.NH.NE.0) GØ TØ 252
IF (M.LT.9) GØTØ 49
IF (M.EQ.9.AND.LST(1).EQ.0) GØ TØ 252
XNTH = XSAVE1
XNTPH = XSAVE2
XNTH = XSAVE3
XNTPH = XSAVE4
252 DØ 250 JKL=1, NLCSE
PL=NL+1
XFTHLD=0.0
XFPHLD=0.0
XFEZLD=0.0
XNTHLD=0.0
XMPHLD=0.0
IR=NL*6-5
IF(LST(IR).NE.0) K=K+LST(IR)
IF (LST(IR+1).EQ.0) GØTØ 44
K=K+1
XFTHLD=ST(K,LL)
44 IF(LST(IR+2).EQ.0) GØTØ 45
K=K+1
XFPHLD=ST(K,LL)
45 IF(LST(IR+3).EQ.0) GØTØ 46
K=K+1
XFEZLD=ST(K,LL)
46 IF(LST(IR+4).EQ.0) GØTØ 47
K=K+1
XNTHLD=ST(K,LL)
47 IF(LST(IR+5).EQ.0) GØTØ 48
K=K+1
XMPHLD=ST(K,LL)
48 CONTINUE
IF (JKL.EQ.2) GØ TØ 251
XFPHL1 = XFPHLD
XFEZEL1 = XFEZLD
251 XFPHL2 = XFPHLD
XFEZEL2 = XFEZLD
250 CONTINUE
49 IF(1STTAB.GE.3.AND.1STTAB.LE.9)GØ TØ 4002
CALL DIF1 (XFPHL1,XFEZEL1,XFPHL2,XFEZEL2)
GØ TØ 77
4002 CALL DIF2 (XFPHL1,XFEZEL1,XFPHL2,XFEZEL2)
77 CONTINUE
GØTØ 75
8001 IERRØR=8001
NERRØR=11
GØTØ 8888
8002 IERRØR=8002
NERRØR=12
GØTØ 8888
8007 IERRØR=8007
NERRØR=15
304930
304940
304950
304960
304970
304980
304990
305000
305010
305020
305030
305041
305040
305050
305060
305070
305080
305090
305100
305110
305120
305130
305140
305150
305160
305170
305180
305190
305200
305210
305220
305230
305240
305250
305260
305270
305280
305290
305300
305310
305320
305330
305340
305350
305360
305370
305380
305390
305400
305410
305420
305430
305440
305450
305460
305470
305480
305490
305500
305510
305520

```

8008 CØTØ 8888
 8008 IERRØR = 8008
 NERRØR=10
 CØTØ 8888
 8031 IERRØR=8031
 NERRØR= 9
 CØTØ 8888
 8036 IERRØR=8036
 NERRØR = 2
 CØTØ 8888
 8086 IERRØR=8086
 NERRØR= 3
 CØTØ 8888
 8087 IERRØR=8087
 NERRØR= 4
 CØTØ 8888
 8088 IERRØR=8088
 NERRØR=27
 CØTØ 8888
 8089 IERRØR=8089
 NERRØR= 5
 CØTØ 8888
 8090 IERRØR=8090
 NERRØR= 6
 CØTØ 8888
 8067 IERRØR=8067
 NERRØR=16
 CØTØ 8888
 8101 IERRØR = 8101
 NERRØR=17
 CØTØ 8888
 8102 IERRØR = 8102
 NERRØR=18
 CØTØ 8888
 8103 IERRØR = 8103
 NERRØR=19
 CØTØ 8888
 8104 IERRØR = 8104
 NERRØR=20
 CØTØ 8888
 8105 IERRØR = 8105
 NERRØR=21
 CØTØ 8888
 8106 IERRØR = 8106
 NERRØR=22
 CØTØ 8888
 8107 IERRØR = 8107
 NERRØR=23
 CØTØ 8888
 8108 IERRØR = 8108
 NERRØR=24
 CØTØ 8888
 8109 IERRØR = 8109
 NERRØR=25
 CØTØ 8888
 8110 IERRØR = 8110
 NERRØR=26
 CØTØ 8888
 8787 IERRØR = 8787
 NERRØR=34
 8888 NIX=1

305530
 305540
 305550
 305560
 305570
 305580
 305590
 305600
 305620
 305630
 305640
 305650
 305660
 305670
 305680
 305690
 305700
 305710
 305720
 305730
 305740
 305750
 305760
 305770
 305780
 305790
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 305810
 305820
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 305840
 305850
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 305870
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 305890
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 305940
 305950
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 305980
 305990
 306000
 306010
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 306090
 306100
 306110
 306120
 306130

```

RETURN
150 CONTINUE
  IF (NH-NE-0) GO TO 925
  WRITE(6,670)
670  FORMAT(/40X,41HMATRIX X AND Y (TRANSP0SED)  MAGIC 0UTPUT)
672  WRITE(6,672) (YC0RR(I),I=1,NEQMS)
925  CONTINUE
  REST0P=R0
  RADUS(IIST0P) = R0
  TADUS(IIST0P)=R0
  AMAT(IIST0P,1) = SAVY(7)
  AMAT(IIST0P,2) = SAVY(8)
  IF (NSC.LT-NSEG) GO TO 9999
  SADUS(IIST0P) = R0
  UADUS(IIST0P)=R0
  AMAT(IIST0P,3) = SAVY(7)
  AMAT(IIST0P,4) = SAVY(8)
  IF (ITIC.LE-IIST0P) GO TO 9999
  SADUS(IIST0P)=RADUS(ITIC)
  UADUS(IIST0P)=RADUS(ITIC)
9999 CONTINUE
RETURN
9998 WRITE(6,9997)
9997 FORMAT(-THE PROGRAM HAS PR0CESSED ALL THE DATA F0R A CHAIN 0F UNC0
          IUPLED SEGMENTS-)
      ST0P
      END

```

306140
306150
306190
306220
306230
306240
306250
306260
306270
306280
306290
306300
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306320
306330
306340
306350
306360
306370
306380
306390

306430
306440
306450
306460
306470
306480

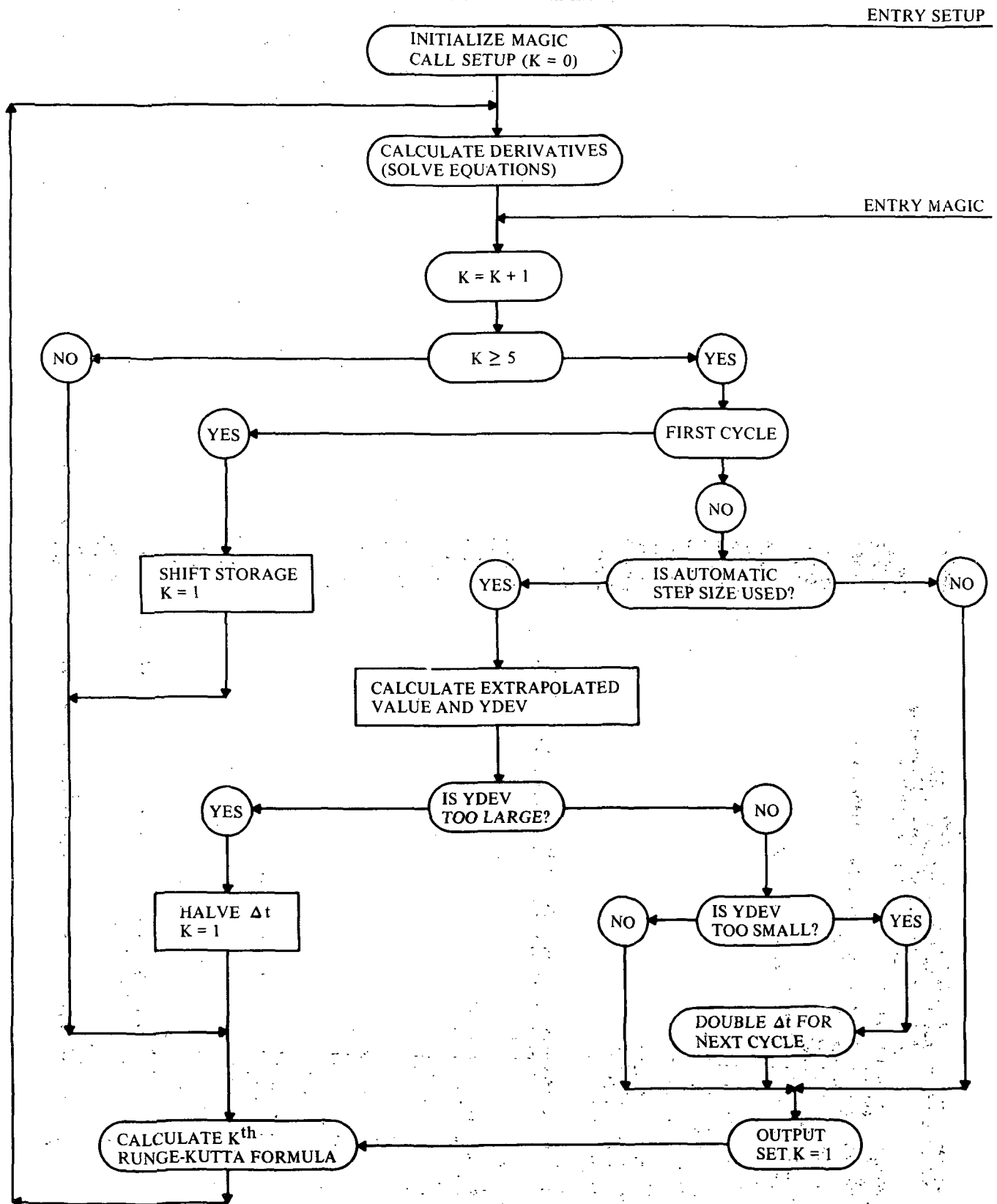
SUBROUTINE SETUP

SETUP is a double entry subroutine called from RIEMAN. It is a mixed precision, numerical integration routine, with automatic selection of a variable integration step size, which utilizes fifth order Runge-Kutta equations to obtain the solution for first order differential equations.

SUBROUTINE MAGIC

MAGIC is an alternate entry point to subroutine SETUP.

RUNGE-KUTTA GENERAL FLOW CHART



```

C ..... ROUTINE **DA ** ABACUS UPDATED 07/07/72 .....
SUBROUTINE SETUP (MAGIN,MAGOUT,TIC,STEP,NEQNS,DTAU,
1 EPSIL,DELTA,ERR,TIME,DTIME,YICS,YPRD,
2 YCRR,YDRT,YNEW,YDEV,FWDEL,TBDEL)
IMPLICIT REAL*8 (A-H,B-Z)
ABSIX = DABSIX)
DIMENSION YICS(1),YPRD(1),YCRR(1),YDRT(1),YNEW(1),
1 YDEV(1),FWDEL(1),TBDEL(1)
DIMENSION C(3),D(3)
COMMON /MAGIK/ KKNT
DOUBLE PRECISION YNEW,YPRD
DATA C,D/500.,500.,1000.,500.,0.00,500/
TIME = TIC
TAU = TIC
IF (DELTA)200,201,200
200 DTIME = 0.0078125
GO TO 225
201 DTIME = STEP
225 DO 102 I = 1,NEQNS
YDEV(I) = 0.0
YPRD(I) = YICS(I)
YCRR(I) = YICS(I)
102 YNEW(I) = YICS(I)
MAGOUT = -2
GO TO 264
555 CONTINUE
ENTRY MAGIC (MAGIN,MAGOUT,TIC,STEP,NEQNS,DTAU,EPSIL,DELTA,ERR,
1 TIME,DTIME,YICS,YPRD,YCRR,YDRT,YNEW,YDEV,FWDEL,
2 TBDEL)
5556 CONTINUE
MSET = 2
IF (MAGOUT) 305,101,101
101 IF (MAGIN) 21, 27, 14
27 K = 0
DO 202 I = 1,NEQNS
202 YNEW(I) = YPRD(I)
21 K = K + 1
KKNT = K
210 DO 2 I = 1,NEQNS
GO TO (9,6,7,4,11),K
9 FWDEL(I) = YDRT(I)
GO TO 105
6 TBDEL(I) = YDRT(I)
GO TO 105
7 TBDEL(I) = TBDEL(I) + YDRT(I)
105 YPRD(I) = YNEW(I) + C(K)*DTIME*YDRT(I)
GO TO (2,2,400),K
400 YCRR(I) = YPRD(I)
2 CONTINUE
TIME = TIME + D(K)*DTIME
99 MAGOUT = 0.0
264 RETURN
400 8 I = 1,NEQNS
YPRD(I) = YNEW(I) + DTIME*(FWDEL(I) + 2*TBDEL(I) + YDRT(I))/6.
8 YDEV(I) = YCRR(I) - YPRD(I)
GO TO 99
11 IF (DELTA)80, 5,80
80 DO 13 I = 1,NEQNS
IF (EPSIL* ABS(YCRR(I)) + ERR - ABS(YDEV(I)))14, 13, 13
13 CONTINUE

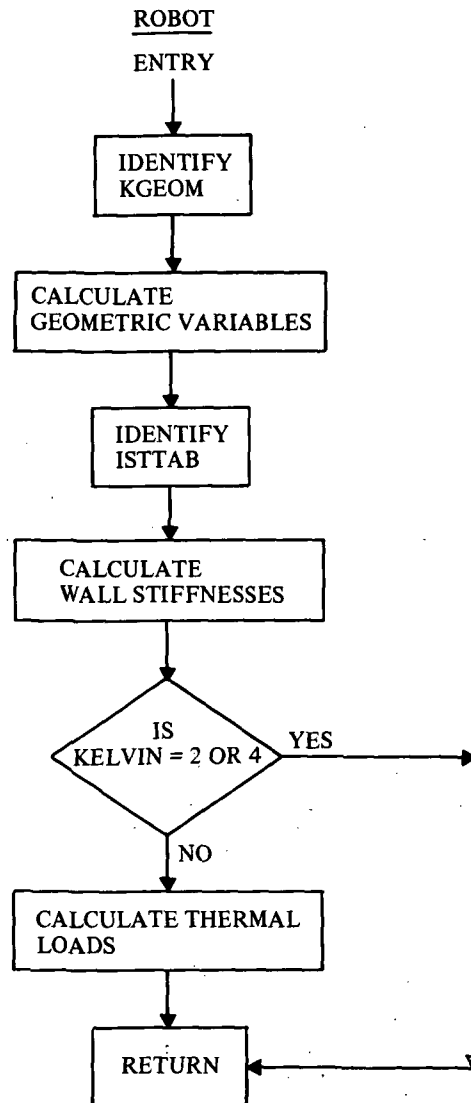
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FORTRAN CODE

ENGINEERING SYMBOLS (REF. 1.)

RO	r_0
RL	r_l
RLDOT	$r_{l,\phi}$
CS	$\cos \phi$
SN	$\sin \phi$
A	a
C	c
XN	n
F2	f_2
F3	f_3
TAN; TN	$\tan \phi$
SEC	$\sec \phi$
TII	T_{ii}
TIK	T_{ic}
TOK	T_{oc}
TOO	T_{oo}
TEFREE	\bar{T}
HI	h_i
HO	h_o
T	t
TI	t_i
TO	t_o
SNSQ	$\sin^2 \phi$
CSSQ	$\cos^2 \phi$
CN	$\cos \phi \sin \phi$
X1CS	$1/\cos \phi$
X1SN	$1/\sin \phi$
R2	r_2
BETA	β

FORTRAN CODE	ENGINEERING SYMBOLS (REF. 1)
X1ROSN	$1/r_0 \sin \phi$
X1ROCS	$1/r_0 \cos \phi$
CSX1R0	$\cos \phi/r_0$
CSX1R1	$\cos \phi/r_1$
CSX1R2	$\cos \phi/r_2$
SNX1R0	$\sin \phi/r_0$
SNX1R1	$\sin \phi/r_1$
X1R1	$1/r_1$
X1R2	$1/r_2$
X1R1SQ	$1/r_1^2$
X1ROSQ	$1/r_0^2$



```

C ..... ROUTINE ** R080T ** ABACUS UPDATED 07/24/72 .....
SUBROUTINE R080T (ST,KLUE2,NR0W,NRW,LL,ER,ES,G2,G3,TIME,ITIC,JTIC,
1
1 INTEGER SAVJTC,SAVSTP,Q,THICK
INTEGER XN1,XN2,XN
REAL*4 I2
DOUBLE PRECISION SAVTIC,TIC,PHI,ST0P,REST0P,RTICK
DOUBLE PRECISION TEMPI,TEMP2,TEMP3,TEMP4,TEMP5,TEMP8,TEMP10,TEMP11
DOUBLE PRECISION YD0T,YASAVE,YANTH,YAMTH,YAJPH,S,SN,CS,SN SQ,
DOUBLE PRECISION CQQ,TAN,SEC,CN,XICS,XLSN,TN,XIR0,XIR0SQ,XISNR0,
1
2 XICSR0,CNIR0,SNIR0,CSIR0,XIR1,XIR2,CSIR1,CSIR2,
3 SNR1,XIR1SQ,R2SQ,R0,BESQ,R0SQ,XNSQ,R1,R2,S1,
4 R1D0T,XNITH,XNTPH,XMTH,XMTPH,XC11,XC22,XC15,
5 XD33,XD22,XD21,XD12,XK11,XK12,XK21,XK22,XK33,
6 XD11,XNPHI,BETA,XC16
DOUBLE PRECISION YPRED,TIME
COMMON ST0RY(16),XMAT(110,10),STD(10),SADUS(30),RADIUS(30)
COMMON TADUS(30),UADUS(30),SAVTIC(900)
COMMON XN,TEREE,TIC,PHI,ST0P,REST0P,RTICK,G1,XNL(2),NH
COMMON NST(30),NKL(30),XMAT(20),SAVJTC(30),SAVSTP(30),JRTIC(30)
COMMON JRST0P(30),NREG,NMPT,NRC,NSC,NIX,TERK0R,KGE0M,ISTAB
COMMON KELVIN,IBEGIN,NPR0B,NSEG,NERR0R,Q,THICK,N0JS,NLINKS,NLCASE
COMMON NTSKL,NZ,NBCT,LINPUT,NTRKL,NPASS,XN1,KBC,NRINGS
COMMON /EQUAZN/ YPRED(80),YD0T(80),YASAVE(80),YANTH,YAMTH,
1
2 YAMPT,YAJPH,S,SN,CS,SN SQ,CQQ,TAN,SEC,CN,XICS,XLSN,TN,
3 XIR0,XIR0SQ,XISNR0,XICSR0,CNIR0,SNIR0,CSIR0,XIR1,XIR2,
4 CSIR1,CSIR2,SNIR1,XIR1SQ,R2SQ,R0,BESQ,R0SQ,XNSQ,BETA,R1,
5 R2,S1,R1D0T,XNITH,XNTPH,XMTH,XMTPH,XFTHLD,XFPHLD,XFZELD,
6 XMHLD,XMPHLD,ETHET(2),EPI(2),XGPT(2),ALPHTH(2),
7 ALPHTH(2),DUM,XNUTP,XNUPT,
8 XC11,XC22,XC15,XD33,XD22,XD21,XD12,XK11,XK12,XK21,XK22,
9 XK33,XD11,XNPHI,M,I,BETA,ZETTA,SAVY(8),XC16
COMMON /SPLNS/ ANG,PSI(100),RAD(100),CUR1(100),CUR2(100),
1
2 DRIDP(100),ZI(14),RI(14),NRZIN
COMMON /ARING/ NRING(28),AMATT(30,4)
DIMENSION ST(72,31)
DATA A/--A --/
IF (KBC.EQ.0) G0 T0 500
L = 1
IF (NLCASE.EQ.1) G0 T0 800
L = 3
SAVY(4) = ST(NRW-1,LL)
SAVY(5) = ST(NRW,LL)
SAVY(6) = 0.0
800 SAVY(1) = ST(NRW-L,LL)
L = L-1
SAVY(2) = ST(NRW-L,LL)
SAVY(3) = 0.0
500 CONTINUE
C
G0T0 (771,772,773,774,775,776,7077),KGE0M
C GEOMETRY FOR ELIPSE(G3=0FFSET DISTANCE )
771 A=G1
BE=G2
BETA = BE
BESQ=BE**2
ASQ=A**2
SN = DSIN(PHI)
CS = DCOS(PHI)
SNSQ = SN**2
2600000
2500010
2500020
2500040
2500060
2500090
2500100
2500110
2500120
2500130
2500140
2500170
2500180
2500190
2500200
2500210
2500220
2500230
2500240
2500250
2500260
2500270
2500280
2500290
2500300
2500310
2500330
2500340
2500350
2500360
2500370
2500380
2500390
2500400
2500410
2500420
2500430
2500440
2500450
2500460
2500470
2500480
2500490
2500500
2500510
2500520
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2500540
2500550
2500560
2500570
2500580
2500590
2500600

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C 772 R1=G1
C=G2
SN = DSIN(PHI)
CS = DCOS(PHI)
IF (SN.EQ.0.0) GOTO 777
R2=R1-C/SN
GOTO 778
777 R2 = 1.0
778 R0 = R1*SN-C
R100T=0.0
GOTO 7775
C 773 CS = COS(G1)
SN=SIN(G1)
S=PHI
SI=1.0/S
R2=CS*SN*PHI
R0=PHI*CS
R100T=0.0
GOTO 7775
C 774 R0 = G1
R100T=0.0
SN = 1.0
CS = 1.0
GOTO 7775
C 775 XNEXP = G1
A = G2
XN1 = 1.0 + XNEXP
XN2 = 1.0/XN1
XN3 = XN1 + 1.0
XN4 = XN3 + 1.0
XN5 = XN4/XN1
SN = DSIN(PHI)
CS = DCOS(PHI)
R2 = A*(2.0/(1.0+SN**XN1))**XN2
R1 = (A/2.0)*(R2/A)**XN3
R0=R2*SN
R100T = -XN3*A*(SN**XNEXP*CS/4.0)*(2.0/(1.0+SN**XN1))**XN5
GOTO 7775
C 776 GENERAL GEOMETRY

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```

776 SN = DSIN(PHI)
   CS = DCOS(PHI)
   TAN= SN/CS
   SEC= 1.0/CS
   IF (TIME.EQ.TIC) CALL GEOMET
   ARG = PHI
   D0 204 J=1,100
   PH0 = PSI(J)
   IF (ANG.EQ.A) IF (ARG-PH0) 221,223,204
   IF (PH0-ARG) 221,223,204
221 IF (J-1) 8502,8502,224
204 CONTINUE
   G0 T0 8503
223 R0 = RAD(J)
   R1 = CUR1(J)
   R2 = CUR2(J)
   RIDOT = DRIDP(J)
   G0 T0 7775
8502 NERR0R = 41
   G0 T0 8888
8503 NERR0R = 42
8888 NIX = 1
   G0 T0 8889
224 SUB1 = ARG-PSI(J-1)
   SUB2 = PSI(J)-PSI(J-1)
   R0 = RAD(J-1)+(RAD(J)-RAD(J-1))*SUB1/SUB2
   R1 = CUR1(J-1)+(CUR1(J)-CUR1(J-1))*SUB1/SUB2
   R2 = CUR2(J-1)+(CUR2(J)-CUR2(J-1))*SUB1/SUB2
   RIDOT = DRIDP(J-1)+(DRIDP(J)-DRIDP(J-1))*SUB1/SUB2
   G0 T0 7775
C      ISOTENS0ID GEOMETRY
7077 CONTINUE
   SN = DSIN(PHI)
   CS = DCOS(PHI)
   A = G1
   R2 = A/DSQRT(SN)
   R1 = 0.5 * R2
   R0 = R2 * SN
   RIDOT = - ((A**2)*0.5)*(R1*CS)/R0**2
7775 TAN=SN/CS.
   IF (TIME.EQ.TIC) RTICK=R0
   IF (NCYC.GT.1) G0 T0 491
   IF (TIME.NE.TIC) G0 T0 491
   RADUS(ITIC) = R0
   AMAT(ITIC,1) = SAVY(7)
   AMAT(ITIC,2) = SAVY(8)
   IF (NSC.NE.1) G0 T0 491
   SADUS(JTIC) = R0
   AMAT(JTIC,3) = SAVY(7)
   AMAT(JTIC,4) = SAVY(8)
491 CONTINUE
   R0SQ = R0**2
   XNSQ=XN**2
   CN=CS*SN
   XICS=1.0/CS
   TN=SN/CS
   XIR0=1.0/R0
   XIR0SQ=1.0/R0**2
   XICSR0=1.0/(CS*R0)
   CNIR0=CN/R0
   SNIR0=SN/R0

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2501220
2501230
2501240
2501250
2501260
2501270
2501280
2501290
2501300
2501310
2501320
2501330
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2501350
2501360
2501370
2501380
2501390
2501400
2501410
2501420
2501430
2501440
2501450
2501460
2501470
2501480
2501490
2501500
2501510
2501520
2501530
2501540
2501550
2501560
2501570
2501580
2501590
2501600
2501610
2501620
2501630
2501640
2501650
2501660
2501670
2501680
2501690
2501700
2501710
2501720
2501730
2501740
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2501760
2501770
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2501790
2501800
2501810
2501820

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```

CS1R0=CS/R0
SNSQ=SN**2
CSSQ=CS**2
IF(KGE0M.EQ.4.0R.KGE0M.EQ.3) G0T0 79
R1SQ = R1**2
R2SQ = R2**2
X1SN=1.0/SN
X1SNR0=1.0/(SN*R0)
X1R1=1.0/R1
X1R2=1.0/R2
CS1R1=CS/R1
CS1R2=CS/R2
SNR1=SN/R1
X1R1SQ=1.0/R1**2
79 XNTI1=0.0
XNTPH=0.0
XMTI1=0.0
XMTPH = 0.

C
C
C COMPUTATION OF K AND D FOR MATERIAL PROPERTY INPUT
C
C0 T0 (711,600,711,32,33,34,35,36,37,28,29,30),ISTAB
THICK
600 G0 T0 (703,702,701,701),THICK
701 H0= ST(4,LL)
702 T = ST(3,LL)
703 H1= ST(2,LL)
G0 T0 40
C
ST11,ST12,ST13
30 H0= ST(14,LL)
29 T = ST(13,LL)
28 H1= ST(12,LL)
GJPH= ST(2,LL)
GJTH= ST(3,LL)
APH = ST(4,LL)
ATH = ST(5,LL)
CPH = ST(6,LL)
CTH = ST(7,LL)
XIPH = ST(8,LL)
XITH= ST(9,LL)
SPH = ST(10,LL)
STH = ST(11,LL)
G0 T0 40
C
HWAFL,RWAF2,RWAF3
34 H0 = ST(10,LL)
33 T = ST(9,LL)
32 H1 = ST(8,LL)
APH = ST(2,LL)
CPH = ST(3,LL)
XIPH= ST(4,LL)
SPH = ST(5,LL)
HETIA=ST(6,LL)
ZETIA = ST(7,LL)
ATH = APH
CTH = CPH
XITH= XIPH
STH = SPH
G0 T0 40
C
ISG1,ISG2,ISG3
37 H0 = ST(9,LL)
36 T = ST(8,LL)

```

```

35 HI = ST(7,LL)
   APH = ST(2,LL)
   CPH = ST(3,LL)
   XIPH = ST(4,LL)
   SPH = ST(5,LL)
   BETTA = ST(6,LL)
   ATH = APH
   CTH = CPH
   XITH = XIPH
   STH = SPH
   GO T0 40
C ST10,RWAF
C RANKIN=THSTND MEANS INTERPOLATE, COMPUTE NTEMP, MTEMP
C RANKIN=NOTHRM MEANS DO NOT INTERPOLATE, DO NOT COMPUTE NTEMP, MTEMP
C RANKIN=THCNST MEANS DO NOT AVERAGE, BUT INTERPOLATE, COMPUTE
C NTEMP, MTEMP
C RANKIN=THINH0 MEANS INTERPOLATE, BUT DO NOT COMPUTE NTEMP, MTEMP
C
711 CONTINUE
   XK11=ST(2,LL)
   XK12=ST(3,LL)
   XK22 = ST(4,LL)
   XK33 = ST(5,LL)
   XD11 = ST(6,LL)
   XD12 = ST(7,LL)
   XD22 = ST(8,LL)
   XD33 = ST(9,LL)
   XC11 = ST(10,LL)
   XC22 = ST(11,LL)
   XC15 = ST(12,LL)
   XC16 = ST(13,LL)
   XK21 = XK12
   XD21 = XD12
   GO T0 103
C
40 CONTINUE
   TEMP3= (1.0-XNUPT * XNUTP)
   PERM= TEMP3
   E1= (ETHET(1)+ EPHI(1))/2.
   E2= (ETHET(2)+ EPHI(2))/2.
   F51= E1+E2
   GO T0 (42,47,49,41),THICK
41 GO T0 (103,42,103,42,47,49,42,47,49,42,47,49),ISTTAB
C
C SINGLE SHEET
C
42 TEMPI= ETHET(1) * HI
   TEMP2= TEMP1 * HI**2
   XK11= TEMPI/TEMP3
   XD11= TEMP2/(12.0* TEMP3)
   TEMPI= EPHI(1)* HI
   TEMP2= TEMPI*HI**2
   XK22= TEMPI/TEMP3
   XD22= TEMP2/(12.0* TEMP3)
   XK33= XGPT(1)* HI
   XD33= XK33*HI**2/12.0
   GO T0 55
C
C EQUAL SHEETS
C
47 EPSUM= FPHI(1)+ EPHI(2)

```


LSUM= ETHET(1)+ ETHET(2)
 XK11= ETSUM * HI/PERM
 XK22= EPSUM * HI/PERM
 XK33= HI*(XGPT(1)+ XGPT(2))
 ZBRIN = (HI*(EI+3.0*E2)+2.0*E2*TI)/(2.0*ESI)
 ZBRUT = (HI*(E2+3.0*EI)+2.0*EI*TI)/(2.0*ESI)
 ZBRUT = (ZBRIN-HI/2.0)**2
 ZBRUT = (ZBRIN-HI/2.0)**2
 XD33= (HI**3*(XGPT(1)+XGPT(2)))/12.0+ HI*(XGPT(1)+ ZBRIN
 + XGPT(2)* ZBRUT)
 1 XD11=(XK11* HI**2)/12.+ HI*(ETHET(1) * ZBRIN + ETHET(2)*ZBRUT)
 1/PERM
 XD22=(XK22* HI**2)/12.+ HI*(EPHI(1) * ZBRIN + EPHI(2)* ZBRUT)
 1/PERM
 GO TO 55
 UNEQUAL FACE SHEETS
 49 CONTINUE
 ZBRIN = (EI*HI**2)+(E2*H0**2) + (2.0*E2*H0*HI) + (2.0*E2*H0*TI) /
 1 (2.0*(EI*HI+E2*H0))
 ZBRUT = (EI*HI**2)+(E2*H0**2) + (2.0*EI*H0*HI) + (2.0*EI*HI*TI) /
 1 (2.0*(EI*HI+E2*H0))
 ZBRIN = (ZBRIN-HI/2.0)**2
 ZBRUT = (ZBRUT-H0/2.0)**2
 XK11= (ETHET(1)* HI + ETHET(2)* H0)/PERM
 XK22= (EPHI(1)* HI + EPHI(2)* H0)/PERM
 XK33= XGPT(1)*HI + XGPT(2)* H0
 XD33 = (XGPT(1)*HI**3+XGPT(2)*H0**3)/12.+HI*(XGPT(1)+ZBRIN)+
 1 XGPT(2)*ZBRUT*H0
 011 = (ETHET(1)*HI**3 + ETHET(2)*H0**3)/12.
 XD11=(011+ (HI*ETHET(1)*ZBRIN) + (H0*ETHET(2)*ZBRUT))/PERM
 D22 = (EPHI(1)* HI**3 + EPHI(2)*H0**3)/12.
 XD22= (D22 +(HI*EPHI(1)*ZBRIN) + (H0*EPHI(2)* ZBRUT)) /PERM
 DETERMINE COMPLETE CONSTANTS DEPENDENT ON REINFORCEMENT CLUE
 55 CONTINUE
 IF(ISTAR.EQ.2)GO TO 103
 EASTH=ER*ATH/STH
 EASPH=ES*APH/SPH
 EISPH= ES* XIPH/SPH
 E1STH= ER* XITH/STH
 CLUE12 (58,60,100),CLUE2
 ST CLUE(10,11,12)
 58 CONTINUE
 XK12= XK11*XNUTP
 XK11= XK11+ EASTH
 XK22= XK22+ EASPH
 XC11= EASTH*CTH
 XC22= EASPH*CPH
 XD22= - XD22 - EISPH
 XD33= XD33 + GJPH/(4.0*SPH)+ GJTH/(4.0*STH)
 XD12= -XD11*XNUTP
 XD11= -XD11- E1STH
 XK21= XK12
 XD21= XD12
 GO TO 103
 RAF CLUE(1,2,3)
 59 CONTINUE

```

60 CONTINUE
  SINB = SIN(BETTA)
  COSB = COS(BETTA)
  SN2T04 = 2*(SINB**4.)
  D = STH*(COSB+SINB)
  ED = ER*ATH/D
  SINB2 = SINB**2.
  HL = 2.0*(ABS(ZETTA)-ABS(CTH))
  I2 = (ATH**3.)/(I3* HL**2)
95 XC22 = 2.0*CTH*COSB**3*ED
  XC15 = 2.0*CTH*COSB*SINB2*ED
  XC16 = XC15
  GRI = ER* I2/(I2.0*(1.0 + XNUTP)*D)
  XC11 = CTH*SN2T04/COSB*ED
  ED1 = ER*XITH/D
  SN4T02 = 4.*SINB2
  XD22 = -XD22-2.0*COSB**3*EDI-SN4T02*COSB*GRI
  TB = 2.0* BETTA
  XD33 = XD33+(14.0*COS(TB))*
  1*2*GRI/ COSB) + (2.0*COSB*SINB2*EDI)
  XD12 = -XD11*XNUTP-(2.0*COSB
  1*SINB2*EDI)-(SN4T02*COSB*GRI)
  XK12 = XK11*XNUTP + (2.0*COSB*SINB2*ED)
  XK22 = XK22+(2*COSB**3*ED)
  XK33 = XK33+(2*COSB*SINB2*ED)
  XK11 = XK11+(SN2T04*ED/COSB)
  XD11 = -XD11-SN2T04*EDI/COSB-{
  1 SN4T02*COSB*GRI)
  XK21 = XK12
  XD21 = XD12
  G0 T0 103
C
C
C   ISG CLUE(7,8,9)
100 CONTINUE
  SNB = SIN(BETTA)
  CSB = COS(BETTA)
  TBETTA = 2.0*BETTA
  CS2B = COS(TBETTA)
  0NEC2B = (1.0+ CS2B)/2.
  SCB2 = (SNB-CS2B*SNB + 2.)/(2.0*CSB)
  SN2B = SIN(TBETTA) /2.
  XK12 = XK11*XNUTP + (EASTH*SNB*0NEC2B/CSB)
  XK11 = XK11+ EASTH*SCB2
  XK22 = XK22+ EASTH*(CSB/SNB*0NEC2B)
  XK33 = XK33+ EASTH* SN2B
  XC11 = (EASTH*CTH* SCB2 )
  XC15 = EASTH*CTH*1 SNB* 0NEC2B/CSB )
  XC16 = EASTH*CTH*SN2B
  XC22 = EASTH*CTH* (CSB/SNB * 0NEC2B)
  XD12 = XD11*XNUTP- E1STH*(SNB*0NEC2B/CSB)
  XD11 = XD11- E1STH*SCB2
  XD22 = -XD22-E1STH*(CSB/SNB*0NEC2B)
  XD33 = XD33+ E1STH*SN2B
  XK21 = XK12
  XD21 = XD12
C
C
C   103 CONTINUE

```

2504270
2504280

C
G0 T0 (716,714,715,714).KELVIN
716 T11 = ST(NRW+1,LL)
T1K = ST(NRW+2,LL)
T0K = ST(NRW+3,LL)
T00 = ST(NRW+4,LL)
G0 T0 717
715 T11 = ST(NRW+1,LL)
T1K = T11
T0K = T11
T00 = T11

2504350
2504360
2504370
2504380
2504390
2504400
2504410
2504420
2504430
2504440
2504450
2504460
2504470
2504480
2504490
2504500
2504510
2504520
2504530
2504540
2504550
2504560
2504570
2504580
2504590
2504600
2504610
2504620
2504630
2504640
2504650
2504660
2504670
2504680
2504690
2504700
2504710
2504720
2504730
2504740
2504750
2504760
2504770
2504780
2504790
2504800
2504810
2504820
2504830
2504840
2504850
2504860
2504870

C
717 TEMP11= ALPHTH(1)+ XNUTP * ALPHPH(1)
TEMP12= ALPHTH(2)+ XNUTP * ALPHPH(2)
TEMP21= ALPHPH(1)+ XNUTP * ALPHTH(1)
TEMP22= ALPHPH(2)+ XNUTP * ALPHTH(2)
TEMP3 = 1-XNUTP*XNUTP
TEMP4 = HI/4.0
ETHK1= ETHET(1)*TEMP11/TEMP3
TEMP5 = HI**2/24.0
ETHK2 = ETHET(2)*TEMP12/TEMP3
TEMP61= T11+ T1K-2* TEFREE
TEMP62= T00+ T0K-2* TEFREE
TEMP71= 2.0* T11 +T1K-3*TEFREE
TEMP72= 2.0* T00 +T0K-3*TEFREE
EPHK1 = EPHI(1)*TEMP21/TEMP3
EPHK2 = EPHI(2)*TEMP22/TEMP3
G0 T0 (811,812,813,814).THICK

C
811 XNTH= ETHK1 * TEMP4 * (TEMP61+ TEMP62)
XNTPH= EPHK1 * TEMP4 * (TEMP61 + TEMP62)
XNTH= ETHK1 * TEMP5 * (TEMP71- TEMP72)
XNTPH= EPHK1 * TEMP5 * (TEMP71 - TEMP72)
G0 T0 714
812 T1 = (HI*(E2-E1)+2.0*E2*T1)/(2.0*(E1+E2))
T0 = (HI*(E1-E2)+2.0*E1*T1)/(2.0*(E1+E2))
TEMP8= HI/2.0
XNTH= ETHK1 * TEMP8*TEMP61 + ETHK2 * TEMP8*
ITEMP62 TEMP8*TEMP61 + EPHK2 * TEMP8*
ITEMP62 TEMP8*TEMP61 + EPHK2 *
XNTH = (ETHK1 * TEMP8 * (HI*TEMP71/3.0+ T1*TEMP61)) - (ETHK2 *
1 TEMP8*(HI*TEMP72/3.0+T0*TEMP62))
XNTPH = (EPHK1 * TEMP8 * (HI*TEMP71/3.0+ T1*TEMP61)) - (EPHK2 *
1 TEMP8*(HI*TEMP72/3.0+T0*TEMP62))
G0 T0 714
813 T1 = (E2*H0**2-E1*H1**2+2.0*E2*H0*T1)/(2.0*(E1*H1+E2*H0))
T0 = (E1*H1**2-E2*H0**2+2.0*E1*H1*T1)/(2.0*(E1*H1+E2*H0))
XNTH = ETHK1*0.5*(HI*TEMP61)+ETHK2*0.5*(H0*TEMP62)
XNTPH = EPHK1*0.5*(HI*TEMP61)+ EPHK2*0.5*(H0*TEMP62)
XNTH = ETHK1*0.5*(HI**2*TEMP71/3.0+T1*HI*TEMP61)-ETHK2*0.5*(H0
**2*TEMP72/3.+T0*H0*TEMP62)
XNTPH = EPHK1*0.5*(HI**2*TEMP71/3.0+T1*HI*TEMP61)-EPHK2*0.5*(H0
**2*TEMP72/3.+ T0*H0*TEMP62)
G0 T0 714
814 TEMP10=(((-XK11*X011)**.5)/(48.0**5)
TEMP11 = (((-XK22*X022)**.5)/(48.0**5)
XNTH = (XK11/4.0 *TEMP11)* TEMP61 + (XK11/4.0*TEMP12) * TEMP62
XNTPH = (XK22/4.0 *TEMP21)* TEMP61 + (XK22/4.0*TEMP22) * TEMP62
XNTH = TEMP10*(TEMP11*TEMP71 - TEMP12* TEMP72)

XMPH = TEM1*(TEMP21*TEMP71 - TEMP22*TEMP72)
714 CONTINUE
8889 RETURN
END

2504880
2504890
2504900
2504910

```

C ..... ROUTINE ** GEOMET ** ABACUS UPDATED 07/24/72 .....
C SUBROUTINE GEOMET
C THIS SUBROUTINE CALCULATES THE GEOMETRY FOR A SHELL SEGMENT.
C THE INPUT VARIABLES ARE . . .
C RI(1) - - DISTANCE FROM AXIS OF REV. TO POINTS
C ON SHELL MERIDIAN.
C ZI(1) - - DISTANCE ALONG AXIS OF REV. TO THE
C INTERSECTION OF THE CORRESPONDING RI(1) AND
C THE AXIS OF REV.
C NRZIN - - NUMBER OF (RI,ZI) PAIRS READ AS INPUT.
C
C COMMON /SPLNS/ ANG,PSI(100),RAD(100),CUR1(100),CUR2(100),
C DRIDP(100),ZI(14),RI(14),NRZIN
C DIMENSION CI(4,13),DRDZ(14),SOUT(14),S(101),RADD(100)
C
C FUN(ARG) = SQRT(1.0 + ARG**2)
C
C RADS = 3.1415926/180.0
C DATA B/-B -/
C AMULT = 1.0
C IF (ANG.EQ.B) AMULT = -1.0
C
C PASS SPLINE CURVE THROUGH INPUT POINTS ON SHELL MERIDIAN, AND
C COMPUTE DR/DZ AT THESE POINTS.
C
C CALL PLIC0 (ZI,RI,NRZIN,CI)
C NDELZ = NRZIN - 1
C DO 60 I=1,NRZIN
C CALL PLINE (ZI,RI,NRZIN,CI,ZI(1),FAKE1,DRDZ(1),FAKE2)
C 60 CONTINUE
C
C COMPUTE MERIDIONAL ARC LENGTH TO INTERPOLATED POINTS BY
C NUMERICAL INTEGRATION (SIMPSON'S RULE). SINCE SIMPSON'S RULE
C REQUIRES AN EVEN NUMBER OF PARTITIONS, INTERPOLATE A POINT
C MIDWAY BETWEEN EACH PAIR OF POINTS USING SUBROUTINE SPLINE.
C
C SOUT(1) = 0.
C DO 70 I=1,NDELZ
C DZ2=(ZI(I+1)-ZI(I))/2.0
C DZ6=DZ2/3.0
C CALL PLINE (ZI,RI,NRZIN,CI,ZI(1)+DZ2,FAKE1,DRDZM,FAKE2)
C SOUT(I+1) = SOUT(1) + DZ6*(FUN(DRDZ(1)) + 4.0*FUN(DRDZM) +
C 1 FUN(DRDZ(I+1)))
C 70 CONTINUE
C
C USE SPLIC0 TO REPRESENT RI(1) AS A FUNCTION OF SOUT(1). THEN USE
C SPLINE TO INTERPOLATE RADD AND CORRESPONDING DERIVATIVES. FROM
C THESE, COMPUTE THE TWO PRINCIPAL RADII OF CURVATURE,
C CUR1 = 1/RI
C CUR2 = 1/R2
C
C OLDHI = SOUT(NRZIN)/99.0
C CALL PLIC0 (SOUT,RI,NRZIN,CI)
C DO 110 I=1,100
C S(I) = FLOAT(I-1)*OLDHI
C CALL PLINE (SOUT,RI,NRZIN,CI,S(I),RAD(1),RADD2)
C IF (ABS(RADD2(I)).GT.1.0) RADD(I)=1.0
C FACTOR = SQRT(1.0-RADD(I)**2)
C CUR1(I) = -RADD2/FACTOR
C CUR2(I) = FACTOR/RAD(I)

```

2700600
2700610
2700620
2700630
2700640
2700650
2700660
2700670
2700680
2700690
2700700
2700710
2700720
2700730
2700740
2700750
2700760
2700770
2700780
2700790
2700800
2700810
2700820
2700830
2700840

```

110 CONTINUE
00 180 J=1,100
C0SPSI = -AMULT*RA0D(J)
PSI(J) = ARC0S(C0SPSI)
SINPSI = -AMULT*RA0D(J)*CUR2(J)
IF (ANG.EQ.8) G0 T0 179
PSI(J) = 2.0*3.1415926-PSI(J)
179 CONTINUE
CUR1(J) = -AMULT/CUR1(J)
CUR2(J) = -AMULT/CUR2(J)
IF (J.EQ.1) G0 T0 180
I = 1
IF (J.EQ.2) G0 T0 181
I = 2
181 IF (ANG.EQ.8) G0 T0 190
DRIDP(J-1) = (CUR1(J)-CUR1(J-1))/(PSI(J)-PSI(J-1))
G0 T0 180
190 DRIDP(J-1) = (CUR1(J)-CUR1(J-1))/(PSI(J-1)-PSI(J))
180 CONTINUE
DRIDP(100) = DRIDP(99)
00 42 J=1,100
DRIDP(J) = DRIDP(J)*0.1
42 CONTINUE
RETURN
END

```

```

C ..... ROUTINE ** PLIC0 ** ABACUS UPDATED 05/20/72 .....
C SUBROUTINE PLIC0 (X,Y,M,C)
SUBROUTINE T0 DETERMINE C(1,K),C(2,K),C(3,K) AND C(4,K).
DIMENSION X(14),Y(14),A(14,3),B(14),Z(14)
DIMENSION D(13),P(13),E(13),C(4,13)
MM = M-1
D0 10 K=1,MM
D(K) = X(K+1) - X(K)
P(K) = D(K)/76.0
10 F(K) = (Y(K+1)-Y(K))/D(K)
D0 20 K=2,MM
20 B(K) = E(K) - E(K-1)
A(1,2) = -1.0-D(1)/D(2)
A(1,3) = D(1)/D(2)
A(2,3) = P(2)-P(1)*A(1,3)
A(2,2) = 2.0*(P(1)+P(2)) - P(1)*A(1,2)
A(2,3) = A(2,3)/A(2,2)
B(2) = B(2)/A(2,2)
D0 30 K=3,MM
A(K,2) = 2.0*(P(K-1)+P(K))-P(K-1)*A(K-1,3)
B(K) = B(K)-P(K-1)*B(K-1)
A(K,3) = P(K)/A(K,2)
30 B(K) = B(K)/A(K,2)
G = D(M-2)/D(M-1)
A(M,1) = 1.0+Q+A(M-2,3)
A(M,2) = -Q-A(M,1)*A(M-1,3)
B(M) = B(M-2)-A(M,1)*B(M-1)
Z(M) = B(M)/A(M,2)
MN = M-2
D0 40 I=1,MN
K = M-I
40 Z(K) = B(K)-A(K,3)*Z(K+1)
Z(1) = -A(1,2)*Z(2)-A(1,3)*Z(3)
D0 50 K=1,MM
Q = 1.0/16.0*D(K)
C(1,K) = Z(K)*Q
C(2,K) = Z(K+1)*Q
C(3,K) = Y(K)/D(K)-Z(K)*P(K)
50 C(4,K) = Y(K+1)/D(K)-Z(K+1)*P(K)
RETURN
END

```

```

2900000
2900010
2900020
2900030
2900040
2900050
2900060
2900070
2900080
2900090
2900100
2900110
2900120
2900130
2900140
2900150
2900160
2900170
2900180
2900190
2900200
2900210
2900220
2900230
2900240
2900250
2900260
2900270
2900280
2900290
2900300
2900310
2900320
2900330
2900340
2900350
2900360
2900370
2900380
2900390
2900400

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C ..... ROUTINE ** PLINE ** ABACUS UPDATED 05/20/72 .....
C SUBROUTINE PLINE (X,Y,M,C,XINT,YINT,DYDX,D2YDX2)
C SUBROUTINE FOR SPLINE FIT INTERPOLATION IN THE TABLE OF VALUES
C (X1,Y1) TO (XM,YM), WHERE M MAY BE AS LARGE AS 100, WHERE THE
C CONSTANTS C(1,K),C(2,K),C(3,K) AND C(4,K) ARE ALREADY COMPUTED
C AND STORED.
C SUBROUTINE ALSO COMPUTES DY/DX AND D2Y/DX2 AT XINT.
C DIMENSION X(14),Y(14),C(4,13)
C IF (XINT-X(1)) 80,10,20
C   10 YINT = Y(1)
C     K=1
C     GO TO 70
C   20 K = 1
C   30 IF (XINT-X(K+1)) 60,40,50
C   40 YINT = Y(K+1)
C     GO TO 70
C   50 K = K + 1
C   IF (M-K) 80,80,30
C   60 YINT = (X(K+1) - XINT)*(C(1,K)*(X(K+1)-XINT)**2+C(3,K))
C     YINT = YINT + (XINT-X(K))*(C(2,K)*(XINT-X(K))**2+C(4,K))
C   70 DYDX=-3.0*(C(1,K)*(X(K+1)-XINT)**2-C(2,K)*(XINT-X(K))**2)
C     -C(3,K)+C(4,K)
C     1 D2YDX2=6.0*(C(1,K)*(X(K+1)-XINT)+C(2,K)*(XINT-X(K)))
C     RETURN
C 80 WRITE (6,90)
C 90 FORMAT (3H OUT OF RANGE FOR INTERPOLATION)
C RETURN
C END
2800000
2800010
2800020
2800030
2800040
2800050
2800060
2800070
2800080
2800090
2800100
2800110
2800120
2800130
2800140
2800150
2800160
2800170
2800180
2800190
2800200
2800210
2800220
2800230
2800240
2800250
2800260
2800270

```


SUBROUTINES DIF1 AND DIFF2

These subroutines are called in RIEMAN as necessary. DIF1 contains the differential equations for the THIC and ST clues, while DIFF2 contains the differential equations for the RWA and ISG clues. Geometry clues, trigonometric values, and predicted values of the differential equation variables are passed via label common area, EQUAZN, to subroutines DIF1 or DIFF2. The coefficients for nonlinear and load terms, X1, X2 and K, are identified depending upon the pass number and convergence criterion.

The specific derivative equations and auxiliary equations are contained in these subroutines. The values of each derivative equation, YDOT, and each auxiliary equation, YA ---, are returned to RIEMAN via label common EQUAZN.

A special equation counter, I, is used in these subroutines, which counts in increments of eight. The first eight values of I, 1 through 57 (in increments of eight), correspond to the eight sets of initial conditions required to compute the segment stiffness matrices in subroutine SEGMAT. The subsequent values of I, 65 and 73 maximum (again in increments of eight) correspond to the computation of each set of eight equations for each loading condition (two conditions corresponding to dead and live loads respectively).

FORTRAN CODE

ENGINEERING SYMBOLS (REF. 1)

XN

n

YDOT (I)

$T_{\phi\theta, \phi}$

$\frac{dT_{\phi\theta}}{ds}$

YDOT (I + 1)

$N_{\phi, \phi}$

$\frac{dN_{\phi}}{ds}$

YDOT (I + 2)

$J_{\phi, \phi}$

$\frac{dJ_{\phi}}{ds}$

YDOT (I + 3)

$M_{\phi, \phi}$

$\frac{dM_{\phi}}{ds}$

YDOT (I + 4)

U_{ϕ}

$\frac{dU}{ds}$

YDOT (I + 5)

V_{ϕ}

$\frac{dV}{ds}$

YDOT (I + 6)

W_{ϕ}

$\frac{dW}{ds}$

YDOT (I + 7)

$\Omega_{\theta, \phi}$

$\frac{d\Omega_{\theta}}{ds}$

YPRED (I)

$T_{\phi\theta}$

YPRED (I + 1)

N_{ϕ}

YPRED (I + 2)

J_{ϕ}

YPRED (I + 3)

M_{ϕ}

YPRED (I + 4)

U

YPRED (I + 5)

V

YPRED (I + 6)

W

YPRED (I + 7)

Ω_{θ}

YAMPT

$M_{\phi\theta}$

YANTH

N_{θ}

YAMTH

M_{θ}

FORTTRAN CODE

ENGINEERING SYMBOLS (REF. 1.)

R2SQ

r_2^2

ROSQ

r_0^2

XLRO

$1/r_0$

S

s

XK12

K_{12}

XK21

K_{21}

XD12

D_{12}

XD21

D_{21}

XC11

C_{11}

XC22

C_{22}

XNSQ

n^2

Non-Linear Redefinitions (Ref. 1)

YDOT (I+2)

$*J_{\phi, \phi}$

$\frac{d*J_{\phi}}{ds}$

YPRED (I+2)

$*J_{\phi}$

YAJPH

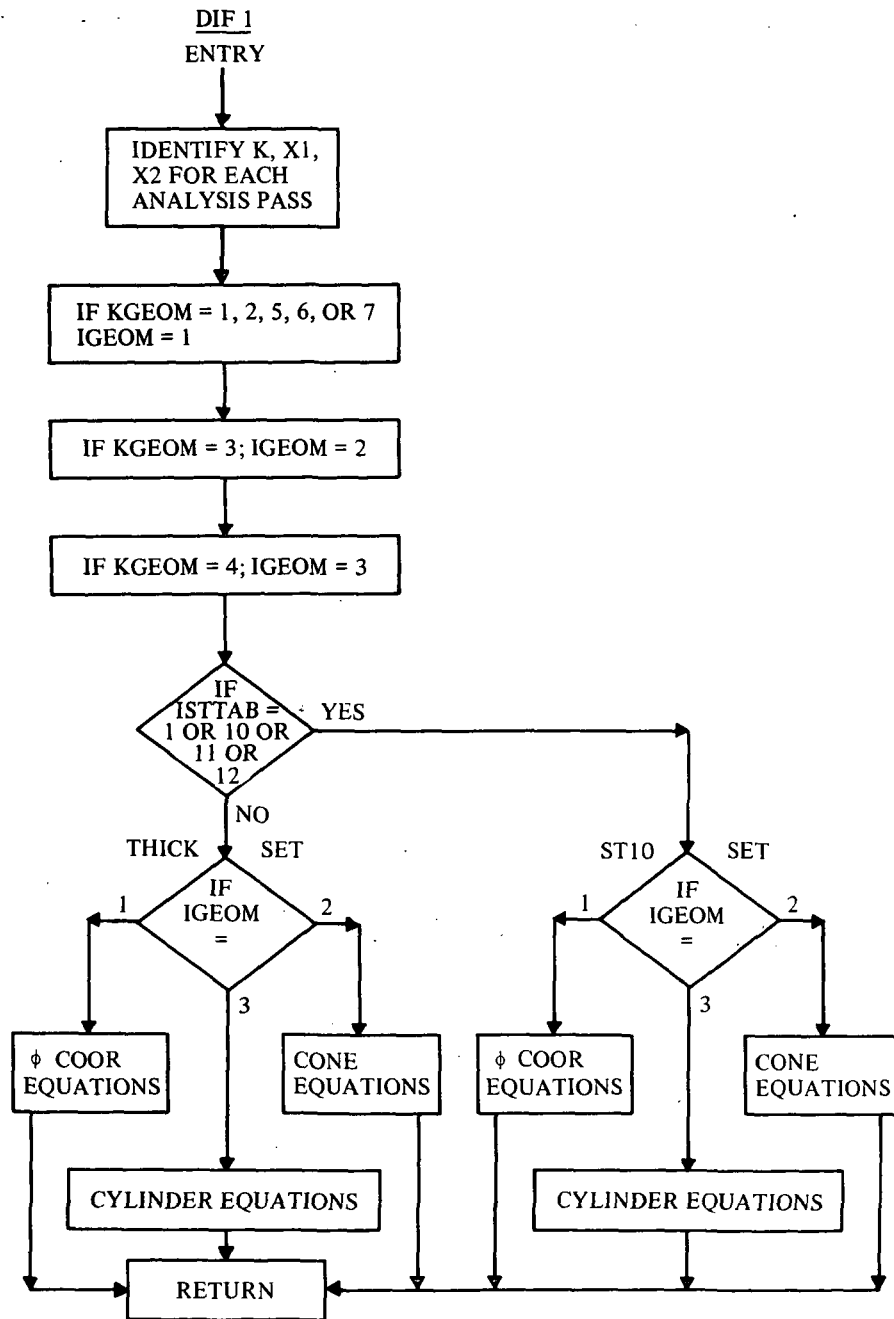
J_{ϕ}

XNL

a

XNPHI

$\frac{a}{N_{\phi}}$



```

C ***** ROUTINE **D5 ** ABACUS UPDATED 07/07/72 *****
SUBROUTINE DIF1 (XPHL1,XFZEL1,XFPHL2,XFZEL2)
INTEGER SAVJTC, SAVSTP,Q, THICK
INTEGER XN1,XN
DOUBLE PRECISION SAVTIC,TIC,PHI,STOP,RESTOP,RTICK
DOUBLE PRECISION YDOT,YASAVE,YANTH,YAMTH,YAMPT,YAJPH,S,SN,CS,SN SQ,
1 CSSQ,TAN,SEC,CN,XICS,XISN,TN,XIR0,XIR0SQ,XISNR0,
2 XICSR0,CNIR0,SNIR0,CSIR0,XIR1,XIR2,CSIR1,CSIR2,
3 SNIR1,XIR1SQ,R2SQ,R0,BESQ,R0SQ,XNSQ,R1,R2,S1,
4 RLD0T,XNTH,XNTPH,XMTH,XMTPH,XC11,XC22,XC15,
5 XD33,XD22,XD21,XD12,XK11,XK12,XK21,XK22,XK33,
6 XD11,XNPHI,BETA,XC16
COMMON STORY(16),XMAT(110,10),STD(101),RADUS(30),RADUS(30)
COMMON RADUS(30),UADUS(30),SAVTIC(900)
COMMON XN,TEFREE,TIC,PHI,STOP,RESTOP,RTICK,G1,XNL(2),NH
COMMON NST(30),NKI(30),NXMAT(20),SAVJTC(30),SAVSTP(30),JRTIC(30)
COMMON JRST0P(30),NREG,NMPT,NRC,NSC,NIX,IERR0R,KGE0M,IGE0M,ISTTAB
COMMON KELVIN,I BEGIN,NPR0B,NSEG,NERR0R,Q,THICK,N0JS,NLINKS,NLCASE
COMMON NTSKL,NZ,NBCT,LINPT,NTRKL,NPASS,XN1,KBC,NRINGS
COMMON /EQUAZN/ YPRED(80),YDOT(80),YASAVE(80),
1 YANTH,YAMTH,YAMPT,YAJPH,
2 S,SN,CS,SN SQ,CSSQ,TAN,SEC,CN,XICS,XISN,TN,
3 XIR0,XIR0SQ,XISNR0,XICSR0,CNIR0,SNIR0,CSIR0,
4 XIR1,XIR2,CSIR1,CSIR2,SNIR1,XIR1SQ,R2SQ,R0,BESQ,
5 R0SQ,XNSQ,BETA,R1,R2,S1,RLD0T,
6 XNTH,XNTPH,XMTH,XMTPH,XFTHLD,XFPHLD,XFZELD,
7 XMTHLD,XMPLHD,ETHET(2),EPI(2),XGPT(2),ALPHTH(2),ALPHPH(2),DUM,
8 XNUTP,XNUTP,XC11,XC22,XC15,XD33,XD22,XD21,XD12,
9 XK11,XK12,XK21,XK22,XK33,XD11,
A XNPHI,M,I,BETTA,ZETTA,SAVY(8),XC16
EQUIVALENCE (XNL(1),X1),(XNL(2),X2)
IF (NH.NE.0) WRITE(6,1333) PHI,SAVY
1333 FORMAT(1X,1P1E16.7,5X,1P6E16.7)
IGE0M = 0
IF (KGE0M.EQ.1.0R.KGE0M.EQ.2.0R.KGE0M.EQ.5.0R.KGE0M.EQ.6) IGE0M = 1
IF (KGE0M.EQ.3) IGE0M=2
IF (KGE0M.EQ.4) IGE0M=3
IF (KGE0M.EQ.7) IGE0M = 1
K = 0
IF (KBC.EQ.0.AND.NH.EQ.0) K = 1
IF (ISTAB.EQ.1) G0 TO 7786
IF (ISTAB.GE.10) G0 TO 7786
C THE FOLLOWING EQUATIONS ARE THE -THICK- SET
G0 TO (151,152,153),IGE0M
C EQUATIONS FOR SHELLS OF REVOLUTION ( PHI COORDINATE )
151 YANTH = XNUTP*YPRED(11)+(XK11-XNUTP**2*XK22)*(XN*YPRED(11+4)+
1 YPRED(11+5)*CS-YPRED(11+6)*SN)*XIR0*K*(XNUTP*XNTPH-
2 XNTH)
2 YAMTH = XNUTP*YPRED(11+3)-(XD11-XNUTP**2*XD22)*XIR0*(XN*
1 YPRED(11+4)*SN-XN*SN*YPRED(11+6))+YPRED(11+7)*CS)*K*
2 (XNUTP*XMTPH-XMTH)
YA0PH = XN*YPRED(11+6)*XIR0-YPRED(11+4)*SNIR0
YAMPT = (-1.0/(1R0/XD33)+(SNSQ*XIR0/XK33))*(-2.0*XN*
1 YPRED(11+7)+YPRED(11+4)*(CSIR1-CNIR0)+XN*YPRED(11+5)*
2 (SNIR0*XIR1)+2.0*XN*YPRED(11+6)*CSIR0*YPRED(11)*SN/
3 XK33+SN*YABPH*(X1*SAVY(3)+X2*SAVY(6)))
YAJPH = YPRED(11+2)-YPRED(11+1)*(X1*SAVY(3)+X2*SAVY(6))
1 -YPRED(11+7)*(X1*SAVY(2)+X2*SAVY(5))
YANPT = YPRED(11)+YAMPT*SNIR0

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```

YD0T(I+4) = R1*(YPRED(I+4)*CSIR0+XN*YPRED(I+5)*XIR0+YPRED(I)/XK33+
1 YAMPT*SNIR0/XK33)+R1*YA0PH*(X1*SAVY(3)+X2*SAVY(6))
YD0T(I) = R1*(1-2.0*YPRED(I)*CSIR0+XN*YANTH*XIR0-XN*YAMTH*SN*
1 XIR3Q-YAMPT*CSIR0*(XIR1-SNIR0))-R1*K*(XFTHLD+XMPHLD*
2 SNIR0)-(YD0T(I+4)*(X1*XFPHL1+X2*XFPHL2)+R1*YA0PH*
3 (X1*XFZEL1+X2*XFZEL2))-R1*SNIR0*(YA0PH*(X1*SAVY(1)+
4 X2*SAVY(4))-YAMPT*(X1*SAVY(3)+X2*SAVY(6)))
YD0T(I+5) = R1*(YPRED(I+6)*XIR1+(1.0/(XK22-XNUTP**2*XK11)))*
1 (YPRED(I+1)-XNUTP*YANTH+K*(XNTPH-XNUTP*XNTH))
2 -R1*YPRED(I+7)*(X1*SAVY(3)+X2*SAVY(6))
LPSITH = XIR0*(XN*YPRED(I+4)+YPRED(I+5)*CS-YPRED(I+6)*SN)
EPSIPH = XIR1*(YD0T(I+5)-YPRC0(I+6))+YPRED(I+7)*(X1*SAVY(3)+
1 X2*SAVY(6))
YD0T(I+1) = R1*(CSIR0*(YANTH-YPRED(I+1))-XN*XIR0*(YPRED(I)+
1 YAMPT*(SN*XIR0+XIR1))+YPRED(I+2)*XIR1)-R1*K*XFPHLD
2 -R1*(EPSITH+EPSIPH)*(X1*XFPHL1+X2*XFPHL2)-YPRED(I+7)*
3 (X1*XFZEL1+X2*XFZEL2))
YD0T(I+2) = R1*(1-YPRED(I+2)*CSIR0-YANTH*SNIR0-YPRED(I+1)*XIR1
1 +XNSQ*YAMTH*XIR0S0-2.0*XN*YAMPT*CS*XIR0S0)+R1*K*
2 (XN*XMPHLD*XIR0-XFZELD)-R1*(EPSITH+EPSIPH)*(X1*
3 XFZEL1+X2*XFZEL2)+YPRED(I+7)*(X1*XFPHL1+X2*XFPHL2))
4 -R1*XIR0*(YAMPT*(X1*SAVY(3)+X2*SAVY(6))-YA0PH*
5 (X1*SAVY(1)+X2*SAVY(4)))
YD0T(I+3) = R1*(YAMTH*CSIR0-YPRED(I+3)*CSIR0-2.0*XN*YAMPT*XIR0+
1 YAJPH+K*XNTHED)
YD0T(I+6) = R1*(YPRED(I+7)-YPRED(I+5)*XIR1)
YD0T(I+7) = R1*(1.0/(X022-XNUTP**2*X011))*(1-YPRED(I+3)+XNUTP*
1 YAMTH-K*(XNTPH-XNUTP*XNTH))
G0T0 9005
EQUATIONS FOR GONE
152 YANTH=XNUTP*YPRED(I+1)+(XK11-XNUTP**2*XK22)*(X1CS/S)+(XN*YPRED(I+4
1 )+YPRED(I+5)*CS-YPRED(I+6)*SN)*K*(XNUTP*XNTPH-XNTH)
YAMTH=XNUTP*YPRED(I+3)-(1.0/S)*X1CS*(XD11-XNUTP**2*XD22)*(1.0/S)*
1 X1CS*(XN*YPRED(I+4)*SN-XNSQ*YPRED(I+6))+YPRED(I+7)*CS)-
2 K*(XNTH-XNUTP*XNTPH)
YA0PH = XN*YPRED(I+6)*X1CS/S-YPRED(I+4)*TAN/S
YAMPT={-1.0/((S*CS/XD33)+(SN*TAN/(XK33*S)))*(-2.0*XN*YPRED(I+7)-
1 YPRED(I+4)*SN/S+XN*YPRED(I+5)*TAN/S+2.0*XN*YPRED(I+6)/S+YPRED
2 (I)*SN/XK33+SN*YA0PH*(X1*SAVY(3)+X2*SAVY(6)))
YAJPH = YPRED(I+2)-YPRED(I+1)*(X1*SAVY(3)+X2*SAVY(6))
1 -YPRED(I+7)*(X1*SAVY(2)+X2*SAVY(5))
YAMPT = YPRED(I)+YAMPT*TAN/S
YD0T(I+4)={1.0/S)*(YPRED(I+4)+XN*YPRED(I+5)*X1CS+YAMPT*TAN/XK33)
1 -YPRED(I)/XK33+YA0PH*(X1*SAVY(3)+X2*SAVY(6))
YD0T(I) = -2.0*YPRED(I)/S+XN*YANTH*X1CS/S-XN*YAMTH*SN*X1CS**2/S**2
1 +YAMPT*TAN/S**2-K*(XFTHLD+XMPHLD*TAN/S)-(YD0T(I+6)*
2 (X1*XFPHL1+X2*XFPHL2)+YA0PH*(X1*XFZEL1+X2*XFZEL2))-
3 TAN/S*(YA0PH*(X1*SAVY(1)+X2*SAVY(4))-YAMPT*(X1*SAVY(3)
4 +X2*SAVY(6)))
YD0T(I+5) = (1.0/(XK22-XNUTP**2*XK11))*(YPRED(I+1)-XNUTP*YANTH+
1 K*(XNTPH-XNUTP*XNTH))-YPRED(I+7)*(X1*SAVY(3)+X2*
2 SAVY(6))
EPSITH = (1.0/(S*CS))*(XN*YPRED(I+4)+CS*YPRED(I+5)-SN*
1 YPRED(I+6))
EPSIPH = YD0T(I+5)+YPRED(I+7)*(X1*SAVY(3)+X2*SAVY(6))
YD0T(I+1) = -YPRED(I+1)/S+YANTH/S-XN*YPRED(I)/(S*CS)-XN*YAMPT*SN/
1 (S**2+CS**2)-K*XFPHLD-(EPSITH+EPSIPH)*(X1*XFPHL1+X2*
2 XFPHL2)+YPRED(I+7)*(X1*XFZEL1+X2*XFZEL2)
YD0T(I+2) = -YPRED(I+2)/S-YANTH*TAN/S+XNSQ*YAMTH/(S**2*CS**2)
1 -2.0*XN*YAMPT/(S**2*CS)+K*(XN*XMPHLD*X1CS/S-XFZELD)
2 -(EPSITH+EPSIPH)*(X1*XFZEL1+X2*XFZEL2)-YPRED(I+7)*

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3      (X1*XFPHL1+X2*XFPHL2)-X1CS/S*KN*(YANPT*(X1*SAVY(3)+
4      X2*SAVY(6))-YAØPH*(X1*SAVY(1)+X2*SAVY(4)))
1      YØDT(I+3)=YANTH/S-YPRED(I+3)/S-2.0*KN*YAMPT/(S*CS1+YAJPH+XMTHLØ
1      *K
1      YØDT(I+6)=YPRED(I+7)
1      YØDT(I+7)=(1.0/(XØ22-XNUTP**2*XØ11))*(-YPRED(I+3)+XNUTP*YAMTH-
1      K*(XMTPH-XNUTP*XMTTH))
1      GØ TØ 9005
C      EQUATIONS FOR CYLINDER
153 YANTH=XNUTP*YPRED(I+1)+(XØ11-XNUTP**2*XK22)*(X1RØ*(XN*YPRED(I+4)-
1      YPRED(I+6)))+K*(XNUTP*XNTPH-XNTTH)
1      YAMTH=XNUTP*YPRED(I+3)-(X1RØ*(XØ11-XNUTP**2*XØ22))*(X1RØ*(XN*YPRED
1      (I+4)-XNSQ*YPRED(I+6)))+K*(XNUTP*XMTPH-XMTTH)
1      YAOØPH = X1RØ*(XN*YPRED(I+6))-YPRED(I+4)
1      YAMPT=(-1.0/(RØ/XØ33)+(X1RØ/XK33))*(-2.0*XN*YPRED(I+7)+XN*X1RØ*
1      YPRED(I+5)+YPRED(I+1)/XK33+YAOØPH*(X1*SAVY(3)+X2*
2      SAVY(6)))
1      YAJPH = YPRED(I+2)-YPRED(I+1)*(X1*SAVY(3)+X2*SAVY(6))
1      -YPRED(I+7)*(X1*SAVY(2)+X2*SAVY(5))
1      YANPT = YPRED(I+YAMPT*X1RØ
1      YØDT(I+4)=XN*YPRED(I+5)*X1RØ+YPRED(I)/XK33+YAMPT*X1RØ/XK33
1      +YAOØPH*(X1*SAVY(3)+X2*SAVY(6))
1      YØDT(I) = XN*YANTH*X1RØ-XN*YAMTH*X1RØSQ-K*(XFTHLØ+XMPHLØ*X1RØ)
1      -(YØDT(I+4)*(X1*XFPHL1+X2*XFPHL2)+YAOØPH*(X1*XFZELL+
2      X2*XFZEL2))-X1RØ*(YAOØPH*(X1*SAVY(1)+X2*SAVY(4))-YANPT*
3      (X1*SAVY(3)+X2*SAVY(6)))
1      YØDT(I+5) = (1.0/(XK22-XNUTP**2*XØ11))*(YPRED(I+1)-XNUTP*YANTH+
1      K*(XNTPH-XNUTP*XNTTH))-YPRED(I+7)*(X1*SAVY(3)+X2*
2      SAVY(6))
1      EPSITH = X1RØ*(XN*YPRED(I+6)-YPRED(I+6))
1      EPSIPH = YØDT(I+5)+YPRED(I+7)*(X1*SAVY(3)+X2*SAVY(6))
1      YØDT(I+1) = -XN*X1RØ*YPRED(I)-XN*YAMPT*X1RØSQ-K*XFPHLØ-(EPSITH+
1      EPSIPH)*(X1*XFPHL1+X2*XFPHL2)+YPRED(I+7)*(X1*XFZELL+
2      X2*XFZEL2)
1      YØDT(I+2) = -YANTH*X1RØ+XNSQ*YAMTH*X1RØSQ+K*(XN*XMPHLØ*X1RØ-
1      XFZELØ)-(EPSITH+EPSIPH)*(X1*XFZELL+X2*XFZEL2)-
2      YPRED(I+7)*(X1*XFPHL1+X2*XFPHL2)-X1RØ*XN*(YANPT*
3      (X1*SAVY(3)+X2*SAVY(6))-YAOØPH*(X1*SAVY(1)+X2*SAVY(4)))
1      YØDT(I+3) = -2.0*XN*YAMPT*X1RØ+YAJPH+K*XMTHLØ
1      YØDT(I+6)=YPRED(I+7)
1      YØDT(I+7) = (1.0/(XØ22-XNUTP**2*XØ11))*(-YPRED(I+3)+XNUTP*YAMTH+
1      K*(XNUTP*XMTTH-XMTPH))
1      GØ TØ 9005
7786 GØ TØ (4771,4772,4773),IGEØM
C      THE FØLLØWING EQUATIONS ARE THE -STIØ- SET
C      EQUATIONS FOR SHELLS ØF REVØLUTION ( PHI CØØRDINATE )
4771 YANTH = XØ12*(1.0/(XK22+XØ22**2/XØ22))*(YPRED(I+1)+K*XNTPH+
1      (XC22/XØ22)*(YPRED(I+3)+K*XMTPH))-K*XNTTH+(X1RØ*XØ11-
1      XØ12*XK21*X1RØ*(1.0/
2      (XK22+XØ22**2/XØ22)))+(XN*YPRED(I+4)+YPRED(I+5)*CS-YPRED(I+
3      6)*SN)-(XØ11+XØ12*XØ22*XØ21/XØ22*(1.0/(XK22+XØ22**2/XØ22)))*
4      (X1RØ**2*(XN*YPRED(I+4)*SN-XN**2*YPRED(I+6))+YPRED(I+7)*CS*
5      X1RØ)
1      YAMTH = -XØ12*(XC22/(XC22+XØ22**2*XK22*XØ22))*(YPRED(I+1)+K*XNTPH)
1      -K*(XMTTH+XØ12*(XC22/(XC22+XØ22**2*XK22*XØ22)))+(YPRED(I+3)+
1      K*XMTPH)+(XØ11*
2      X1RØ+XØ12*XØ22*X1RØ*(XC22/(XC22+XØ22**2*XK22*XØ22)))+(XN*YPRED(
3      I+4)+YPRED(I+5)*CS-YPRED(I+6)*SN)+(XØ11-XØ12*XØ22*XØ21/(
4      XC22+XØ22**2*XK22*XØ22))*(X1RØSQ*(XN*YPRED(I+4)*SN-XNSQ*YPRED
5      (I+6))+YPRED(I+7)*CS*X1RØ)
1      YAOØPH = XN*YPRED(I+6)*X1RØ-YPRED(I+4)*SN1RØ

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YAMPT = (-1.0/(1R0/XD33)+(SNSQ*X1R0/XK33))*(-2.0*KN*
1 YPRED(I+7)+YPRED(I+4)*(CS1R1-CN1R0)+KN*YPRED(I+5)*
2 (SNIR0*X1R1)+2.0*KN*YPRED(I+6)+CS1R0*YPRED(I+5)*
3 XK33+SN*YA0PH*(X1*SAVY(3)+X2*SAVY(6)))
YAJPB = YPRED(I+2)-YPRED(I+1)*(X1*SAVY(3)+X2*SAVY(6))
1 -YPRED(I+7)*(X1*SAVY(2)+X2*SAVY(5))
YANPT = YPRED(I+YAMPT*SNIR0
Y00T(I+4) = R1*(YPRED(I+4)*CS1R0+KN*YPRED(I+5)*X1R0+YPRED(I+3)*
1 YAMPT*SNIR0/XK33)+R1*YA0PH*(X1*SAVY(3)+X2*SAVY(6))
Y00T(I) = R1*(-2.0*YPRED(I+1)*CS1R0+KN*YANTH*X1R0-KN*YAMTH*SN*
1 X1R0SQ-YAMPT*CS1R0*(X1R1-SNIR0))-R1*(X1*SAVY(3)+X2*SAVY(6))
2 SNIR0)-(Y00T(I+4)*(X1*SAVY(3)+X2*SAVY(6)))+(X1*SAVY(3)+X2*SAVY(6))
3 (X1*SAVY(3)+X2*SAVY(6)))+(X1*SAVY(3)+X2*SAVY(6))
4 X2*SAVY(6)))+(X1*SAVY(3)+X2*SAVY(6))
Y00T(I+5) = R1*(YPRED(I+6)*X1R1-YPRED(I+7)*(X1*SAVY(3)+X2*SAVY(6))
1 +(1.0/(XK22+XC22**2/XD22)))*(YPRED(I+1)+K*XNTPH*(XC22/
2 XD22)*YPRED(I+3)+K*XNTPH)-XK21*X1R0*(XN*
3 YPRED(I+4)+YPRED(I+5)*CS-YPRED(I+6)*SN)-(XC22*XD21/XD22
4 *(X1R0SQ*(XN*YPRED(I+4)*SN-XNSQ*YPRED(I+6))+YPRED(I+7)
5 *CS*X1R0)))
EPSITH = X1R0*(XN*YPRED(I+4)+YPRED(I+5)*CS-YPRED(I+6)*SN)
EPSIPH = X1R1*(Y00T(I+5)-YPRED(I+6))+YPRED(I+7)*(X1*SAVY(3)+
1 X2*SAVY(6))
Y00T(I+1) = R1*(CS1R0*(YANTH-YPRED(I+1))-KN*X1R0*(YPRED(I+1)+
1 YAMPT*(SN*X1R0+X1R1))+YPRED(I+2)*X1R1)-R1*(X1*SAVY(6))
2 -R1*(EPSITH+EPSIPH)*(X1*SAVY(3)+X2*SAVY(6))-YPRED(I+7)*
3 (X1*SAVY(3)+X2*SAVY(6)))
Y00T(I+2) = R1*(YPRED(I+2)*CS1R0-YANTH*SNIR0-YPRED(I+1)*X1R1
1 +XNSQ*YAMTH*X1R0SQ-2.0*KN*YAMPT*CS*X1R0SQ)*R1*(X1*
2 (XN*YAMTH*X1R0-XFZELD))-R1*(EPSITH+EPSIPH)*(X1*
3 XFZELD+X2*XFZEL2)+YPRED(I+7)*(X1*SAVY(3)+X2*SAVY(6))
4 -R1*(X1R0*KN*(YAMPT*(X1*SAVY(3)+X2*SAVY(6)))-YA0PH*
5 (X1*SAVY(3)+X2*SAVY(6)))
Y00T(I+3) = R1*(YANTH*CS1R0-YPRED(I+3)*CS1R0-2.0*KN*YAMPT*X1R0+
1 YAJPH+K*XMTPLD)
Y00T(I+6) = R1*(YPRED(I+7)-YPRED(I+5)*X1R1)
Y00T(I+7) = R1*(-XC22/(XC22**2+XK22*XD22))*(YPRED(I+1)+K*XNTPH-
1 (XK21/
2 R0)*(XN*YPRED(I+4)+YPRED(I+5)*CS-YPRED(I+6)*SN))
3 +(XK22/(XC22**2+XK22*XD22))*(YPRED(I+3)+K*XMTPH)-(XK22*
4 XD21/(XC22**2+XK22*XD22))*X1R0SQ*(XN*YPRED(I+4)*SN-XNSQ
5 *YPRED(I+6))+YPRED(I+7)*CS*X1R0))
C0 T0 9005
EQUATIONS FOR C0NE
4772 YANTH = XK12*(1.0/(XK22+XC22**2/XD22))*(YPRED(I+1)+K*XNTPH+
1 (XC22/XD22)*(YPRED(I+3)+K*XMTPH))-K*XNTTH*(1.0/(CS*SN))
2 *(XK11-XK12*XK21)
3 1.0/(XK22+XC22**2/XD22))*(XN*YPRED(I+4)+YPRED(I+5)*CS-
4 YPRED(I+6)*SN)-(XK11*(XK12*XD21*XC22/XD22)*(1.0/(XK22+XC22*
5 (I+6))+YPRED(I+7)/S)
YAMTH = -XD12*(XC22/(XC22**2+XK22*XD22))*(YPRED(I+1)+K*XNTPH)
1 -K*XMTTH*XD12*(XC22/(XC22**2+XK22*XD22))*(YPRED(I+3)+
2 K*XMTPH)+(XC11/
3 (S*CS)+XD12*XK21/(S*CS))*(XC22/(XC22**2+XK22*XD22))*(XN*
4 YPRED(I+4)+YPRED(I+5)*CS-YPRED(I+6)*SN)+(XD11-XD12*XK22*
5 XD21/(XC22**2+XK22*XD22))*(1.0/(S*CS))*2*(XN*YPRED(I+4)*
6 SN-XNSQ*YPRED(I+6))+YPRED(I+7)/S)
YA0PH = XN*YPRED(I+6)*X1CS/S-YPRED(I+4)*TAN/S
YAMPT = (-1.0/(1S*CS/XD33)+(SN*TN/XK33*SN))*(-2.0*KN*YPRED(I+7)-
1 YPRED(I+4)*SN/S+KN*YPRED(I+5)*TN/S+2.0*KN*YPRED(I+6)/S+YPRED

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2      (1)*SN/XK33+SN*YABPH*(X1*SAVY(3)+X2*SAVY(6)))
YA JPH      = YPRED(I+2)-YPRED(I+1)*(X1*SAVY(3)+X2*SAVY(6))
1      -YPRED(I+7)*(X1*SAVY(2)+X2*SAVY(5))
YANPT      = YPRED(I)*YAMPT*TAN/S
YD0T(I+4)  = (1.0/S)*(YPRED(I+4)+XN*YPRED(I+5)*X1CS+YAMPT*TN/XK33)
1      +YPRED(I)/XK33+YABPH*(X1*SAVY(3)+X2*SAVY(6))
YD0T(I)    = -2.0*YPRED(I)/S+XN*YANTH*X1CS/S-XN*YANTHSN*X1CS**2/S**2
1      +YAMPT*TAN/S**2-K*(XFTHLD+XMPHLD*TAN/S)-(YD0T(I+4)*
2      (X1*XFPHL1+X2*XFPHL2)+YABPH*(X1*XFZEL1+X2*XFZEL2))-
3      TAN/S*(YABPH*(X1*SAVY(1)+X2*SAVY(4))-YANPT*(X1*SAVY(3)
4      +X2*SAVY(6)))
YD0T(I+5)  = -YPRED(I+7)*(X1*SAVY(3)+X2*SAVY(6))+1.0/(XK22+XC22**2
1      /XD22)*(YPRED(I+1)+K*XNTPH+(XC22/XD22)*(YPRED(I+3)
2      +K*XNTPH)-(XK21/(S*CS))*(XN*YPRED(I+4)+YPRED(
3      I+5)*CS-YPRED(I+6)*SN)-(XC22*X021/XD22)*(1.0/(S**2*CS**
4      2))*(XN*YPRED(I+4)*SN-XNSQ*YPRED(I+6))+YPRED(I+7)/S))
EPSITH     = (1.0/(S*CS))*(XN*YPRED(I+4)+CS*YPRED(I+5)-SN*
1      YPRED(I+6))
EPSIPH     = YD0T(I+5)+YPRED(I+7)*(X1*SAVY(3)+X2*SAVY(6))
YD0T(I+1)  = -YPRED(I+1)/S+YANTH/S-XN*YPRED(I)/(S*CS)-XN*YAMPT*SN/
1      (S**2*CS**2)-K*XFPHLD-(EPSITH+EPSIPH)*(X1*XFPHL1+X2*
2      XFPHL2)+YPRED(I+7)*(X1*XFZEL1+X2*XFZEL2)
YD0T(I+2)  = -YPRED(I+2)/S-YANTH*TAN/S+XNSQ*YANTH/(S**2*CS**2)
1      -2.0*XN*YAMPT/(S**2*CS)+K*(XN*XMPHLD*X1CS/S-XFZELD)
2      -(EPSITH+EPSIPH)*(X1*XFZEL1+X2*XFZEL2)-YPRED(I+7)*
3      (X1*XFPHL1+X2*XFPHL2)-X1CS/S*XN*(YANPT*(X1*SAVY(3))+
4      X2*SAVY(6))-YABPH*(X1*SAVY(1)+X2*SAVY(4))
YD0T(I+3)  = YANTH/S-YPRED(I+3)/S-2.0*XN*YAMPT/(S*CS)+YAJPH+XNTHLD
1      *K
YD0T(I+6)  = YPRED(I+7)
YD0T(I+7)  = -(XC22/(XC22**2+XK22*XD22))*(YPRED(I+1)+K*XNTPH-XK21*
1      (XN*
2      YPRED(I+4)+YPRED(I+5)*CS-YPRED(I+6)*SN)/(S*CS))
3      +(XK22/(XC22**2+XK22*XD22))*(YPRED(I+3)+K*XNTPH)-(XK22*
4      XD21
5      /XC22**2+XK22*XD22))*(1.0/(S*CS)*XK21*(XN*YPRED(I+4)*SN
6      -XN**2*YPRED(I+6))+YPRED(I+7)/S)
GO TO 9005
C      EQUATIONS FOR CYLINDER
4773 YANTH      = XK12*(1.0/(XK22+XC22**2/XD22))*(YPRED(I+1)+K*XNTPH+
1      (XC22/XD22)*(YPRED(I+3)+K*XNTPH))-K*XNTPH*(X1R0*(XK11-
2      XK12*XK21*(1.0/
3      XK22+XC22**2/XD22)))+(XN*YPRED(I+4)-YPRED(I+6))-(XK11*(
4      XK12*XC22*XD21/XD22)*(1.0/(XK22+XC22**2/XD22))*(X1R0**2*(
5      XN*YPRED(I+4)-XNSQ*YPRED(I+6)))
YANTH      = -X012*(XC22/(XC22**2+XK22*XD22))*(YPRED(I+1)+K*XNTPH)
1      -K*XNTPH*X012*(XK22/(XC22**2+XK22*XD22))*(YPRED(I+3)+
2      K*XNTPH)*(XK11*
3      X1R0+X012*XK21*(X1R0*(XC22/(XC22**2+XK22*XD22)))+(XN*YPRED
4      (I+4)-YPRED(I+6)))+(X011-X012*XK22*XD21/(XC22**2+XK22*XD22)
5      )*(X1R0SQ*(XN*YPRED(I+4)-XNSQ*YPRED(I+6)))
YABPH      = X1R0*(XN*YPRED(I+6)-YPRED(I+4))
YAMPT      = (-1.0/(1R0/XD31)+(X1R0/XK33))*(-2.0*XN*YPRED(I+7)+XN*X1R0*
1      YPRED(I+5)+YPRED(I)/XK33+YABPH*(X1*SAVY(3)+X2*
2      SAVY(6)))
YA JPH      = YPRED(I+2)-YPRED(I+1)*(X1*SAVY(3)+X2*SAVY(6))
1      -YPRED(I+7)*(X1*SAVY(2)+X2*SAVY(5))
YANPT      = YPRED(I)*YAMPT*X1R0
YD0T(I+4)  = XN*YPRED(I+5)*X1R0+YPRED(I)/XK33+YAMPT*X1R0/XK33
1      +YABPH*(X1*SAVY(3)+X2*SAVY(6))
YD0T(I)    = XN*YANTH*X1R0-XN*YANTH*X1R0SQ-K*(XFTHLD+XMPHLD*X1R0)

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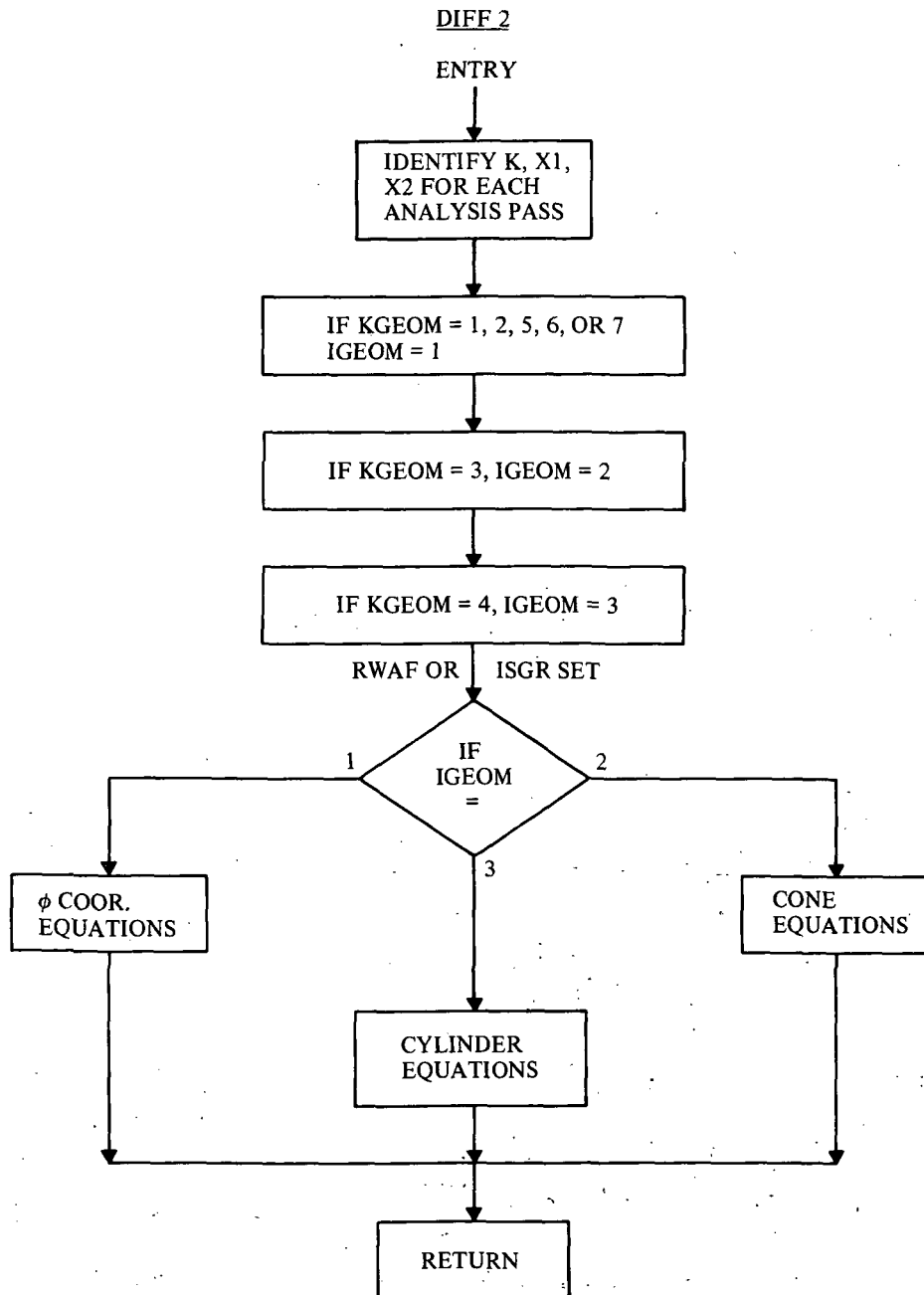
1      -(YD0T(I+4)*(X1*XFPHL1+X2*XFPHL2)+YA0PH*(X1*XFZEL1+
2      X2*XFZEL2))-X1R0*(YA0PH*(X1*SAVY(1)+X2*SAVY(4))-YANPT*
3      (X1*SAVY(3)+X2*SAVY(6)))
      YD0T(I+5) = -YPRED(I+7)*(X1*SAVY(3)+X2*SAVY(6))*(1-0/(XK22+XC22**2
1      /XD22))*(YPRED(I+1)+K*XNTPH+(XC22/XD22)*(YPRED(I+3)
2      +K*XNTPH)-(XK21*X1R0)*(XN*YPRED(I+4))-YPRED
3      (I+6))-(XC22*XD21/XD22)*(X1R0SQ*(XN*(YPRED(I+4))-XN*YPRE
      D(I+6))))
      EPSITH = X1R0*(XN*YPRED(I+4))-YPRED(I+6))
      EPSIPH = YD0T(I+5)+YPRED(I+7)*(X1*SAVY(3)+X2*SAVY(6))
      YD0T(I+1) = -XN*X1R0*YPRED(I)-XN*YAMPT*X1R0SQ-K*XFPHL2-(EPSITH+
1      EPSIPH)*(X1*XFPHL1+X2*XFPHL2)+YPRED(I+7)*(X1*XFZEL1+
2      X2*XFZEL2)
      YD0T(I+2) = -YANTH*X1R0+XNSQ*YAMTH*X1R0SQ+K*(XN*XMPHLD*X1R0-
1      XFZEL2)-(EPSITH+EPSIPH)*(X1*XFZEL1+X2*XFZEL2)-
2      YPRED(I+7)*(X1*XFPHL1+X2*XFPHL2)-X1R0*XN*(YANPT*
3      (X1*SAVY(3)+X2*SAVY(6))-YA0PH*(X1*SAVY(1)+X2*SAVY(4)))
      YD0T(I+3) = -2-0*XN*YAMPT*X1R0+YAJPH+K*XMTHLD
      YD0T(I+6)=YPRED(I+7)
      YD0T(I+7) = -(XC22/(XC22**2+XK22*XD22))*(YPRED(I+1)+K*XNTPH-XK21*
1      X1R0*X1
2      XN*YPRED(I+4))-YPRED(I+6)))+(XK22/(XC22**2+XK22*XD22))*(
3      YPRED(I+3)+K*XNTPH)-(XK22*XD21/(XC22**2+XK22*XD22))*(
      X1R0SQ*(XN*YPRED(I+4))-XNSQ*YPRED(I+6)))
9005 CONTINUE
      RETURN
      END

```

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```

C ..... ROUTINE **D6 ** ABACUS UPDATED 07/07/72 .....
SUBROUTINE DIFF2 (XPHL1,XFZEL1,XFPHL2,XFZEL2)
INTEGER SAVJTC,SAVSTP,Q,THICK
INTEGER XN1,XN
DOUBLE PRECISION YPRED
DOUBLE PRECISION SAVTIC,TIC,PHI,STOP,RESTOP,RTICK
1 YDOT,YASAVE,YANTH,YAMPT,YAJPH,S,SN,CS,SNSQ,
2 CSSQ,TAN,SEC,CN,X1CS,X1SN,TN,X1R0,X1R0SQ,X1SNR0,
3 X1CSR0,CNIR0,SNIR0,CSIR0,X1R1,X1R2,CSIR1,CSIR2,
4 SNIR1,X1R1SQ,R2SQ,R0SQ,XNSQ,R1,R2,S1,
5 R1D0T,XN1TH,XN1TPH,XN1TH,XN1TPH,XC11,XC22,XC15,
6 X033,X022,XD21,XD12,XK11,XK12,XK21,XK22,XK33,
7 X011,XNPHI,BETA,XC16
COMMON STORY(16),XMAT(110,10),STD(10),RADUS(30),
COMMON TADUS(30),UADUS(30),SAVTIC(900)
COMMON XN,TEREE,TIC,PHI,STOP,RESTOP,RTICK,G1,XNL(2),NH
COMMON NST(30),NKL(30),NXMAT(20),SAVJTC(30),SAVSTP(30),JRTIC(30)
COMMON JRST0P(30),NREG,NMPT,NRC,NSC,NIX,IERR0R,KGE0M,IGE0M,ISTTAB
COMMON KELVIN,IBEGIN,NPR0B,NSEG,NERR0R,Q,THICK,N0JS,NLINKS,NLCASE
COMMON NTSKL,NZ,NBCT,LINPUT,NTRKL,NPASS,XN1,KBC,NRINGS
COMMON /EQUAZN/ YPRED(80),YDOT(80),YASAVE(80),
1 YANTH,YAMTH,YAMPT,YAJPH,
2 S,SN,CS,SNSQ,CSSQ,TAN,SEC,CN,X1CS,X1SN,IN,
3 XIR0,XIR0SQ,X1SNR0,X1CSR0,CNIR0,SNIR0,CSIR0,
4 XIR1,XIR2,CSIR1,CSIR2,SNIR1,XIR1SQ,R2SQ,R0,BESQ,
5 R0SQ,XNSQ,BETA,R1,R2,S1,R1D0T,
6 XN1TH,XN1TPH,XN1TH,XN1TPH,XFTHLD,XFPHLD,XFZELD,
7 XNTHLD,XMPHLD,ETHET(2),EPHI(2),XGPT(2),ALPHTH(2),ALPHPH(2),DUM,
8 XNUPT,XNUPT,XC11,XC22,XC15,XD33,XD22,XD21,XD12,
9 XK11,XK12,XK21,XK22,XK33,XD11,
A XNPHI,N,I,BETTA,ZETTA,SAVY(8),XC16
EQUIVALENCE (XNL(1),X1),(XNL(2),X2)
IGE0M = 0
IF (KBC.EQ.1.0R.KGE0M.EQ.2.0R.KGE0M.EQ.5.0R.KGE0M.EQ.6) IGE0M = 1
IF (KGE0M.EQ.3) IGE0M = 2
IF (KGE0M.EQ.4) IGE0M = 3
IF (KGE0M.EQ.7) IGE0M = 1
K = 0
IF (KBC.EQ.0.AND.NH.EQ.0) K = 1
7447 G0 T0 (7341,7342,7343),IGE0M
C THE FOLLOWING EQUATIONS ARE THE -RWAF- SET
C EQUATIONS FOR SHELLS OF REVOLUTION ( PHI COORDINATE )
7341 YANTH = (YPRED(1+1)+K*XNTPH)*(XC15*XC22+XD22*XK12)/(XK22*XD22+
1 XC22*XD22+KX22*XD22)+X1R0*(XN*YPRED(1+4)+YPRED(1+5)*CS-
2 YPRED(1+6)*SN)*(XK11+XC15*(XC15*XC22-2.0*XK12*XC22)-XK12*XK12*
3 XD22)/(XK22*XD22+KX22*XD22)+(X1R0SQ*(XN*YPRED(1+4)*SN-XNSQ
4 *YPRED(1+6))+X1R0*YPRED(1+7)*CS)*I-XC11+(XC15*XC15*XC22+
5 XC15*(XK12*XD22+KX22*XD12)-XK12*XD22*XD22)/(XK22*XD22+KX22*XD22)
6 YAMTH = (YPRED(1+3)+K*XNTPH)*(XC15*XC22+KX22*XD12)/(XK22*XD22+
1 XC22*XD22)+(YPRED(1+1)+K*XNTPH)*(XD22*XC15-XD12*XK22)/(XD22*XD22+
2 XC22*XD22)-K*XNTPH*(X1R0SQ*(XN*YPRED(1+4)*SN-XNSQ*YPRED(1+6))+
3 X1R0*YPRED(1+7)*CS)*IXD11-(XD12*XD12*XK22+XC15*(2.0*XC22*XD12-
4 XD22)/(XC22*XD22+KX22*XD22))+X1R0*(XN*YPRED(1+4)+YPRED(1+5)*CS-
5 YPRED(1+6)*SN)*(XC11+XD12*XC22+KX12-XC15*(XC15*XD22+XD12*XK22+
6 XD22*XK12)/(XC22*XD22+KX22*XD22))
YAPPH = XN*YPRED(1+6)+X1R0-YPRED(1+4)*SNIR0
YAMPT = (1.0/(XC16*SN*X1R0-XK33-SN*X1R0*(XD33*SN/(
1 *(XK33*XD33-XC16**2)*X1R0*(-2.0*XN*YPRED(1+7)+YPRED(1+4)*

```

```

2 (CS*X1R1-CNIR0)+XN*YPRD(I+5)*(X1R1+SNIR0)+2.0*XN*YPRD 600600
3 (I+6)*CS*X1R0+YA0PH*SN*(X1*SAVY(3)+X2*SAVY(6))+YPRD(I)* 600610
4 {XD33*SN*X1R0-XC16}} 600620
YA0PH = YPRD(I+2)-YPRD(I+1)*(X1*SAVY(3)+X2*SAVY(6)) 600630
1 -YPRD(I+7)*(X1*SAVY(2)+X2*SAVY(5)) 600640
YANPT = YPRD(I)+YAMPT*SNIR0 600650
YD0T(I+4) = R1*(YPRD(I+4)*CS*X1R0+YA0PH*(X1*SAVY(3)+X2*SAVY(6)) 600660
+XN*YPRD(I+5)*X1R0+1.0/(XK33- 600670
XC16**2/XD33))*(YPRD(I)+YAMPT*(SN*X1R0-XC16/XD33)) 600680
1 YD0T(I) = R1*(-2.0*YPRD(I)*CS1R0+XN*YANTH*X1R0-XN*YANTH*SN* 600690
X1R0SQ-YAMPT*CS1R0*(X1R1-SNIR0))-R1*(XETHLD+XMPHLD+ 600700
SNIR0)-(YD0T(I+4)*(X1*XFPHL1+X2*XFPHL2)+R1*YA0PH* 600710
(X1*XFZEL1+X2*XFZEL2))-R1*SNIR0*(YA0PH*(X1*SAVY(1)+ 600720
X2*SAVY(4))-YAMPT*(X1*SAVY(3)+X2*SAVY(6))) 600730
YD0T(I+5) = YPRD(I+6)-R1*YPRD(I+7)*(X1*SAVY(3)+X2*SAVY(6))+R1* 600740
(XD22*(YPRD(I+1)+K*XNTPH)+XC22*(YPRD(I+3)+K*XMTPH)- 600750
X1R0*(XN*YPRD(I+4)+YPRD(I+5)*CS-YPRD(I+6)*SN)* 600760
(XK12*XD22+XC15*XC22)-(X1R0SQ*(XN*YPRD(I+4)-XNSQ* 600770
/(XK22*XD22+XC22**2)) 600780
EPSITH = X1R0*(XN*YPRD(I+4)+YPRD(I+5)*CS-YPRD(I+6)*SN) 600790
LPSIPH = X1R1*(YD0T(I+5)-YPRD(I+6))+YPRD(I+7)*(X1*SAVY(3)+ 600800
X2*SAVY(6)) 600810
1 YD0T(I+1) = R1*(CS1R0*(YANTH-YPRD(I+1))-XN*X1R0*(YPRD(I)+ 600820
YAMPT*(SN*X1R0+X1R1))+YPRD(I+2)*X1R1)-R1*(K*XFPHL 600830
-R1*(EPSITH+EPSIPH)*(X1*XFPHL1+X2*XFPHL2)-YPRD(I+7)* 600840
(X1*XFZEL1+X2*XFZEL2)) 600850
YD0T(I+2) = R1*(-YPRD(I+2)*CS1R0-YANTH*SNIR0-YPRD(I+1)*X1R1 600860
+XNSQ*YAMTH*X1R0SQ-2.0*XN*YAMPT*CS*X1R0SQ)+R1*(K* 600870
(XN*XMPHLD+X1R0-XFZELD)-R1*(EPSITH+EPSIPH)*(X1* 600880
XFZEL1+X2*XFZEL2))+YPRD(I+7)*(X1*XFPHL1+X2*XFPHL2)) 600890
4 -R1*X1R0*(XN*(YAMPT*(X1*SAVY(3)+X2*SAVY(6))-YA0PH* 600900
(X1*SAVY(1)+X2*SAVY(4))) 600910
YD0T(I+3) = R1*(YANTH*CS1R0-YPRD(I+3)*CS1R0-2.0*XN*YAMPT*X1R0+ 600920
YA0PH*(XN*YTHLD)) 600930
YD0T(I+6) = R1*(YPRD(I+7)-YPRD(I+5)*X1R1) 600940
YD0T(I+7) = R1*(XC22*(YPRD(I+3)+K*XMTPH)-XC22*(YPRD(I+1)+K* 600950
XNTPH)+X1R0 600960
1*(XN*YPRD(I+4)+YPRD(I+5)*CS-YPRD(I+6)*SN)*(XK12*XC22-XK22*XC15) 600970
2-(X1R0SQ*(XN*YPRD(I+4)*SN-XNSQ*YPRD(I+6))+X1R0*YPRD(I+7)*CS)* 600980
3(XC15*XC22+XC22*XD12)/(XC22**2+XC22*XD22) 600990
60 10 9005 601000
601010
C EQUATIONS FOR CUNE 601020
7342 YANTH = (YPRD(I+1)+K*XNTPH)*(XC15*XC22+XD22*XK12)/(XK22*XD22+ 601030
1 XC22**2)-K*XNTTH*(XK12*XC22-XK22*XC15)*(YPRD(I+3)+K*XMTPH)/ 601040
2 (XC22*XC22+XC22*XD22)+(XN*YPRD(I+4)+YPRD(I+5)*CS-YPRD(I+6) 601050
3 *SN)/(S*CS)*(XK11+(XC15*(XC15*XK22-2.0*XK12*XC22)-XK12*XK12* 601060
4 XD22)/(XK22*XD22+XC22*XC22)))+(XN*YPRD(I+4)*SN-XNSQ* 601070
5 YPRD(I+6))/(S*S*CSQ)+YPRD(I+7)/S)*(X11+(XC15*XC15*XC22+ 601080
6 XC15*(XK12*XD22+XC22*XD12)-XK12*XD12*XC22)/(XK22*XD22+XC22*XC22)) 601090
YAMTH = (YPRD(I+3)+K*XNTPH)*(XC15*XC22+XC22*XD12)/(XK22*XD22+ 601100
1 XC22**2)+(YPRD(I+1)+K*XNTPH)*(XD22*XC15-XD12*XC22)/(XD22*XK22+ 601110
2 XC22**2)-K*XNTTH*1.0/(S*S*CSQ)*(XNSQ*YPRD(I+6)+XN*YPRD(I+4)* 601120
3 SN+YPRD(I+7)/S)*(XD11-(XD12*XD12*XC15*(2.0*XC22*XD12-XC15* 601130
4 XD22))/(XC22*XC22+XC22*XD22))+1.0/(S*CS)*(XN*YPRD(I+4)+ 601140
5 YPRD(I+5)*CS- 601150
6 YPRD(I+6)*SN)*(XC11+(XD12*XC22*XK12-XC15*(XC15*XC22+XD12*XK22+ 601160
7 XD22*XK12))/(XC22*XC22+XC22*XD22)) 601170
YA0PH = XN*YPRD(I+6)*X1CS/S-YPRD(I+4)*TAN/S 601180
YAMPT = ((XC16*TAN/S-XK33-(TAN/S)*(XD33*TAN/S-XC16))*(-1))*(XK33* 601190
1 XD33-XC16**2)*(1.0/(S*CS1)+(XNSQ*YPRD(I+7)-YPRD(I+4)* 601200

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2 SN/S+XN*YPRD(I+5)*TAN/S+2.0*XN*YPRD(I+6)/S)+YA0PH*SN*
3 (X1*SAVY(3)+X2*SAVY(6))+YPRD(I+1)*(XD33*TAN/S-XC16))
YA0PH = YPRD(I+2)-YPRD(I+1)*(X1*SAVY(3)+X2*SAVY(6))
1 YANPT = YPRD(I+7)*(X1*SAVY(2)+X2*SAVY(5))
YANPT = YPRD(I+1)+YAMPT*TAN/S
YD0T(I+4) = YPRD(I+4)/S+YA0PH*(X1*SAVY(3)+X2*SAVY(6))+XN*
YPRD(I+5)/(S*CS)+(1.0/(XK33-XC16**2/
1 XD33))*YPRD(I+1)+YAMPT*(TAN/S-XC16/XD33))
1 YD0T(I) = -2.0*YPRD(I)/S+XN*YANTH*XICS/S-XN*YAMTH*SN*XICS**2/S**2
+YAMPT*TAN/S**2-K*(XFTHLD+XMPHLD*TAN/S)-(YD0T(I+4)*
1 (X1*XFPHL1+X2*XFPHL2)+YA0PH*(X1*XFZEL1+X2*XFZEL2))-
2 TAN/S*(YA0PH*(X1*SAVY(1)+X2*SAVY(4))-YANPT*(X1*SAVY(3)
3 +X2*SAVY(6)))
4 YD0T(I+5) = -YPRD(I+7)*(X1*SAVY(3)+X2*SAVY(6))+XD22*(YPRD(I+1)
+K*XNTPH)+XC22*(YPRD(I+3)+K*XMTPH)-(XK12*
1 XD22*XC15*XC22)*(1.0/(S*CS))*(XN*YPRD(I+4)+YPRD(I+5)*
2 CS-YPRD(I+6)*SN))-(XC22*XD12-XC15*XD22)*((-XNSQ*
3 YPRD(I+6)+XN*YPRD(I+4)*SN)/(S*CS*SSQ)+YPRD(I+7)/S))
4 /XK22*XD22+XC22*XC22)
EPSITH = (1.0/(S*CS))*(XN*YPRD(I+4)+CS*YPRD(I+5))-SN*
1 YPRD(I+6))
EPSIPH = YD0T(I+5)+YPRD(I+7)*(X1*SAVY(3)+X2*SAVY(6))
YD0T(I+1) = -YPRD(I+1)/S+YANTH/S-XN*YPRD(I)/(S*CS)-XN*YAMPT*SN/
1 XFPHL2)+YPRD(I+7)*(X1*XFZEL1+X2*XFZEL2)
2 YD0T(I+2) = -YPRD(I+2)/S-YANTH*TAN/S+XNSQ*YANTH/(S*CS**2)
-2.0*XN*YAMPT/(S**2*CS)+K*(XN*XMPHLD*XICS/S-XFZEL0)
1 -EPSITH+EPSIPH*(X1*XFZEL1+X2*XFZEL2)-YPRD(I+7)*
2 (X1*XFPHL1+X2*XFPHL2)-XICS/S*XN*(YANPT*(X1*SAVY(3)+
3 X2*SAVY(6))-YA0PH*(X1*SAVY(1)+X2*SAVY(4)))
4 YD0T(I+3) = YAMTH/S-YPRD(I+3)/S-2.0*XN*YAMPT/(S*CS)+YAJPH+XMTHLD
*K
1 YD0T(I+6)=YPRD(I+7)
YD0T(I+7) = (XK22*(YPRD(I+3)+K*XMTPH)-XC22*(YPRD(I+1)+K*XNTPH)+
1 (XK12*XC22-XK22*XC15)*(1.0/(S*CS))*(XN*YPRD(I+4)+
2 YPRD(I+5)*CS-YPRD(I+6)*SN))-(XC15*XC22+XK22*XD12)*
3 ((-XNSQ*YPRD(I+6)+XN*YPRD(I+4)*SN)/(S*CS*SSQ)+
4 YPRD(I+7)/S))/(XK22*XD22+XC22*XC22)
G0 T0 9005
C EQUATIONS FOR CYLINDER
7343 YANTH = (YPRD(I+1)+K*XNTPH)*(XC15*XC22+XD22*XK12)/(XK22*XD22+
1 XC22**2)-K*XNTTH+XK12*XC22-XK22*XC15)*(YPRD(I+3)+K*XMTPH)/
2 (XC22*XC22+XK22*XD22)+X1R0*(XN*YPRD(I+4))-
3 YPRD(I+6))*(XK11+XC15*(XC15*XC22-2.0*XK12*XC22)-XK12*XK12*
4 XD22)/(XK22*XD22+XC22*XC22)+(X1R0SQ*(XN*YPRD(I+4))-XNSQ
5 *YPRD(I+6))*(XC11+XC15*XC15*XC22+
6 XC15*(XK12*XD22+XK22*XC12)-XK12*XD12*XC22)/(XK22*XD22+XC22*XC22))
YAMTH = (YPRD(I+3)+K*XMTPH)*(XC15*XC22+XK22*XD12)/(XK22*XD22+
1 XC22**2)+YPRD(I+1)+K*XNTPH*(XD22*XC15-XD12*XC22)/(XK22*XD22+
2 XC22**2)-K*XMTTH+X1R0SQ*(XN*YPRD(I+4))-XNSQ*YPRD(I+6))
3 *XD11-(XD12*XD12*XK22*XC15*(2.0*XC22*XD12-XC15*
4 XD22)/(XC22*XC22+XK22*XD22))+X1R0*(XN*YPRD(I+4))-
5 YPRD(I+6))*(XC11+XC12*XC22*XK12-XC15*(XC15*XC22+XK12*XC22+
6 XD22*XK12))/(XC22*XC22+XK22*XD22)
YA0PH = X1R0*(XN*YPRD(I+6))-YPRD(I+4))
YAMPT = (1/(XC16*X1R0-XK33-X1R0*(XD33*X1R0-XC16)))*(XK33*XD33-XC16
1 **2)*X1R0*(-2.0*XN*YPRD(I+7)+XN*X1R0*YPRD(I+5))+YA0PH*
2 (X1*SAVY(3)+X2*SAVY(6))+YPRD(I+1)*(XD33*X1R0-XC16))
YA0PH = YPRD(I+2)-YPRD(I+1)*(X1*SAVY(3)+X2*SAVY(6))
1 -YPRD(I+7)*(X1*SAVY(2)+X2*SAVY(5))
YANPT = YPRD(I+1)+YAMPT*X1R0

```

```

YD0T(I+4) = (YA0PH*(X1*SAYV(3)+X2*SAYV(6))+XN*YPRED(I+5)/R0)+
1 (1-0/(XK33-XC16**2/XD33))*(YPRED(I)+
1 YAMPT*(X1R0-XC16/XD33))
YD0T(I) = XN*YANTH*X1R0-XN*YANTH*X1R0SQ-K*(XFTHLD+XMPHLD*X1R0)
1 - (YD0T(I+4)*(X1*XFPHL1+X2*XFPHL2)+YA0PH*(X1*XFZEL1+
2 X2*XFZEL2))-X1R0*(YA0PH*(X1*SAYV(1)+X2*SAYV(4))-YAMPT*
3 (X1*SAYV(3)+X2*SAYV(6)))
YD0T(I+5) = -YPRED(I+7)*(X1*SAYV(3)+X2*SAYV(6))+{XD22*(YPRED(I+1)
1 +K*XNTPH)+XC22*(YPRED(I+3)+K*XMTPH)-X1R0*
1 (XN*YPRED(I+4)-YPRED(I+6))*(XK12*XD22+XC15*XC22)-X1R0SQ*(XN*YPRED
2 (I+4)-XNSQ*YPRED(I+6))*(XC22*XD12-XC15*XD22)}/(XK22*XD22+XC22**2)
EPSITH = X1R0*(XN*YPRED(I+4)-YPRED(I+6))
YD0T(I+1) = -XN*X1R0*YPRED(I)-XN*YAMPT*X1R0SQ-K*XFPHLD-(EPSITH+
1 EPSIPH)*(X1*XFPHL1+X2*XFPHL2)+YPRED(I+7)*(X1*XFZEL1+
2 X2*XFZEL2)
YD0T(I+2) = -YANTH*X1R0+XNSQ*YANTH*X1R0SQ+K*(XN*XMPHLD*X1R0-
1 XFZELD)-(EPSITH+EPSIPH)*(X1*XFZEL1+X2*XFZEL2)-
2 YPRED(I+7)*(X1*XFPHL1+X2*XFPHL2)-X1R0*XN*(YAMPT*
3 (X1*SAYV(3)+X2*SAYV(6))-YA0PH*(X1*SAYV(1)+X2*SAYV(4)))
YD0T(I+3) = -2.0*XN*YAMPT*X1R0+YAJPH+K*XMTHL
YD0T(I+6)=YPRED(I+7)
YD0T(I+7) = (XK22*(YPRED(I+3)+K*XMTPH)-XC22*(YPRED(I+1)+K*XNTPH)
1 +X1R0*
1 (XN*YPRED(I+4)-YPRED(I+6))*(XK12*XC22-XK22*XC15)-X1R0SQ*(XN*YPRED
2 (I+4)-XNSQ*YPRED(I+6))*(XC15*XC22+XK22*XD12)}/(XC22**2+XK22*XD22)
9005 CONTINUE
RETURN
END

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SUBROUTINE SEGMAT

The results of the subroutine link, RIEMAN, are passed through the label common area, LYCORR, to this subroutine. SEGMAT places the elements of the YCORR array into several double-subscripted arrays, forms some coordinate transformation arrays, and calls subroutine SREVN2 for double precision matrix inversion.

As a result of appropriate matrix operations this subroutine produces a segment stiffness matrix, the XKS array, and a segment load matrix, the XLS array, for each segment. In passes other than the first pass, first cycle, the XLS array is not calculated. SEGMAT also orients each segment into the global coordinate system of the structure as a result of the matrix operations.

Subroutine SREVN2

SREVN2 is a subroutine called by SEGMAT to invert a real, double-precision, in-core matrix utilizing Gauss-Jordan elimination with partial pivoting.

FORTRAN CODE

ENGINEERING SYMBOLS (REF. 1)

SNI

si

SNJ

sj

CSI

ci

CSJ

cj

A MATRIX

$$\begin{bmatrix} \text{IFT} & 0 \\ 0 & \text{JFT} \end{bmatrix}$$

B MATRIX

$$\begin{bmatrix} 0 & I_4 & 0 \\ X_1 & X_2 & X_3 \end{bmatrix}$$

C MATRIX

$$\begin{bmatrix} I_4 & 0 & 0 \\ 0 & Y_2^{-1} & 0 \\ 0 & 0 & I_p \end{bmatrix}$$

D MATRIX

$$\begin{bmatrix} I_4 & 0 & 0 \\ -Y_1 & \text{JDT}^T & -Y_3 \\ 0 & 0 & I_p \end{bmatrix}$$

E MATRIX

$$\begin{bmatrix} \text{IDT}^T & 0 & 0 \\ 0 & I_4 & 0 \\ 0 & 0 & I_p \end{bmatrix}$$

XKT MATRIX

$$\begin{bmatrix} k & l \end{bmatrix}$$

XMAX MATRIX

$$\begin{bmatrix} 2\pi r_0(i) & \\ & 2\pi r_0(j) \end{bmatrix}$$

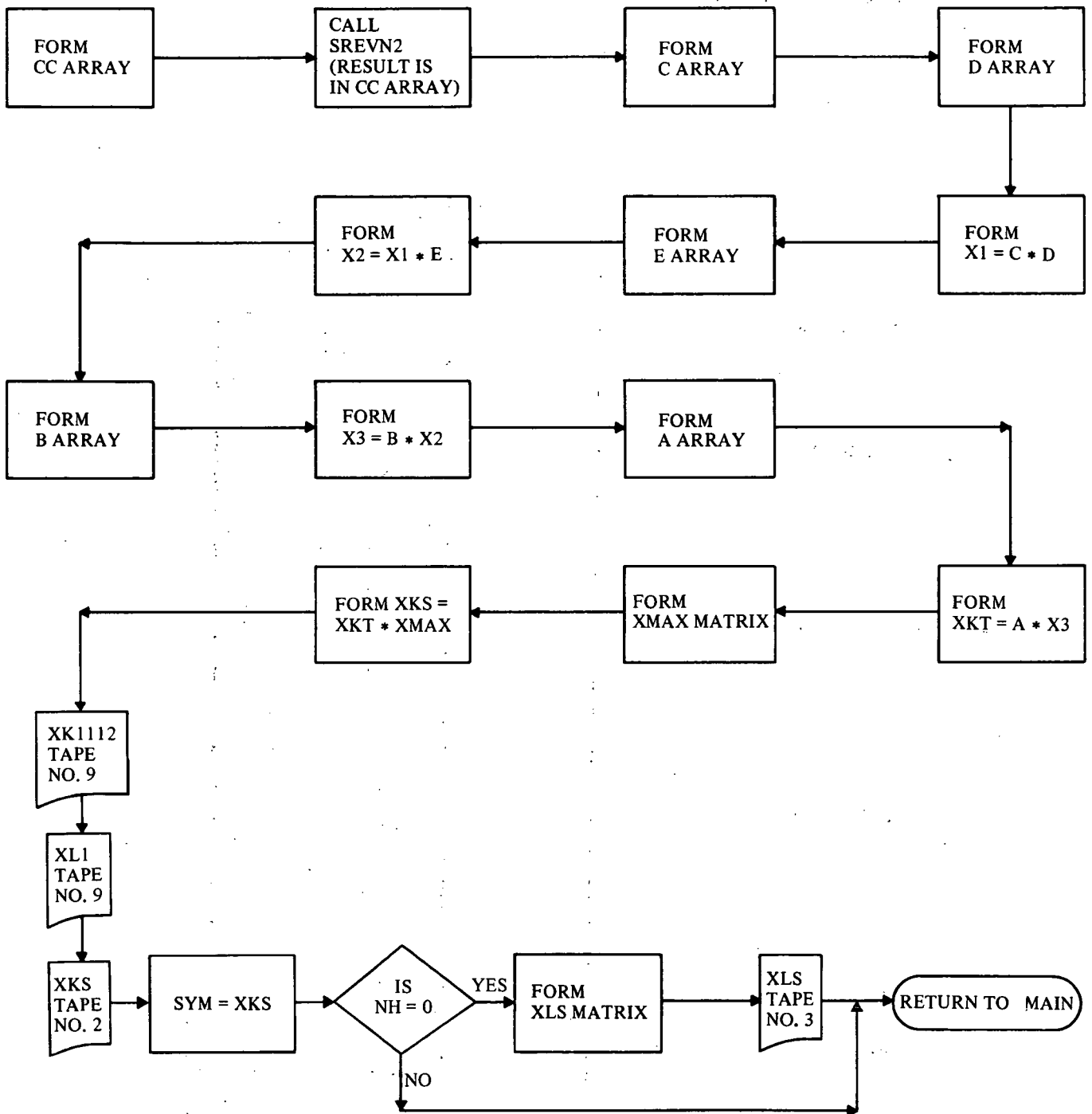
XKS MATRIX

$$s \begin{bmatrix} \hat{k} \end{bmatrix} (n)$$

XLS MATRIX

$$s \begin{bmatrix} \hat{l} \end{bmatrix} (n)$$

SEGMAT



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C ..... ROUTINE **D7 ** ABACUS UPDATED 07/07/72 .....
SUBROUTINE SEGMAI
  INTEGER SAVJTC, SAVSTP, Q, THICK
  INTEGER XN1, XN
  DOUBLE PRECISION SAVTIC, TIC, PHI, STØP, RESTØP, RTICK, YCØRR, A1
  DOUBLE PRECISION C, CC, D, E, B, A, X1, X2, X3, XKT, XMAX, XKS
  DOUBLE PRECISION RI, RJ, CSI, CSJ, SNI, SNJ, X2ØIRI, X2ØIRJ
  COMMON STØRY(16), XMAT(110,10), STDI(10), SADUS(30), RADUS(30)
  COMMON TADUS(30), UADUS(30), SAVTIC(900)
  COMMON XN, TEFREE, TIC, PHI, STØP, RESTØP, RTICK, G1, XN1(2), NH
  COMMON NST(30), NK1(30), NKMAT(20), SAVJTC(30), SAVSTP(30), JRTIC(30)
  COMMON JRSTØPI(30), NREG, NMPT, NRC, NSC, NIX, IERRØR, KGEØM, IGEØM, ISTDAB
  COMMON KELVIN, IØEGIN, NPRØB, NSEG, NERRØR, Q, THICK, NØJS, NLINKS, NLCASE
  COMMON NTSKL, NZ, NBCT, LINPUT, NTRKL, NPASS, XN1, KBC, NRINGS
  COMMON /LYCØRR/ YCØRR(80)
  DIMENSION C(18,18), CC(4,4), D(18,18), E(18,18), B(8,18), A(8,8)
  DIMENSION X1(18,18), X2(18,18), X3(18,18), XKT(18,18), XMAX(8,18)
  DIMENSION XKS(8,18), XLS(8,2), SYM(8,18)
  DIMENSION DEAD(4)
  DIMENSION LABEL(16)
  DIMENSION N1(2), N2(2), N3(2), N4(2)
  DIMENSION N5(2), N6(2), N7(2), N8(2)
  EQUIVALENCE (LABEL( 1), N1(1)), (LABEL( 3), N2(1))
  EQUIVALENCE (LABEL( 5), N3(1)), (LABEL( 7), N4(1))
  EQUIVALENCE (LABEL( 9), N5(1)), (LABEL(11), N6(1))
  EQUIVALENCE (LABEL(13), N7(1)), (LABEL(15), N8(1))
  EQUIVALENCE (C(1), E(1), X3(1), XMAX(1), XLS(1))
  EQUIVALENCE (X2(1), D(1), A(1), XKS(1)), (X1(1), B(1), XKT(1), SYM(1))
  SIN(X) = DSIN(X)
  COS(X) = DCOS(X)
  DATA N1 /8HFØRCE T1/,
  DATA N2 /8HFØRCE Z1/,
  DATA N3 /8HFØRCE R1/,
  DATA N4 /8HMØMENT 1/,
  DATA N5 /8HFØRCE T2/,
  DATA N6 /8HFØRCE Z2/,
  DATA N7 /8HFØRCE R2/,
  DATA N8 /8HMØMENT 2/
  IF (NH.EQ.0) WRITE(6,1726)
1726 FORMAT(1H1)
  A1=G1
  GØTØ (601,602,603), IGEØM
  601 SNI = SIN(TIC)
  SNJ = SIN(STØP)
  CSI = COS(TIC)
  CSJ = COS(STØP)
  GØTØ 1
  602 SNI = COS(1.570796-A1)
  SNJ = SNI
  CSI = SIN(1.570796-A1)
  CSJ = CSI
  GØTØ 1
  603 SNI = 1.0
  SNJ = 1.0
  CSI = 0.0
  CSJ = 0.0
  1 JJ = 8*NPRØB
  DØ 111 J=1,18
  DØ 111 I=1,18
  111 C(I,I,J)=0.0

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K=28
D0 112 J=1,4
K=K+8
L=K
D0 112 I=1,4
L=L+1
112 CC(I,J)=YC0RR(L)
CALL SREVN2 (CC,4,DEAD,4,NIX)
IF (NIX.NE.0) GOT0 8120
J1=0
D0 113 J=5,8
J1=J1+1
I1=0
D0 113 I=5,8
I1=I1+1
113 C(I,J)=CC(I,I,J1)
D0 114 IJ=1,4
114 C(IJ,IJ)=1.0
D0 115 IJ=9,JJ
115 C(IJ,IJ)=1.0
D0 116 J=1,18
D0 116 I=1,18
116 O(I,J)=0.0
D0 117 IJ=1,4
117 O(IJ,IJ)=1.0
I=5
D(I,I)=1.0
D(I+1,I+1)=-SNJ
D(I+2,I+2)=-SNJ
D(I+3,I+3)=1.0
D(I+1,I+2)=CSJ
D(I+2,I+1)=-CSJ
D0 218 IJ=9,JJ
218 O(IJ,IJ)=1.0
K=-4
D0 118 J=1,4
K=K+8
L=K
D0 118 I=5,8
L=L+1
118 D(I,J)= -YC0RR(L)
K=60
D0 119 J=9,JJ
K=K+8
L=K
D0 119 I=5,8
L=L+1
119 D(I,J)=-YC0RR(L)
D0 120 J=1,JJ
D0 120 I=1,JJ
X1(I,J)=0.0
D0 120 M=1,JJ
120 X1(I,J)=X1(I,J)+C(I,M)*O(M,J)
D0 121 J=1,18
D0 121 I=1,18
121 E(I,J)=0.0
I=1
E(I,I)=1.0
E(I+1,I+1)=-SNI
E(I+2,I+2)=-SNI
E(I+3,I+3)=1.0

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E(I+1,I+2)=CSI
E(I+2,I+1)=-CSI
D0 122 J=5,JJ
122 F(I,J)=1.0
D0 123 J=1,JJ
D0 123 I=1,JJ
X2(I,J)=0.0
D0 123 M=1,JJ
123 X2(I,J)=X2(I,J)+X1(I,M)*E(M,J)
D0 124 J=1,JJ
D0 124 I=1,8
124 B(I,J)=0.0
J=4
D0 125 I=1,4
J=J+1
125 B(I,J)=1.0
K=-8
D0 126 J=1,4
K=K+8
L=K
D0 126 I=5,8
L=L+1
126 B(I,J)=YC0RR(L)
K = 24
D0 127 J=5,8
K=K+8
L=K
D0 127 I=5,8
L=L+1
127 B(I,J)=YC0RR(L)
K=56
D0 128 J=9,JJ
K=K+8
L=K
D0 128 I=5,8
L=L+1
128 B(I,J)=YC0RR(L)
D0 129 J=1,JJ
D0 129 I=1,8
X3(I,J)=0.0
D0 129 M=1,JJ
129 X3(I,J)=X3(I,J)+B(I,M)*X2(M,J)
D0 130 J=1,8
D0 130 I=1,8
130 A(I,J)=0.0
I=1
A(I,I)=-1.0
A(I+1,I+1)=SNI
A(I+2,I+2)=SNI
A(I+1,I+2)=CSI
A(I+2,I+1)=-CSI
A(I+3,I+3)=1.0
I=5
A(I,I)=1.0
A(I+1,I+1)=-SNJ
A(I+2,I+2)=-SNJ
A(I+3,I+3)=-1.0
A(I+1,I+2)=-CSJ
A(I+2,I+1)=CSJ
D0 131 J=1,JJ
D0 131 I=1,8

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XKT(I,J)=0.0
D0 131 M=1,8
131 XKT(I,J)=XKT(I,J)*A(I,M)*X3(M,J)
PI=3.1415927
RI=RTICK
X2PIR1=2.0*PI*RI
RJ=RESTOP
X2PIRJ=2.0*PI*RJ
D0 132 J=1,8
D0 132 I=1,8
132 XMAX(I,J)=0.0
D0 133 I=1,4
133 XMAX(I,I)=X2PIR1
D0 134 J=5,8
134 XMAX(J,J)=X2PIRJ
D0 135 J=1,JJ
D0 135 I=1,8
XKS(I,J)=0.0
D0 135 M=1,8
135 XKS(I,J)=XKS(I,J)+XMAX(I,M)*XKT(M,J)
D0 139 J=1,JJ
D0 139 I=1,4
139 SYM(I,J)=XKT(I,J)
WRITE(9) ((SYM(I,J),J=1,8),I=1,4),ICE0M,G1
IF (NH.EQ.0) WRITE(9) ((SYM(I,J),J=9,JJ),I=1,4)
IF (NH.EQ.0.OR.IBEGIN.EQ.1) WRITE(6,781)
781 FORMAT(/////////55X,22HSTIFFNESS COEFFICIENTS//14X,8HDELTA 11,7X,
1 8HDELTA 21,7X,8HDELTA R1,7X,7HTHETA 1,8X,8HDELTA 12,7X,8HDELTA 22
2 ,7X,8HDELTA R2,7X,7HTHETA 2)
III=0
D0 20 M=1,8
II=III+1
11=II+1
IF (NH.EQ.0.OR.IBEGIN.EQ.1) WRITE(6,23) (LABEL(I),I=II,III),
1 (XKS(M,J),J=1,8)
23 FORMAT(/1X,2A*,1X,8(E14.7,1X))
D0 20 J=1,8
SYM(M,J)=XKS(M,J)
20 CONTINUE
9968 FORMAT(1H ,8(E14.7,2X)/(5X,8(E14.7,2X)))
J1=8
ISEG=0
NRC1=NRC-1
IF(NRC1.EQ.0)GOTO 143
D0 244 I=1,NRC1
244 ISEG=ISEG+NST(II)
143 ISEG=ISEG+NSC
SAVTIC(ISEG)=TIC
WRITE(2) ((SYM(I,J),J=1,8),I=1,8)
D0 137 J=1,8
D0 137 I=1,8
137 SYM(I,J)=0.0
INDEC=0
D0 138 I=1,8
D0 138 J=1,8
IF(J.NE.1)G0 T0 138
IF(XKS(I,J).GE.0.0)G0 T0 138
INDEC=1
138 SYM(I,J)=XKS(I,J)
138 IF(INDEC.EQ.0)G0 T0 151
IF (NH.NE.0) G0 T0 151

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WRITE(6,152)
152 FORMAT(///- ***** WARNING - NEGATI
IVES APPEAR ON MAIN DIAGONAL. REVISE SIZING *****-//)
151 JJ=2
N = 8
J = 1
DO 42 II=1,7
M = JJ
DO 43 I=M,N
ALPH = ABS(SYM(I,J)) - ABS(SYM(J,I))
IF(ALPH) 47,71,48
47 IF(SYM(I,J).EQ.0.0) GOT0 71
SYM(I,J) = SYM(J,I) / SYM(I,J)
GOT0 43
48 IF(SYM(J,I).EQ.0.0) GOT0 71
SYM(J,I) = SYM(I,J) / SYM(J,I)
GOT0 43
71 SYM(I,J) = 1.0
43 SYM(J,I) = 0.0
JJ = JJ +1
J = J+1
42 CONTINUE
IF (INH.NE.0.AND.IBEGIN.NE.1) GOT0 145
WRITE(6,785)
785 FORMAT(//55X,22HSEGMENT SYMMETRY CHECK, )
DO 144 I=1,8
144 WRITE(6,9968) (SYM(I,J),J=1,8)
145 IF (NPR08.EQ.0) GOT0 9999
DO 136 J=1,NPR08
J1=J1+1
DO 136 I=1,8
136 XLS(I,J)=XKS( I,J1)
WRITE(3)((XLS(I,J),J=1,NPR08),I=1,8)
WRITE(6,782)
782 FORMAT(//55X,22HSEGMENT LOAD MATRICES , )
DO 840 I=1,8
840 WRITE(6,9968)(XLS(I,J),J=1,NPR08)
GOT0 9999
8120 IERR08=8120
NERR08=29
8888 NIX=1
9999 CONTINUE
IF (INH.EQ.0.OR.IBEGIN.EQ.1) WRITE(6,795) RTICK,REST0P
795 FORMAT( /- RZER0(I) =-,1PE15.6,10X,-RZER0(J) =-,1PE15.6)
RETURN
END

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C ..... ROUTINE **D8      ** ABACUS UPDATED 07/07/72 .....
SUBROUTINE SREVN2(A,M,L0C,MID,NIX)
DOUBLE PRECISION A(MID,1),PIV0T,TEMP1
INTEGER L0C(1)
100 N = M
D0 190 K = 1,N
PIV0T = 0.00
D0 120 I = K,N
IF (PIV0T - DABS(A(I,K))) 110,110,120
110 PIV0T = DABS(A(I,K))
L = I
120 CONTINUE
IF (PIV0T) 140,130,140
130 NIX = -1
G0 T0 210
140 L0C(K) = L
D0 150 J = 1,N
TEMP1 = A(K,J)
A(K,J) = A(L,J)
150 A(L,J) = TEMP1
TEMP1 = A(K,K)
A(K,K) = 1.00
D0 160 J = 1,N
160 A(K,J) = A(K,J)/TEMP1
D0 190 I = 1,N
IF (I - K) 170,190,170
170 TEMP1 = -A(I,K)
A(I,K) = 0.00
D0 180 J = 1,N
180 A(I,J) = A(I,J) + TEMP1*A(K,J)
190 CONTINUE
D0 200 K = 1,N
NK = N - K
L = L0C(NK+1)
D0 200 I = 1,N
TEMP1 = A(I,NK+1)
A(I,NK+1) = A(I,L)
200 A(I,L) = TEMP1
NIX = 0
210 RETURN
END

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SUBROUTINE REGMAT

The segment stiffness matrices, XKS, and the segment load matrices, XLS, are passed from SEGMAT to REGMAT via Tapes #2 and #3, and are placed in the XKRTOT array and the XLRTOT array, respectively. If kinematic links occur between segments in the region, the XKRTOT array and the XLRTOT array are modified to represent the situation. In the case of discrete rings the routine RINGER is called and provides the necessary matrices.

A horizontal and vertical partitioning of the XKRTOT array occurs while the XLRTOT array is subjected to a horizontal partitioning only. Appropriate matrix operations are performed upon the partitions of each array, thus reducing the size of the region stiffness and load matrices and resulting in increased program capacity. The results of these manipulations are the region stiffness matrix, XKR, and the region load matrix, XLR. In passes other than the first pass, first cycle, the load calculations are not performed.

Subroutines Called from REGMAT

Subroutine SWITCH: Is a routine used to arrange a matrix in a form convenient for use by another routine employing a positive definite method for solving linear algebraic equations.

Subroutine CHASE: Is a routine used to obtain the solution X of the linear system $AX = Y$, given at least one right side of Y and the positive, definite, symmetric, real coefficient matrix A .

Subroutine FUTILE: Is a routine called from CHASE and used to obtain the factorization of the positive definite, real, symmetric matrix A into the product of a lower triangular matrix and its transpose by utilizing a Cholesky decomposition.

Subroutine TRIEQ: Is a routine called by CHASE or EIGVAL to solve a triangular system of algebraic equations.

FORTRAN CODE

ENGINEERING SYMBOLS (REF. 1)

SKL MATRIX

$$[SKL]$$

SKLTR MATRIX

$$[SKL]^T$$

XKRTOT MATRIX

$$\begin{bmatrix} K'_{11} & K'_{12} \\ K'_{21} & K'_{22} \end{bmatrix}$$

XLRTOT MATRIX

$$\begin{bmatrix} L'_{iR1} \\ L'_{jR1} \\ L' \end{bmatrix}$$

SKL22 MATRIX

$$[SKL_{22}]$$

REGTOT MATRIX

$$\begin{bmatrix} K_{11} & K_{12} \\ K_{21} & K_{22} \end{bmatrix}$$

STORE MATRIX

$$\begin{bmatrix} L_{iR1} \\ L_{jR1} \\ L \end{bmatrix}$$

XK11 PARTITION

$$\begin{bmatrix} \hat{K}_{11} \end{bmatrix}$$

XK12 PARTITION

$$\begin{bmatrix} \hat{K}_{12} \end{bmatrix}$$

XK22 PARTITION

$$\begin{bmatrix} \hat{K}_{22} \end{bmatrix}$$

XK21 PARTITION

$$\begin{bmatrix} \hat{K}_{21} \end{bmatrix}$$

FORTRAN CODE.

ENGINEERING SYMBOLS (REF. 1)

XL1 PARTITION

$$\begin{bmatrix} \hat{L}_{R1} \end{bmatrix}$$

XL2 PARTITION

$$\begin{bmatrix} \hat{L} \end{bmatrix}$$

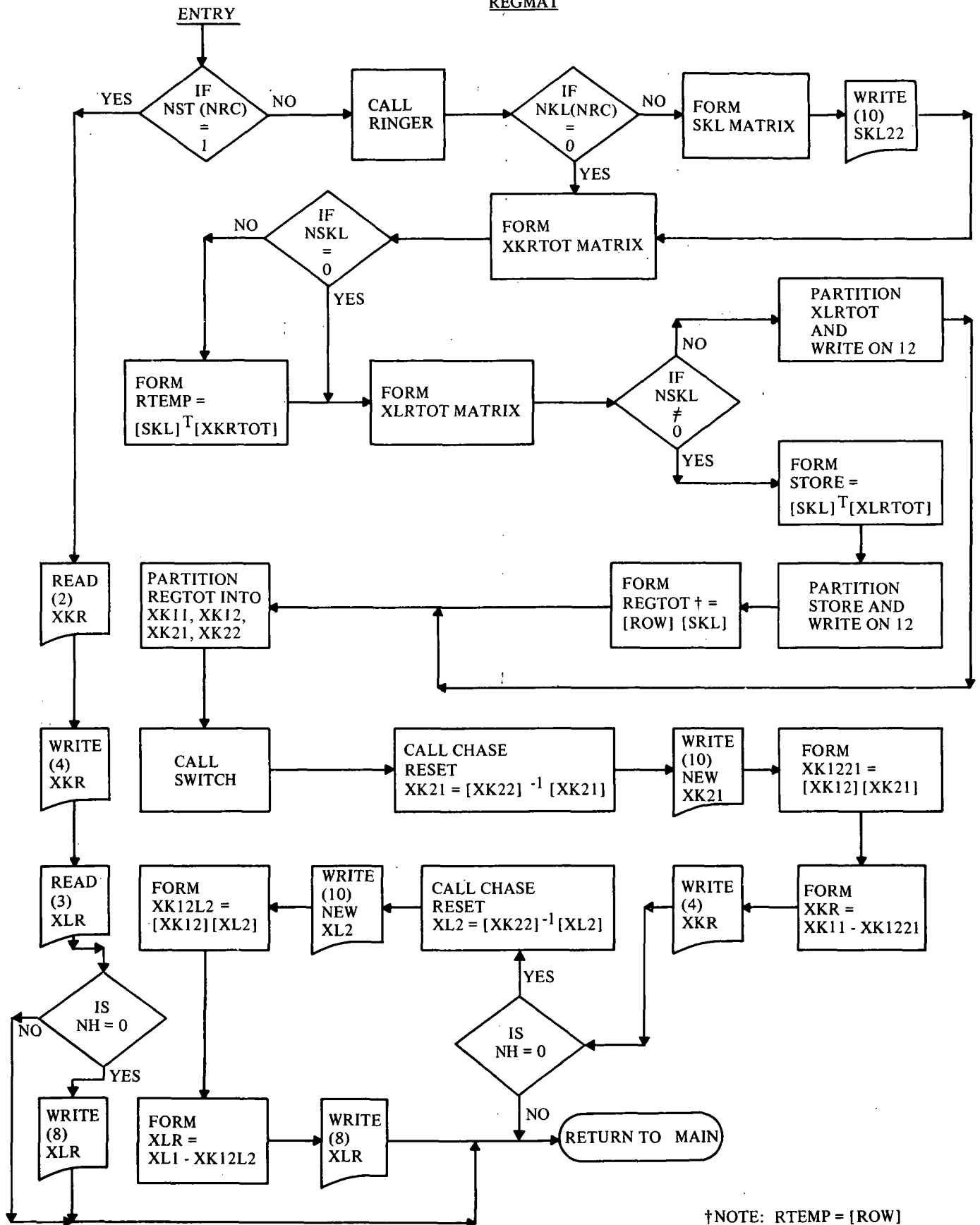
XKR MATRIX

$$\begin{bmatrix} \hat{K}_R \end{bmatrix}$$

XLR MATRIX

$$\begin{bmatrix} \hat{L}_R \end{bmatrix}$$

REGMAT



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C ..... ROUTINE **D9 ** ABACUS UPDATED 07/24/72 .....
SUBROUTINE REGMAT
INTEGER SAVJTC, SAVSTP, Q, THICK
INTEGER XN1, XN
COMMON STORY(16), XMAT(110,10), STD(10), SADUS(30), RADIUS(30)
COMMON RADUS(30), UADUS(30), SAVTIC(900)
COMMON XN1, TEFREE, TIC, PHI, ST0P, REST0P, RTICK, G1, XNL(2), NH
COMMON NST(30), NKL(30), NXMAT(20), SAVJTC(30), SAVSTP(30), JRTIC(30)
COMMON JRST0P(30), NREG, NMPT, NRC, NSC, NIX, IERR08, KGE0M, ICE0M, ISTIAB
COMMON KELVIN, IBEGIN, INPR0B, NSEG, NERR0R, Q, THICK, N0JS, NLINKS, NLCASE
COMMON NTSKL, NZ, NBCT, LINPUT, NTRKL, NPASS, XN1, KBC, NRINGS
COMMON /OPT2/ PRINT
COMMON /ARING/ RRING(28), AMAT(30,4), IRLC(28)
DIMENSION OPENI(4,4)
DIMENSION XTEMP(8,8), SKL(120,120), SKLTR(120)
DIMENSION SYM(8,8)
DIMENSION XKRTO(120,120), RTEMP(120), XLRTOT(120,2), XKEEP(8,2)
DIMENSION ST0RE(120,2), R0W(120), REGTO(120), H0LD(4,120)
DIMENSION XK2(112,112), XK1(8,8), XK12(8,112), XK21(112,8)
DIMENSION XKIV(6328), XK1221(8,8), XKR18(8,8)
DIMENSION XL1(8,2), XL2(112,2), XK12L2(8,2), XLR(8,2)
DIMENSION JDEP(112), JIND(15), ANGLE(15)
DIMENSION RNGTO(14,4), RNL0D(4,28), JTN0(28)
DIMENSION LABEL(16)
DIMENSION N1(2), N2(2), N3(2), N4(2)
DIMENSION N5(2), N6(2), N7(2), N8(2)
EQUIVALENCE (SYM(1), XK12L2(1), XK1221(1), H0LD(1), JDEP(1))
EQUIVALENCE (LABEL(1), N1(1), LABEL(3), N2(1))
EQUIVALENCE (LABEL(5), N3(1), LABEL(7), N4(1))
EQUIVALENCE (LABEL(9), N5(1), LABEL(11), N6(1))
EQUIVALENCE (LABEL(13), N7(1), LABEL(15), N8(1))
EQUIVALENCE (SKL(1), XKRTO(1), XK22(1), XKIV(1), XLRTOT(1))
EQUIVALENCE (XKR(1), XK1(1), XTEMP(1), XLR(1), XL1(1), XKEEP(1),
1 RTEMP(1), R0W(1))
EQUIVALENCE (SKLTR(1), REGTO(1), OPENI(1), XK12(1))
EQUIVALENCE (ST0RE(1), XL2(1), XK21(1))
DOUBLE PRECISION SAVTIC, TIC, PHI, ST0P, REST0P, RTICK
DATA N1 /8HF0RCE T1/
DATA N2 /8HF0RCE Z1/
DATA N3 /8HF0RCE R1/
DATA N4 /8HM0MENT 1/
DATA N5 /8HF0RCE T2/
DATA N6 /8HF0RCE Z2/
DATA N7 /8HF0RCE R2/
DATA N8 /8HM0MENT 2/
REWIND 2
REWIND 3
REWIND 12
D = 0.0
PRINT = 0.0
N0J = NST(NRC) + NKL(NRC) + 1
N0J4 = N0J*4
NSKL = NKL(NRC)
NH4 = 4
NJTNH4 = NH4*N0J
NJINK4 = (N0J-NSKL)*4
M8 = NJINK4-8
NKIV = NJINK4 - 8
IF (INST(NRC).EQ.1) G0T0 1
IF (INH.NE.0.AND.IBEGIN.NE.1) G0T0 690

```

```

1726 WRITE(6,1726)
    FORMAT(IHL)
681 WRITE(6,681) NRC,N0J,NSKL
    FORMAT(//251X3INPUT DATA FOR SEGMENT COUPLING//25X14HREGION NU
IMBER ,12,5X25HNUMBER OF SEGMENT JOINTS ,13,5X,26HNUMBER OF KINEMAT
2IC LINKS ,13//)
    WRITE(6,682)
682 FORMAT(1X,7HSEGMENT,11X,8HJ0INT(1),11X,8HJ0INT(J)//)
    DO 683 I=1,NSEG
        KTIC = SAVJTC(I)
        KST0P= SAVSTP(I)
        WRITE(6,684) I,KTIC,KST0P
684 FORMAT(43X,2(I3,16X),13)
683 CONTINUE
690 CONTINUE
        NNT = NST(NRC)
        DO 350 I=1,N0J4
            DO 350 J=1,N0J4
                350 XRT0(I,J)=0.0
591 FORMAT (315,16A4)
        DO 701 NS=1,NNT
            READ(2) ((XTEMP(I,J),J=1,8),I=1,8)
            J1 = SAVJIC(NS)
            J2 = SAVSTP(NS)
            I1 = 4*(J1-1)
            L = II
            IF (J1.GT.J2) G0T0 950
            DO 910 I = 1,8
                JJ = L
                II = II + 1
                DO 910 J = 1,8
                    JJ = JJ + 1
510 XRT0(II,JJ)=XRT0(II,JJ)+XTEMP(I,J)
                    G0T0 701
950 JJ = 4*(J2-1)+1
            II = II + 1
            DO 960 JK = 1,4
                G0T0 (951,952,953,954) , JK
951 IX = II
                IND = II
                DO 961 I=1,4
                    DO 961 J=1,4
961 OPEN(I,J) = XTEMP(I,J)
                G0T0 955
952 IX = II
                IND = JJ
                DO 962 I=1,4
                    DO 962 J=1,4
962 OPEN(I,J) = XTEMP(I,J+4)
                G0T0 955
953 IX = JJ
                IND = II
                DO 963 I=1,4
                    DO 963 J=1,4
963 OPEN(I,J) = XTEMP(I+4,J)
                G0T0 955
954 IX = JJ
                IND = JJ
                DO 964 I=1,4
                    DO 964 J=1,4
964 OPEN(I,J) = XTEMP(I+4,J+4)

```

```

955 D0 956 I=1,4
JX = IND
D0 957 J=1,4
XKRTOT(IX,JX) = XKRTOT(IX,JX) + OPEN(I,J)
957 JX = JX + 1
956 IX = IX + 1
960 CONTINUE
701 CONTINUE
NRNG = NRING(NRC)
IF (NRING(NRC).EQ.0) G0 T0 210
IF (Q.EQ.5) WRITE(6,300)
300 FORMAT(///)
MFLG = 1
D0 211 J=1,NRNG
CALL RINGER (Q,XN,RNGT0T,RNGL0D,J,RADUS,TADUS,SAVJTC,SAVSTP,JTN0,
1
JT = 4*(JTN0(J)-1)
D0 220 I=1,4
D0 220 IK=1,4
220 XKRTOT(JT+I,JT+IK) = XKRTOT(JT+I,JT+IK)+RNGT0T(I,IK)
211 CONTINUE
IF (Q.NE.5) G0 T0 210
WRITE(6,300)
READ(5,2000)
210 CONTINUE
REWIND 2
IF(NSKL.NE.0) G0 T0 931
D0 5504 I=1,N0J4
WRITE(2) (XKRTOT(I,J),J=1,N0J4)
5504 CONTINUE
G0 T0 101
931 CONTINUE
WRITE(12) ((XKRTOT(I,J),J=1,N0J4),I=1,N0J4)
REWIND 12
D0 501 J=1,NJTNH4
D0 501 I=1,NJTNH4
501 SKL(I,J)=0.0
IF (INH.EQ.0) WRITE(6,685)
685 FORMAT(/60X13HSEGMENT LINKS//43X8HJ0INT(J)5X8HJ0INT(I)5X20HANGLE
10F ORIENTATION//)
D0 103 NRIG = 1,NSKL
IF (Q.EQ.1) G0 T0 566
READ(5,503) JDEP(NRIG),JIND(NRIG),ANGLE(NRIG)
503 FORMAT (212,E14.7,15A4)
WRITE(1) JDEP(NRIG),JIND(NRIG),ANGLE(NRIG)
WRITE(6,686) JDEP(NRIG),JIND(NRIG),ANGLE(NRIG)
686 FORMAT(45X,I3,10X,I3,11X,E14.7)
IF(JIND(NRIG).GE.JDEP(NRIG)) G0 T0 8797
G0 T0 103
566 READ(1) JDEP(NRIG),JIND(NRIG),ANGLE(NRIG)
103 CONTINUE
IF (Q.EQ.5) READ(5,2000)
2000 FORMAT(1X)
J' = -3
N = 1
D0 100 IJ = 1,N0J
I = 4*IJ-3
IF(IJ.EQ.JDEP(N)) G0T0 11
J = J + 4
G0T0 12
11 JD = JDEP(N)

```

```

JI = JIND(N)
COTAN = COS(ANGLE(N))/SIN(ANGLE(N))
IF (N.LT.NRIG) N=N+1
SKL( I, J) = RADUS(JD)/RADUS(JI)
SKL(I+1,J+3) = -(RADUS(JD)-RADUS(JI))
SKL(I+2,J+3) = -SKL(I+1,J+3)*COTAN
GOT0 13
12 SKL( I, J) = 1.0
13 SKL(I+1,J+1) = 1.0
SKL(I+2,J+2) = 1.0
SKL(I+3,J+3) = 1.0
100 CONTINUE
5000 FORMAT(1H,8(E14.7,2X)/(5X,8(E14.7,2X)))
II = N0J4 - 4
JJ = NJINK4 - 4
D0 768 I=5,II
768 WRITE(10) (SKL(I,J),J=5,JJ)
D0 702 J=1,NJINK4
702 WRITE(2) (SKL(I,J),I=1,N0J4)
WRITE(2) ((SKL(I,J),J=1,NJINK4),I=1,N0J4)
REWIND 2
READ(12) ((XKRT0T(I,J),J=1,N0J4),I=1,N0J4)
REWIND 12
1000 CONTINUE
D0 740 I=1,NJINK4
740 READ(12) (SKL(I,J),J=1,N0J4)
D0 741 J=1,N0J4
RTEMP (J)=0.0
D0 741 K=1,N0J4
741 RTEMP (J)=RTEMP (J)+SKL(I,K)*XKRT0T(K,J)
WRITE(12) (RTEMP (J),J=1,N0J4)
740 CONTINUE
REWIND 12
101 IF (NPR0B.EQ.0) G0 T0 1001
REWIND 2
D0 436 I=1,N0J4
D0 436 J=1,NPR0B
436 XLRT0T(I,J)=0.0
D0 971 NS = 1,NNT
JTIC = SAVJTIC(NS)
JST0P= SAVJSTIC(NS)
READ (3) ((XKEEP(I,J),J=1,NPR0B),I=1,8)
D0 971 N =1,2
G0T0 (981,982),N
981 II = (JTIC-1)*4 + 1
III= II + 3
G0T0 983
982 II = (JST0P-1)*4 + 1
III= II + 3
983 D0 971 J=1,NPR0B
I=0
IF (N.EQ.2) I=4
D0 971 IL = II,III
I = I + 1
971 XLRT0T(IL,J)= XLRT0T(IL,J)+ XKEEP(I,J)
IF (NRNG.EQ.0) G0 T0 230
D0 225 J=1,NRNG
JT = 4*(JTN0(J)-1)
D0 226 I=1,4
D0 226 IK=1,NPR0B
IF (IK.EQ.1.AND.IRLC(J).EQ.2) G0 T0 226

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```

          XLRTOT(JT+I,IK) = XLRTOT(JT+I,IK)+RNGLOD(I,J)
226 CONTINUE
225 CONTINUE
230 CONTINUE
      REWIND 3
      IF (NSKL.NE.0) GOT0 147
      D0 119 I=1,4
      119 WRITE(3) (XLRTOT(I,J),J=1,NPR0B)
      M3=NJINK4-3
      D0 118 I=M3,NJINK4
      118 WRITE(3) (XLRTOT(I,J),J=1,NPR0B)
      M4=NJINK4-4
      D0 117 I=5,M4
      117 WRITE(3) (XLRTOT(I,J),J=1,NPR0B)
      REWIND 3
      GOT0 102
      147 D0 747 I=1,NJINK4
      READ(2) (SKLTR(J),J=1,N0J4)
      D0 748 J=1,NPR0B
      ST0RE(I,J)=0.0
      D0 748 K=1,N0J4
      748 ST0RE(I,J)=ST0RE(I,J)+SKLTR(K)*XLRTOT(K,J)
      747 CONTINUE
      D0 919 I=1,4
      919 WRITE(3) (ST0RE(I,J),J=1,NPR0B)
      M3=NJINK4-3
      D0 918 I=M3,NJINK4
      918 WRITE(3) (ST0RE(I,J),J=1,NPR0B)
      M4=NJINK4-4
      D0 917 I=5,M4
      917 WRITE(3) (ST0RE(I,J),J=1,NPR0B)
      REWIND 3
      1001 CONTINUE
      IF (NSKL.EQ.0) GOT0 102
      READ(2) ((SKL(I,J),J=1,NJINK4),I=1,N0J4)
      REWIND 2
      D0 750 I=1,NJINK4
      READ(12) (R0W(I),J=1,N0J4)
      D0 751 J=1,NJINK4
      REGT0T (J)=0.0
      D0 751 K=1,N0J4
      751 REGT0T (J)=REGT0T (J) + R0W(K)*SKL(K,J)
      750 WRITE(2) (REGT0T(J),J=1,NJINK4)
      C THE 780 LOOP REARRANGES AND PARTITIONS THE REGION STIFFNESS MATRIX
      102 NJINK = NJINK4/4
      REWIND 2
      D0 625 INK=1,8
      D0 626 JAK=1,8
      626 XK11(INK,JAK)=0.0
      D0 625 KIX=1,M8
      XK12(INK,KIX)=0.0
      XK21(KIX,INK)=0.0
      625 CONTINUE
      D0 627 KIX=1,M8
      D0 627 LAX=1,M8
      627 XK22(KIX,LAX)=0.0
      NREAD=0
      KOUNT=-8
      NJINK3=NJINK-1
      D0 780 N=1,NJINK
      NREAD=NREAD+1

```

```

KOUNT=KOUNT+4
DØ 781 I=1,4
781 IF(NREAD.LE.2.ØR.NREAD.GE.NJINK3)GØ TØ 790
KK=KOUNT+1
KK=KOUNT+12
DØ 785 L=KK,KKK
IRØW=4*(NREAD-2)
J=L-4
DØ 785 K=1,4
IRØW=IRØW+1
785 XK22(IRØW,J)=HØLD(K,L)
GØ TØ 780
790 IF(NREAD.EQ.1)GØ TØ 791
IF(NREAD.EQ.2)GØ TØ 792
IF(NREAD.EQ.NJINK3)GØ TØ 793
IF(NREAD.EQ.NJINK)GØ TØ 794
791 DØ 796 I=1,4
DØ 796 J=1,4
XK11(I,J)=HØLD(I,J)
JJ=J+4
796 XK12(I,J)=HØLD(I,JJ)
GØ TØ 780
792 DØ 797 I=1,4
DØ 797 J=1,4
XK21(I,J)=HØLD(I,J)
JJ=J+4
XK22(I,J)=HØLD(I,JJ)
JJJ=J+8
IF(INT.EQ.2) GØ TØ 795
XK22(I,JJ)=HØLD(I,JJJ)
GØ TØ 797
795 XK21(I,JJ)=HØLD(I,JJJ)
797 CONTINUE
GØ TØ 780
793 M1=NJINK4-11
M4=NJINK4-4
M8=NJINK4-8
KRØW=M8-4
DØ 798 I=1,4
KRØW=KRØW+1
KCØL=4
K8=M8-8
DØ 798 J=M11,M8
K8=K8+1
XK22(KRØW,K8)=HØLD(I,J)
JJ=J+4
KK=K8+4
XK22(KRØW,KK) =HØLD(I,JJ)
JJJ=J+8
KCØL=KCØL+1
798 XK21(KRØW,KCØL)=HØLD(I,JJJ)
GØ TØ 780
794 KEND=NJINK4-8
KRØW=4
M4=NJINK4-4
M7=NJINK4-7
DØ 799 I=1,4
KRØW=KRØW+1
K4=KEND-4
KCØL=4

```

```

903680
903690
903700
903710
903720
903730
903740
903750
903760
903770
903780
903790
903800
903810
903820
903830
903840
903850
903860
903870
903880
903890
903900
903910
903920
903930
903940
903950
903960
903970
903980
903990
904000
904010
904020
904030
904040
904050
904060
904070
904080
904090
904100
904110
904120
904130
904140
904150
904160
904170
904180
904190
904200
904210
904220
904230
904240
904250
904260
904270
904280

D0 799 J=M7,M4
K4=K4+1
XK12(KR0W,K4)=H0LD(I,J)
KC0L=KC0L+1
JJ=J+4
799 XK11(KR0W,KC0L)=H0LD(I,JJ)
780 CONTINUE
7703 NSING=NKIV*(NKIV+1)/2
N=NKIV
IK=1
D0 10 K=1,N
D0 10 I=K,N
XK22(I,K)=(XK22(I,K)+XK22(K,I))/2.
XKIV(IK)=XK22(I,K)
10 IK=IK+1
CALL SWITCH (XKIV,-NKIV)
CALL CHASE (XKIV,NKIV,XK21,8,112,NIX)
IF (NIX.LT.0) G0T0 8841
WRITE (10) ((XK21(I,J),J=1,8),I=1,M8)
WRITE (10) ((SAVJTC(I),SAVSTP(I)),I=1,NNT)
D0 81 J=1,8
D0 81 I=1,8
XK1221(I,J)=0.0
D0 81 K=1,NKIV
D0 81 K1221(I,J)=XK1221(I,J)+XK12(I,K)*XK21(K,J)
-81 D0 82 J=1,8
D0 82 I=1,8
D0 650 J=1,7
K=J+1
D0 650 I=K,8
XKR(I,J)=(XKR(I,J)+XKR(J,I))/2.0
650 XKR(J,I)=XKR(I,J)
WRITE (4) ((XKR(I,J),J=1,8),I=1,8)
IF (NH.NE.0.AND.IBEGIN.NE.1) G0 T0 691
WRITE(6,5011)
5011 FORMAT(///55X23HKEGION STIFFNESS MATRIX//14X8HDELTA 11X8HDELTA 2
11,7X,8HDELTA 11,7X,7HTHETA 1,8X,8HDELTA 12,7X,8HDELTA 22,7X,8HDELTA
2A,R2,7X,7HTHETA 2)
111=0
D0 687 M=1,8
111=111+1
111=111+1
111=111+1
WRITE(6,688) ((LABEL(I),I=11,111),(XKR(M,J),J=1,8)
688 FORMAT(1X,244,1X,81E14.7,1X))
687 CONTINUE
691 CONTINUE
D0 137 J=1,8
D0 137 I=1,8
137 SYM(I,J)=0.0
INDEC=0
D0 138 I=1,8
D0 138 J=1,8
IF(I.NE.1)G0 T0 138
IF(XKR(I,J)-GE.0.0)G0 T0 138
INDEC=1
138 SYM(I,J)=XKR(I,J)
IF(INDEC.EQ.0)G0 T0 151
IF (NH.NE.0) G0 T0 151
WRITE(6,152)
152 FORMAT(///- ***** WARNING - NEGATI

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```

IVES APPEAR ON MAIN DIAGONAL. REVISE SIZING *****-//
151 JJ=2
N = 8
J = 1
DO 42 I=1,7
M = JJ
DO 43 I=M,N
ALPH = ABS(SYM(I,J)) - ABS(SYM(J,I))
IF(ALPH) 47,71,48
47 IF(SYM(I,J).EQ.0.0) GOT0 71
SYM(I,J) = SYM(J,I) / SYM(I,J)
GOT0 43
48 IF(SYM(I,J).EQ.0.0) GOT0 71
SYM(I,J) = SYM(I,J) / SYM(J,I)
GOT0 43
71 SYM(I,J) = 1.0
43 SYM(J,I) = 0.0
JJ = JJ + 1
J = J + 1
42 CONTINUE
IF (NH,NE.0.AND.IBEGIN,NE.1) G0 T0 692
WRITE(6,157)
157 FORMAT(/56X,21HREGION SYMMETRY CHECK/)
DO 1730 I=1,8
WRITE(6,5000) (SYM(I,J),J=1,8)
1730 CONTINUE
692 CONTINUE
IF (NPR08.EQ.0) G0 T0 150
DO 819 I=1,4
819 READ(3) (XL1(I,J),J=1,NPR08)
DO 818 I=5,8
818 READ(3) (XL1(I,J),J=1,NPR08)
D = 0.0
M8 = NJINK4-8
DO 817 I=1,M8
817 READ(3) (XL2(I,J),J=1,NPR08)
CALL CHASE (XKIV,NKIV,XL2,-NPR08,I12,NIX)
IF (NIX.LT.0) GOT0 8842
WRITE (10) ((XL2(I,J),J=1,NPR08),I=1,M8 )
NL2=NPR08
DO 205 J=1,NPR08
DO 205 I=1,8
XK12L2(I,J)=0.0
DO 205 K=1,NKIV
DO 206 J=1,NPR08
DO 206 I=1,8
XLR(I,J)=XL1(I,J)-XK12L2(I,J)
WRITE(10) ((XLR(I,J),J=1,NPR08),I=1,8)
IF (NH,NE.0.AND.IBEGIN,NE.1) G0 T0 150
WRITE(6,5012)
5012 FORMAT(/57X,18HREGION LOAD MATRIX/)
DO 5512 I=1,8
5512 WRITE(6,5000) (XLR(I,J),J=1,NPR08)
GOT0 150
8841 TERR0R=8841
NERR0R=30
GOT0 150
8797 IERR0R = 8797
NERR0R=33
G0 T0 150

```

904900
904910
904920
904930
904940
904950
904960
904970
904980
904990
905000
905010
905020
905030
905040

```

8842 IERROR=8842
      NERROR=31
      GOT0 150
      1 READ (2) ((XKR(I,J),J=1,8),I=1,8)
      DO 651 J=1,7
      K = J+1
      DO 651 I=K,8
      XKR(I,J) = (XKR(I,J)+XKR(J,I))/2.0
651  XKR(J,I) = XKR(I,J)
      WRITE(4) ((XKR(I,J),J=1,8),I=1,8)
      IF (NPR08.EQ.0) GOT0 150
      READ(3) ((XLR(I,J),J=1,NPR08),I=1,8)
      WRITE(8) ((XLR(I,J),J=1,NPR08),I=1,8)
150  RETURN
      END

```

```

C ..... ROUTINE **DIO ** ABACUS UPDATED 07/07/72 .....
SUBROUTINE SWITCH(A,M)
DIMENSION A(1)
N = IABS(M)
IF (N - 2) 190,190,90
90 L = (N*(N+1)) / 2
KEY = 1
LOCK = N/2 + 1
IF (M) 100,190,160
100 IF (N - 3) 110,140,110
110 KKT = 3
NKF = N - 1
IMAGE = L
INT0 = L - 3
I = 3
D0 130 K = 2,LOCK
D0 120 IK = KKT,NKF
X = A(IK)
A(IK) = A(INT0)
A(INT0) = X
INT0 = INT0 - I
120 I = I + 1
KKT = NKF + K
NKF = NKF + N - K
IMAGE = IMAGE - K
INT0 = IMAGE
130 I = K
140 IF (KEY) 150,190,150
150 KEY = 0
160 L0V2 = L / 2
K = L - 2
D0 170 I = 3,L0V2
X = A(I)
A(I) = A(K)
A(K) = X
170 K = K - 1
IF (KEY) 180,190,180
180 KEY = 0
GO TO 100
190 RETURN
END

```

```

1100C00
1100010
1100020
1100030
1100C40
1100050
1100060
1100C70
1100080
1100090
1100100
1100110
1100120
1100130
1100140
1100150
1100160
1100170
1100180
1100190
1100200
1100210
1100220
1100230
1100240
1100250
1100260
1100270
1100280
1100290
1100300
1100310
1100320
1100330
1100340
1100350
1100360
1100370
1100380
1100390
1100400

```

```

C ..... ROUTINE **D11 ** ABACUS UPDATED 07/07/72 .....
SUBROUTINE CHASE(A,M0,Y,NO,MID,NIX)
REAL A(1),Y(1)
COMMON /WINTER/ INDIC8
COMMON /BOND/ M,L
COMMON /OPT2/ PRINT
9 FORMAT(12H1SOLUTION(S)/1H0)
10 FORMAT(15,1P8E15.7/(5X,8E15.7))
M=M0
INDIC8=0
N = IABS(INO)
IF (NO) 110,100,100
100 CALL FUTURE(A,M,NIX)
IF (NIX) 170,110,110
110 PRINT = 0.0
IF (PRINT .GT. 0.0) WRITE(6,9)
MK1 = 1
L = 1.
I1 = M
DO 160 K = 1,N
CALL TRIEQ(A,Y(MK1))
IF (PRINT .GT. 0.) WRITE (6,10) K,(Y(K1), K1 = MK1,I1)
I1 = I1 + MID
MK1 = MK1 + MID
160 CONTINUE
170 RETURN
END

```

```

1200000
1200010
1200020
1200030
1200040
1200050
1200060
1200070
1200080
1200090
1200100
1200110
1200120
1200130
1200140
1200150
1200160
1200170
1200180
1200190
1200200
1200210
1200220
1200230
1200240
1200250
1200260

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```

C ..... ROUTINE **012 ** ABACUS UPDATED 07/19/72 .....
SUBROUTINE FUTILE(A,N,NIX)
  DIMENSION A(1)
  DOUBLE PRECISION SUM
  EQUIVALENCE (SUM,SUM)
  K1 = 1
  KK = 0
  DO 210 K = 1,N
    KK = KK + K
    IK = KK
    KK1 = KK - 1
    IF (KK1) 60,50,60
  50 ASSIGN 100 TO LEAP
  60 ASSIGN 80 TO LEAP
  70 I1 = K1
  DO 140 I = K,N
    SUM = -A(IK)
    GO TO LEAP, (80,100)
  80 IJ = I1
  DO 90 KJ = K1,KK1
    SUM = SUM + A(IJ)*A(KJ)
  90 IJ = IJ + 1
  100 I1 = I1 + 1
  105 DENOM = -SUM
  IF (DENOM) 980,980,110
  110 DENOM = -SQRT(DENOM)
    A(IK) = -DENOM
    GO TO 130
  120 A(IK) = SUM / DENOM
  130 IK = IK + 1
  140 CONTINUE
    K1 = K1 + K
  210 CONTINUE
  NIX = 0
  220 RETURN
  980 NIX = -K
    GO TO 220
  END

```

```

1300000
1300010
1300020
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1300040
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1300090
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1300110
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1300130
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1300210
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1300360
1300370
1300380
1300390

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```

C ..... ROUTINE **013 ** ABACUS UPDATED 07/19/72 .....
SUBROUTINE TRIC8(A,Y)
  REAL A(1),Y(1)
  COMMON /WINTER/INDIC8
  COMMON /BOND/ M,L
  EQUIVALENCE (SUN,SUM)
  L1 = L
  MML = M - 1
  MML = M - L1
  IF (INDIC8) 130,100,100
100 Y(L1) = Y(L1) / A(L1)
  L1 = L1
  L1 = L1
  IF (MML) 105,125,105
105 DO 120 I = L1,MML
  L1 = L1 + 1
  SUM = -Y(I+1)
  L1 = L1
  DO 110 J = L1,I
  SUM = SUM + A(IJ)*Y(J)
110 LJ = LJ + 1
  L1 = LJ
120 Y(I+1) = -SUM / A(I1)
125 IF (INDIC8) 170,140,170
130 IF ( ( MML + 1 ) * ( M + L1 ) ) / 2
140 I = M
145 Y(I) = Y(I) / A(I1)
  L1 = I1 - 1
  I = I - 1
  IF (I - L1) 170,150,150
150 SUM = -Y(I+1)
  LJ = I1 + L1
  DO 160 J = L1,I
  Y(IJ) = Y(IJ) + SUM*A(IJ)
160 LJ = LJ + 1
  GO TO 145
170 RETURN
  END

```

```

1400000
1400010
1400020
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1400040
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1400070
1400080
1400090
1400100
1400110
1400120
1400130
1400140
1400150
1400160
1400170
1400180
1400190
1400200
1400210
1400220
1400230
1400240
1400250
1400260
1400270
1400280
1400290
1400300
1400310
1400320
1400330
1400340
1400350
1400360
1400370

```

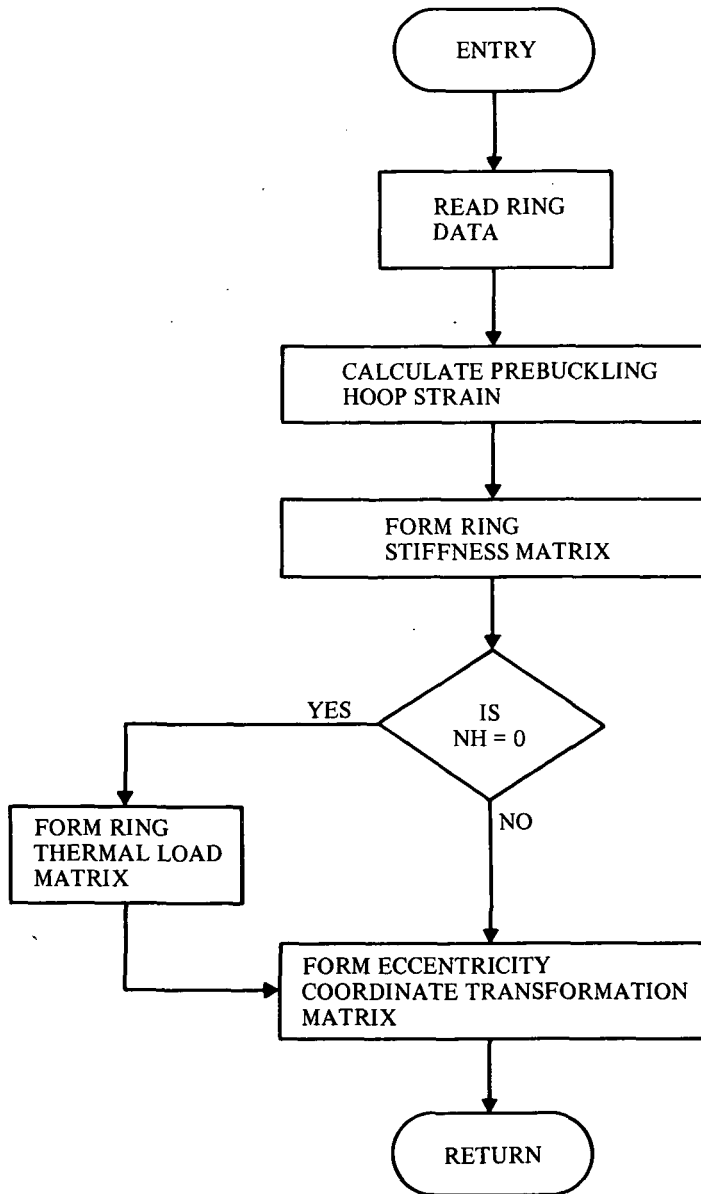
SUBROUTINE RINGER

This subroutine reads the discrete ring geometric data, and temperatures, and forms the ring stiffness and thermal load matrices. These matrices are passed back to either of subroutines REGMAT or STRMAT (see next) as necessary, for incorporation into the region or structure matrices, respectively. If the present pass is a nonlinear one, the effects of prebuckling hoop strain are considered, and the load calculations are omitted.

The calculations in RINGER account for the eccentricity of the ring centroid from the base shell wall, and the offset of the ring centroid from the shear center.

FORTRAN CODE	ENGINEERING SYMBOLS (REF. 1)
RNGTOT MATRIX	$\begin{bmatrix} k_R \end{bmatrix}$
TDEL MATRIX	$\begin{bmatrix} T_\Delta \end{bmatrix}$
RNGLOD MATRIX	$\begin{bmatrix} l_R \end{bmatrix}$
RC	r_c
RS	r_s
XC	x_c
YC	x_s

RINGER



```

C ..... ROUTINE ** RINGER ** ABACUS UPDATED 06/18/72 .....
SUBROUTINE RINGER (Q,XN,RNGT0T,RNGL0D,J,ADUS,BADUS,JTIC,JST0P,
1 JTN0,KBC,XNL,MELG,NSEG)
INTEGER Q,XN
COMMON /ARING/ RING(28),AMAT(30,4),IRLC(28)
DIMENSION RNGT0T(4,4),RNGL0D(4,28),TDEL(4,4),XKT0T(4,4),XNL(4)
DIMENSION ADUS(30),BADUS(30),JTIC(30),JST0P(30),JTN0(28),XNL(2)
X1 = XNL(1)
X2 = XNL(2)
IF (Q.EQ.1) G0 T0 212
READ(5,213) JTN0(J),EA,EIY,EIX,GJ,EIX,ALPR,RC,XC,YC,XBAR,YBAR,XI,
X0,TI,T0,TF,IRLC(J), R0J,ENTHJ,ENTHK
213 FORMAT(12,5E14.7/6E12.5/5E14.7,12/3E14.7)
AMN = (TI-T0)/(XI-X0)
RN = ((T0-TF)*XI-(TI-TF)*X0)/(XI-X0)
WRITE(1) JTN0(J),EA,EIY,EIX,GJ,EIX,ALPR,RC,XC,YC,XBAR,YBAR,
AMN,BN,IRLC(J), R0J,ENTHJ,ENTHK
1 WRITE(6,300) JTN0(J),EA,EIY,EIX,GJ,EIX,ALPR,RC,XC,YC,XBAR,YBAR,
XI,X0,TI,T0,TF, R0J
300 FORMAT(75X,-RING AT JOINT N0. -,12/- EA =-,1PE12.5,6X,-EIY =-,
1 1PE12.5,5X,-EIY =-,1PE12.5,4X,-GJ =-,1PE12.5,6X,-EIX =-,1PE12.5,
2 5X,-ALPR =-,1PE12.5/- RC =-,1PE12.5,6X,-XC =-,1PE12.5,6X,-YC =-,
3 1PE12.5,6X,-XBAR =-,1PE12.5,4X,-YBAR =-,1PE12.5,4X,-XI =-,
4 1PE12.5/- X0 =-,1PE12.5,6X,-TI =-,1PE12.5,6X,-T0 =-,1PE12.5,6X,
5 -TFREE =-,1PE12.5,3X, -RN =-,1PE12.5)
IF (KBC.NE.0) WRITE(6,301) ENTHJ,ENTHK
301 FORMAT(- NTHETA1 =-,1PE12.5,8X,- NTHETA2 =-,1PE12.5)
G0 T0 211
212 READ(1) JTN0(J),EA,EIY,EIX,GJ,EIX,ALPR,RC,XC,YC,XBAR,YBAR,
1 AMN,BN,IRLC(J), R0J,ENTHJ,ENTHK
211 CONTINUE
IF (KBC.EQ.0) G0 T0 100
EPSIL1=ENTHJ/EA
EPSIL2=ENTHK/EA
G0 T0 101
100 K = JTN0(J)
IF (MFLG.EQ.2) G0 T0 102
EPSIL1=AMAT(K,1)
EPSIL2=AMAT(K,2)
G0 T0 101
102 EPSIL1=AMAT(K,3)
EPSIL2=AMAT(K,4)
101 CONTINUE
RS = RC*XC
AM = XN
AM2 = AM*AM
AM4 = AM2*AM2
RCS = RC*RS
RC2 = RC*RC
RS2 = RS*RS
RCS3 = RCS*RS2
XC2 = XC*XC
YC2 = YC*YC
TW0PI = 2.0*3.1415927
EPSIL=(X1*EPSIL1+X2*EPSIL2)*RC/R0J
EAPS = EA*EPSIL
RNGT0T(1,1) = 1.0/RCS*(EA*(XC2*AM4/RS2-2.0*XC*AM2/RS+1.0)+
1 EIY/RC2*(AM4-2.0*AM2+1.0))
2 +EAPS*AM2*RC/RS3-EAPS*RC/RS3

```

```

RNGT0T(1,2,1) = 1.0/RCS*(EA*YC*AM2*(XC*AM2/RS2-1.0/RS)+E1Y*YC*AM2/
1 (RC2*RS)*(AM2-1.0)+E1XY*AM2/RCS*(AM2-1.0))
RNGT0T(1,3,1) = EA*AM/RS2*(-XC*AM2/RS+1.0)
RNGT0T(1,4,1) = 1.0/RCS*(EA*YC*(XC*AM2/RS-1.0)+E1Y*YC/RC2*
1 (AM2-1.0)+E1XY/RC*(AM2-1.0))
2 -EAPS*AM2*YC/RS2+EAPS*YC/RS2
RNGT0T(1,2) = RNGT0T(1,1)
RNGT0T(1,2,2) = AM4/RCS3*(EA*YC2+E1Y*YC2/RC2+E1X+2.0*E1XY*YC/RC)+
1 GJ*AM2/RS2*RS2)
2 +AM2/RCS*EAPS
RNGT0T(1,3,2) = -EA*YC*AM2*AM/(RS2*RS)
RNGT0T(1,4,2) = AM2/(RS2*RC)*(YC2*(EA+E1Y/RC2)+E1X+2.0*E1XY*YC/RC
1 +GJ*RC/RS)
2 +AM2/RCS*(EAPS*XC)
RNGT0T(1,3) = RNGT0T(1,1)
RNGT0T(1,2,3) = RNGT0T(1,3,2)
RNGT0T(1,3,3) = EA*AM2*RC/(RS2*RS)
RNGT0T(1,4,3) = -EA*YC*AM/RS2
RNGT0T(1,1,4) = RNGT0T(1,1)
RNGT0T(1,2,4) = RNGT0T(1,4,2)
RNGT0T(1,3,4) = RNGT0T(1,4,3)
RNGT0T(1,4,4) = 1.0/RCS*(YC2* EA+E1Y*YC/RC+E1X+2.0*E1XY*YC/RC)+
1 GJ*AM2/RS2
2 +1.0/RCS*EPSIL*(EA*(-YC2)+(E1Y+E1X)*AM2-E1X)
IF (Q.EQ.1) GO TO 400
TEM1 = EA*ALPR*(AMN*XC+BN)/RS
RNGLD(1,J) = TEM1
RNGLD(1,2,J) = 0.0
RNGLD(1,3,J) = 0.0
RNGLD(1,4,J) = -TEM1*YC-E1XY*ALPR*AMN/RS
400 CONTINUE
XBRS = 1.0-XBAR/RS
TDEL(1,1) = 0.0
TDEL(2,1) = 0.0
TDEL(3,1) = -1.0/XBRS
TDEL(4,1) = 0.0
TDEL(1,2) = 0.0
TDEL(2,2) = -1.0
TDEL(3,2) = -AM*YBAR/(RS*XBRS)
TDEL(4,2) = 0.0
TDEL(1,3) = -1.0
TDEL(2,3) = 0.0
TDEL(3,3) = -AM*XBAR/(RS*XBRS)
TDEL(4,3) = 0.0
TDEL(1,4) = -YBAR
TDEL(2,4) = +XBAR
TDEL(3,4) = 0.0
TDEL(4,4) = -1.0
D0 813 L=1,4
D0 813 M=1,4
XKT0T(L,M) = 0.0
D0 813 N=1,4
813 XKT0T(L,M) = XKT0T(L,M)+RNGT0T(L,N)*TDEL(N,M)
D0 814 L=1,4
D0 814 M=1,4
RNGT0T(L,M) = 0.0
D0 814 N=1,4
814 RNGT0T(L,M) = RNGT0T(L,M)+TDEL(N,L)*XKT0T(N,M)
IF (Q.EQ.1) GO TO 401
D0 815 L=1,4
XL(L) = 0.0

```

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3300590
3300600
3300620
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3300650
3300660
3300670
3300680
3300690
3300700
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3300780
3300800
3300820
3300830
3300840
330085
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3300870
3300880
3300890
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3300910
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3300980
3300990
3301000
3301010
3301020
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3301080
3301090
3301100
3301110
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3301150
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3301170
3301180
3301190
3301200
3301210
3301220
3301230
3301240

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```

00 815 N=L,4
815 XL(L) = XL(L)+TDEL(N,L)*RNGLED(N,J)
00 816 L=L,4
816 RNGLED(L,J) = XL(L)
401 CONTINUE
00 1100 L=L,NSEC
IF (JTH2(J).EQ.JTIC(L)) GO TO 1105
1100 CONTINUE
00 10 1107
1105 R = JTIC(L)
RMULT = ADUS(M)*TW0PI
00 10 1111
1107 00 1101 L=L,NSEC
IF (JTH2(J).EQ.JSTEP(L)) GO TO 1106
1101 CONTINUE
1106 M = JSTEP(L)
RMULT = RADUS(M)*TW0PI
1111 CONTINUE
00 920 L=L,4
00 820 M=M,4
820 RNOT0(L,M) = RNGT0(L,M)*RMULT
IF (Q.EQ.1) GO TO 402
00 821 L=L,4
821 RNGLED(L,J) = RNGLED(L,J)*RMULT
402 RETURN
END

```

```

3301250
3301260
3301270
3301280
3301290
3301300
3301310
3301320
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3301340
3301350
3301360
3301370
3301380
3301390
3301400
3301410
3301420
3301430
3301440
3301450
3301460
3301470
3301480
3301490
3301500

```

SUBROUTINE STRMAT

The region stiffness matrices, XKR, and the region load matrices, XLR, are passed from REGMAT to STRMAT via Tape #4 and Tape #8, and are placed in the XKSTOT array and the XLSTOT array, respectively. A matrix, BCD, is formed to represent the boundary conditions, and, if kinematic links occur between regions, the RKL matrix is developed to represent this situation. The subroutine RINGER is again called for discrete ring matrices. In passes other than the first pass, first cycle, the load calculations are not performed.

As a result of appropriate matrix operations, a reduced structure stiffness matrix is formed. In passes other than the first pass, first cycle, STRMAT terminates here. In the first pass, first cycle, the following calculations are made. Subroutine FLEX, a routine identical to SREVN2 (except for being in single precision) with the name changed due to the structure of the OVERLAY option, is called to invert the structure stiffness matrix thus producing A, the flexibility matrix for the structure. The region end deflection array, DRE, is produced as the result of another set of matrix operations.

FORTTRAN CODE

ENGINEERING SYMBOLS (REF. 1)

BCD MATRIX

$[BC]$

BCT MATRIX

$[BC]^T$

XST MATRIX

$\hat{[K]}_T$

XKF MATRIX

$\hat{[K]}_F$

A MATRIX

$\hat{[A]}_F$

XSL MATRIX

$\hat{[L]}_T$

XLS ARRAY

$\hat{\{L\}}_F$

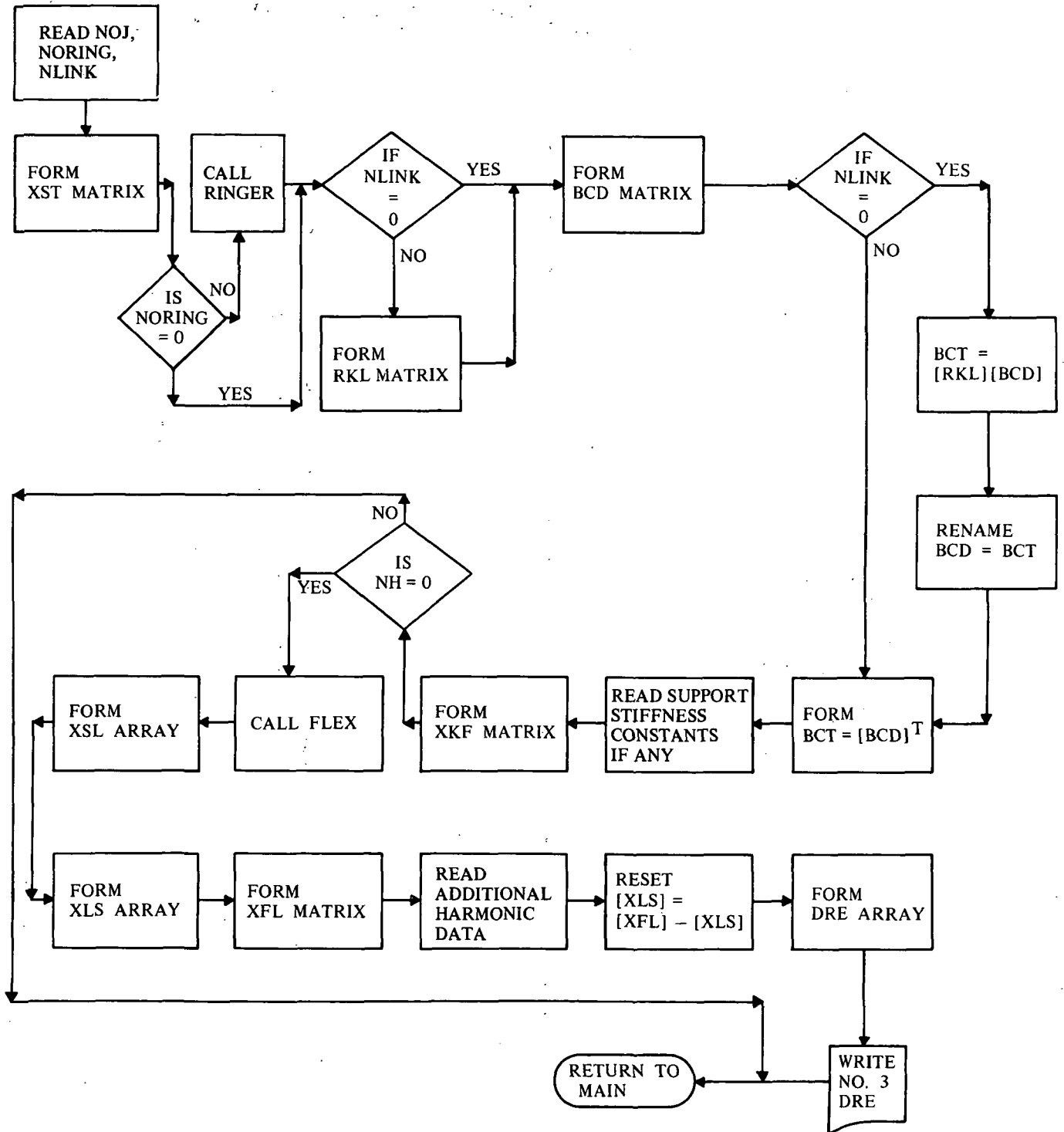
XFL ARRAY

$\hat{\{F\}}_F$

DRE ARRAY

$\{\Delta\}_T$

STRMAT



```

C..... ROUTINE *DI4 / ** ABACUS UPDATED 07/19/72 .....
SUBROUTINE STRMAT
  INTEGER SAVJTC, SAVSTP, Q, THICK
  INTEGER XN1, XN
  DOUBLE PRECISION SAVTIC, TIC, PHI, ST0P, REST0P, RTICK
  COMMON ST0RY(16), XMAT(110,10), STD(10), SADUS(30), RADUS(30)
  COMMON XN, TEFREE, TIC, PHI, ST0P, REST0P, RTICK, G1, XNL(2), NH
  COMMON NST(30), NKL(30), NXMAT(20), SAVJTC(30), SAVSTP(30), JRTIC(30)
  COMMON JRST0P(30), NREG, NPMPT, NRC, NSC, NIX, TERR0R, KGE0M, IGE0M, ISTTAB
  COMMON KELVIN, IBEGLN, NPR0B, NSEG, NERR0R, Q, THICK, N0JS, NLINKS, NLCASE
  COMMON NTSKL, NZ, NBCT, LINPUT, NTRKL, NPASS, XNL, KBC, NRINGS
  COMMON /ARING/ NRING(28), AMAT(30,4), IRLC(28)
  DIMENSION SCLA(128), L0C(128)
  DIMENSION IC0L(10)
  DIMENSION RKL(120,120), 0PEN(4,4)
  DIMENSION DLP(4), BCD(124,124), TEMP(124), BCT(124), XKF(128), BC(128)
  DIMENSION A(124,124), XSL(124,2), XFL(124,2), DRE(128,2), BCA(128)
  DIMENSION XKR(8,8), XSTR(128), XLS(128,2), XLR(8,2)
  DIMENSION XST(124,124), XSTBC(124,124), TEMP1(124)
  DIMENSION RNGT0T(4,4), RNL0D(4,28), JTN0(28)
  DIMENSION C0LTTL(2)
  EQUIVALENCE (XST(1),BCD(1),A(1),XSTBC(1),RKL(1),XLS(1))
  EQUIVALENCE (XSTR(1),XKF(1),XFL(1),XSL(1),DRE(1),SCLA(1),
    1 TEMP(1),0PEN(1))
  EQUIVALENCE (XKR(1),XLR(1),BC(1),BCT(1),BCA(1),TEMP1(1),L0C(1))
  DATA C0LTTL/4H C0,4HLUMN/
  REMIND 2
  REMIND 3
  REMIND 4
  REMIND 8
  REMIND 9
  REMIND 14
  REMIND 15
  1 FORMAT(1H,8(E14.7,2X)/(3X,8(E14.7,2X)))
  101 FORMAT(3I5,16A4)
  1726 WRITE(6,1726)
  1726 IF (NPR0B.EQ.0.AND.NH.NE.0) G0 T0 1700
  READ(5,101) N0J,N0RING,NLINK
  N0JS = N0J
  NLINKS = NLINK
  NRINGS = NRING
  G0 T0 1701
  1700 N0J = N0JS
  NLINK = NLINKS
  NRING = NRINGS
  1701 CONTINUE
  NH4=4
  NH8=8
  NJTNH4=N0J*NH4
  D0 102 J=1,NJTNH4
  D0 102 I=1,NJTNH4
  102 XST(I,J)=0.0
  D0 100 NR=1,NREG
  READ(4)((XKR(I,J),J=1,8),I=1,8)
  J1=JRTIC(NR)
  J2=JRST0P(NR)
  I1=4*(J1-1)
  450 JJ=4*(J2-1)+1

```

```

11=I+1
D0 460 JK=1,4
G0 T0 (451,452,453,454),JK
451 IX=I
IND=II
D0 461 I=1,4
D0 461 J=1,4
461 OPEN(I,J)=XKR(I,J)
452 IX=II
IND=JJ
D0 462 I=1,4
D0 462 J=1,4
462 OPEN(I,J)=XKR(I,J+4)
453 IX=JJ
IND=II
D0 463 I=1,4
D0 463 J=1,4
463 OPEN(I,J)=XKR(I+4,J)
G0 T0 455
454 IX=JJ
IND=JJ
D0 464 I=1,4
D0 464 J=1,4
464 OPEN(I,J)=XKR(I+4,J+4)
455 D0 456 I=1,4
JX=IND
D0 457 J=1,4
XST(IX,JX)=XST(IX,JX)+OPEN(I,J)
457 JX=JX+1
456 IX=IX+1
460 CONTINUE
100 CONTINUE
IF (NBRING.EQ.0) G0 T0 1170
MFLG = 2
D0 1211 J=1,NBRING
CALL RINGER (Q,XN,RNGT0T,RNGL0D,J,SADUS,UADUS,JRTIC,JRST0P,JTN0,
1 KBC,XNL,MFLG,NREG)
JT = 4*(JTN0(J)-1)
D0 1220 I=1,4
D0 1220 IK=1,4
1220 XST(JT+I,JT+IK) = XST(JT+I,JT+IK)+RNGT0T(I,IK)
1211 CONTINUE
IF (Q.NE.5) G0 T0 1170
WRITE(6,300)
300 FORMAT(///)
READ(5,2000)
2000 FORMAT(IX)
1170 CONTINUE
D0 107 I=1,NJTNH4
107 WRITE (2) (XST(I,J),J=1,NJTNH4)
REWIND 2
REWIND 4
IF (NH.NE.0) G0 T0 3108
C GENERATION 0F BC BOUNDARY CONDITION SCRAMBLING MATRIX
WRITE(6,347) N0J,NLINK
347 FORMAT(///51X30HINPUT DATA FOR REGION COUPLING///31X24HNUMBER 0F
1 REGION JOINTS ,13,14X26HNUMBER 0F KINEMATIC LINKS ,13///44X6HREGI0
2N11X8HJ0INT(11)11X8HJ0INT(11)///)
D0 348 I=1,NREG
1500620
1500630
1500640
1500650
1500660
1500670
1500680
1500690
1500700
1500710
1500720
1500730
1500740
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1500800
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1500980
1500990
1501000
1501010
1501020
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1501040
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1501060
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1501080
1501090
1501100
1501110
1501120
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1501160
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1501180
1501190
1501200
1501220

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1501230
1501240
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1501360
1501370
1501380
1501390
1501400
1501410
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1501500
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1501580
1501590
1501600
1501610
1501620
1501630
1501640
1501650
1501660
1501670
1501680
1501690
1501700
1501710
1501720
1501730
1501740
1501750
1501760
1501770
1501780
1501790
1501800
1501810
1501820
1501830

KTIC=JRTIC(I)
KSTOP=JRSTOP(I)
WRITE(6,349) I,KTIC,KSTOP
349 FORMAT(40X,I2,2(10X,I3))
348 CONTINUE
IF(NLINK.EQ.0) GO TO 3108
DO 756 I=1,NJTNH4
DO 756 J=1,NJTNH4
756 RKL(I,J)=0.0
DO 757 I=1,NJTNH4
757 RKL(I,I)=1.0
DO 789 I=1,4
DO 789 J=1,4
789 OPEN(I,J)=0.0
OPEN(2,2)=1.0
OPEN(3,3)=1.0
OPEN(4,4)=1.0
WRITE(6,1824)
1824 FORMAT(/760X,12HREGION LINKS//43X,8HJOINT(J),5X,8HJOINT(I),
15X,20HANGLE OF ORIENTATION)
DO 502 NRIG=1,NLINK
READ(5,503) JD,JI,COTAN
503 FORMAT(212,E14,7)
1828 WRITE(6,1828) JD,JI,COTAN
1828 FORMAT(40X,I2,11X,I2,11X,E14,7)
COTAN = COS(COTAN)/SIN(COTAN)
OPEN(1,1) = SADUS(JD) / SADUS(JI)
OPEN(2,4) = - (SADUS(JD)-SADUS(JI))
OPEN(3,4) = - OPEN(2,4)* COTAN
IXX= JD*4-3
DO 504 I=1,4
DO 504 J=1,4
JXX= JI*4-3
DO 505 J=1,4
RKL(IXX,JXX)=OPEN(I,J)
505 JXX=JXX+1
504 IXX=IXX+1
502 CONTINUE
READ(5,2000)
NTRKL = 15
DO 781 I=1,NJTNH4
781 WRITE(15) (RKL(I,J),J=1,NJTNH4)
3108 KEND 15
IF (LINPUT.EQ.0) GO TO 3200
DO 108 J=1,NJTNH4
DO 108 I=1,NJTNH4
108 RCD(I,J)=0.0
ICR = 1
WRITE(6,2372)
2372 FORMAT(////57X19HBOUNDARY CONDITIONS//30XSHJOINTSX7HDELTA T,5X,7
1HDELTA 2,5X,7HDELTA R,5X,7H THETA ,7X,11HANGLE ALPHA)
DO 109 J=1,NØJ
109 J=J+1
READ (5,110) JN,DLP(1),DLP(2),DLP(3),DLP(4),ANGLE
110 FORMAT (12,4F2.0,E14,1)
I1 = DLP(1)
I2 = DLP(2)
I3 = DLP(3)
I4 = DLP(4)
WRITE(6,2373) JN,I1,I2,I3,I4,ANGLE
2373 FORMAT(/31X,I3,9X,I2,10X,I2,10X,I2,7X,E14,7)
I1 = (4*JN)-3

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D0 121 I=1,4
IF(OLP(I)-1,0) 113,114,115
115 IF(OLP(I)-2,0) 116,116,117
114 BCD(I,I,ICR)=1,0
G0 T0 118
116 BCD(I,I,ICR)=SIN(ANGLE)
BCD(I+1,I,ICR)= -COS(ANGLE)
G0 T0 118
117 BCD(I+1,I,ICR)=COS(ANGLE)
BCD(I,I,ICR)=SIN(ANGLE)
118 ICR=ICR+1
113 I=I+1
121 CONTINUE
109 CONTINUE
READ(5,2000)
ICR=ICR-1
NZ=ICR
IF(NLINK.EQ.0) G0 T0 3124
D0 783 N=1,NJTNH4
READ(NTRKL) (TEMP(M),M=1,NJTNH4)
D0 782 J=1,NZ
BCD(J)=0,0
D0 782 I=1,NJTNH4
782 BCT(J)=BCT(J)+TEMP(I)*BCD(I,J)
783 WRITE (4) (BCT(L),L=1, NZ)
REWIN NTRKL
REWIN 4
D0 126 M=1,NJTNH4
126 READ(4) (BCD(M,N),N=1,NZ)
C AT THIS POINT THE BCD ARRAY IS THE PRODUCT OF RKL AND BCD ARRAYS
3124 CONTINUE
NBCT = 3
D0 124 J=1,NZ
124 WRITE (3) (BCD(I,J),I=1,NJTNH4)
D0 125 I=1,NJTNH4
125 WRITE (3) (BCD(I,J),J=1,NZ)
REWIN 3
WRITE(14) ((BCD(I,J),J=1,NZ),I=1,NJTNH4)
D0 3300 J=1,NZ
3300 WRITE(14) (BCD(I,J),I=1,NJTNH4)
REWIN 4
G0 T0 3201
3200 READ(14) ((BCD(I,J),J=1,NZ),I=1,NJTNH4)
3201 CONTINUE
READ (2) (XSTR(J),J=1,NJTNH4)
D0 184 M=1,NZ
TEMP(M) = 0,0
D0 181 N=1,NJTNH4
181 TEMP(M) = TEMP(M)+XSTR(N)*BCD(N,M)
184 CONTINUE
184 WRITE(14) (TEMP(I),I=1,NZ)
180 CONTINUE
REWIN 4
D0 183 I=1,NJTNH4
183 READ (4) (XSTBC(I,J),J=1,NZ)
REWIN 4
D0 182 N=1,NZ
READ(NBCT) (BCT(J),J=1,NJTNH4)
D0 185 M=1,NZ
XKF(N)=0,0

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D0 186 K=1,NJTNH4
186 XKF(M)=XKF(M)+BCI(K)*XSTBCI(K,M)
185 CONTINUE
WRITE (4) (XKF(I),I=1,NZ)
IF (NLCASE.NE.1-0R.XN1.NE.0-0.0R.NH.NE.0) G0 T0 188
WRITE(11) (XKF(I),I=1,NZ)
G0 T0 182
188 CONTINUE
IF (NLCASE.EQ.1.AND.XN.EQ.0-0) G0 T0 182
IF (I(XN.EQ.XN1.AND.NPASS.EQ.2)-0R.(NH.NE.0.AND.NPASS.EQ.1))
1 WRITE(11) (XKF(I),I=1,NZ)
182 CONTINUE
NBCT = 14
KEMIND 2
REWIND 4
D0 187 I=1,NZ
187 READ(4) (A(I,J),J=1,NZ)
IF (IBEGIN.EQ.0) G0 T0 1750
WRITE(6,1726)
2365 FORMAT(50X,29H THE REDUCED STIFFNESS MATRIX/)
NUMBER = 2
JJ = 0
JJJ = 0
1725 JJ = JJJ + 1
JJJ = JJJ + 8
MM = 8
IF (JJJ.GT.NZ) MM=8-(JJJ-NZ)
MMH = JJ
IF(JJJ.GT.NZ) JJJ=NZ
D0 1721 M=1,MM
IC0L(M)=MMH
1721 MMH = MMH + 1
NUMBER = NUMBER + 3
WRITE(6,1729) ((C0LITL,IC0L(M)),M=1,MM)
1729 FORMAT(/10H R0W ,8(2A4,1X,13,3X)/)
D0 1722 I=1,NZ
NUMBER = NUMBER + 1
WRITE(6,1728) I,(A(I,J),J=JJ,JJJ)
1728 FORMAT(3X,13,4X,8(E14.7,1X))
IF(NUMBER.LT.55) G0 T0 1722
NUMBER = 3
WRITE(6,1726)
WRITE(6,1729) ((C0LITL,IC0L(M)),M=1,MM)
1722 CONTINUE
IF(JJJ.NE.NZ) G0 T0 1725
1750 CONTINUE
IF (NH.NE.0-0R.KBC.NE.0) G0 T0 7
DDC = 0-0
R0R = 0-0
CALL FLEX (A,NZ,SCLA,124,NIX)
IF (NIX.NE.0) G0 T0 8777
D0 804 L=1,NJTNH4
READ(3) (BC(I),I=1,NZ)
D0 716 M=1,NZ
TEMP(M) = 0-0
D0 805 N=1,NZ
805 TEMP(M) = TEMP(M) + BC(N)*A(N,M)
716 CONTINUE
WRITE (2) (TEMP(I),I=1,NZ)
804 CONTINUE

```

```

REWIND 2
REWIND 3
DØ 991 J=1,NPRØB
DØ 991 I=1,NJTNH4
991 XSL(I,J) = 0.0
1001 DØ 777 NR=1,NREG
J1 = JRTIC(NR)
J2 = JRSTØP(NR)
READ(8) ((XLR(I,J),J=1,NPRØB),I=1,NH8)
DØ 777 N2 = 1,2
GØTØ (I1,I2),N2
11 I1 = (J1-I1)*NH4+1
I1I = I1+NH4-1
GØTØ 3
12 I1 = (J2-I1)*4+1
I1I = I1+NH4-1
3 DØ 777 J=1,NPRØB
I=0
IF(N2.EQ.2) I=NH4
DØ 777 IL=I1,I1I
I=I+1
777 XSL(IL,J) = XSL(IL,J)+XLR(I1,J)
IF (NØRTING.EQ.0) GØ TØ 1150
DØ 1225 J=1,NØRING
JT = 4*(JTNØ(J)-1)
DØ 1226 I=1,4
DØ 1226 IK=1,NPRØB
IF (IK.EQ.1.AND.IRLC(J).EQ.2) GØ TØ 1226
XSL(JT+I,IK) = XSL(JT+I,IK)+RNGLDØ(I,J)
1226 CØNTINUE
1225 CØNTINUE
1150 CØNTINUE
DØ 876 N=1,NZ
READ(3) (BCT(J),J=1,NJTNH4)
DØ 717 M=1,NPRØB
XLS(N,M) = 0.0
DØ 806 K=1,NJTNH4
806 XLS(N,M) = XLS(N,M) + BCT(K)*XSL(K,M)
717 CØNTINUE
876 CØNTINUE
REWIND 3
DØ 301 J=1,NPRØB
DØ 301 I=1,NZ
301 XFL(I,J) = 0.0
READ(5,302) LINLØD,(STØRY(I),I=1,16)
302 FØRMAT(I14,16A4)
IF(LINLØD.EQ.0) GØ TØ 303
WRITE(6,341)
341 FØRMAT(I1H1//57X,19HEXTERNAL LINE LØADS///36X,14HPRØBLEM NUMBER,7X
120HPØINT ØF APPLICATION,7X,12HAPPLIED LØAD//)
DØ 304 N=1,LINLØD
READ(5,305) JEXT2,JEXT1,XFL(JEXT1,JEXT2)
305 FØRMAT(I215,E14.7)
WRITE(6,342) JEXT2,JEXT1,XFL(JEXT1,JEXT2)
342 FØRMAT(I41X,13,22X,13,15X,E14.7)
304 CØNTINUE
303 CØNTINUE
READ(5,2000)
DØ 811 J=1,NPRØB
DØ 811 I=1,NZ
XLS(I,J)=XFL(I,J)-XLS(I,J)

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      IF (J.EQ.2) XLS(I,J)=XLS(I,I)+XFL(I,I)
811 CONTINUE
      REWIND 3
      DO 812 J=1,NJTMH4
      READ (2) (BCA(K),K=1,NZ)
      DO 813 M=1,NPR0B
      DRE(J,M)=0.0
      DO 813 N=1,NZ
      813 DRE(J,M)=DRE(J,M)+BCA(N)*XLS(N,M)
812 CONTINUE
      WRITE(6,1726)
      WRITE(6,2368)
2368 FORMAT(31X,70THE EXPANDED REGION JOINT DISPLACEMENT MATRIX (REGIO
IN END DEFLECTIONS))
      WRITE(6,1770)
1770 FORMAT(/,14X,5HJ0INT,14X,7HPR0BLEM,13X,7HDELTA T,13X,7HDELTA Z,13X
1,7HDELTA R,11X,11H0MEGA-THETA)
      NUMBER = 4
      KK=-3
      DO 1735 J=1,N0J
      NUMBER = NUMBER + NPR0B + 1
      IF (NUMBER.LT.56) GO TO 1745
      WRITE(6,1726)
      WRITE(6,1770)
      NUMBER=2+NPR0B+3
1745 KK=KK+4
      KKK=KK+3
      WRITE(6,1739)
1739 FORMAT(1H )
      DO 1764 L=1,NPR0B
      WRITE(6,1765) J,L,(DRE(K,L),K=KK,KKK)
1765 FORMAT(15X,12,18X,12,9X,4(3X,E14.7,3X))
1764 CONTINUE
1735 CONTINUE
      DO 71 NR=1,NREG
      DO 71 K=1,2
      II=(JRTIC(NR) - 1) *4 +1
      IF (K.EQ.2) II= JRST0P(NR)*4-3
      III= II + 3
      DO 71 I = II,III
      71 WRITE(3) (DRE(I,J),J=1,NPR0B)
      REWIND 2
      REWIND 3
      REWIND 4
      GO TO 7
8777 HERR0R =8777
      HERR0R=32
      NIX=1
      7 CONTINUE
      RETURN
      END
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C ..... ROUTINE **D15 ** ABACUS UPDATED 07/19/72 .....
C SUBROUTINE FLEX (A,M,L0C,MID,NIX)
C
C MATRIX INVERSION
C
C A-CONVENTIONAL FORTRAN DOUBLE ARRAY CONTAINING MATRIX TO BE INVERTED
C M- MATRIX ORDER
C L0C- SINGLE ARRAY DIMENSIONED AT LEAST TO M
C MID- FIRST DIMENSION OF A, NOT LESS THAN M
C NIX- ERROR INDICATOR, SET TO ZERO AFTER SUCCESSFUL EXECUTION.
C
      DIMENSION A(MID,1)
      INTEGER L0C(1)
      100 N = M
      DO 190 K = 1,N
        PIVOT = 0.0
        DO 120 I = K,N
          IF (PIVOT - ABS(A(I,K))) 110,110,120
        110 PIVOT = ABS(A(I,K))
        L = I
      120 CONTINUE
      IF (PIVOT) 140,130,140
      130 NIX = -1
      GO TO 210
      140 L0C(K) = L
      DO 150 J = 1,N
        TEMP1 = A(K,J)
        A(K,J) = A(L,J)
        150 A(L,J) = TEMP1
        TEMP1 = A(K,K)
        A(K,K) = 1.0
        DO 160 J = 1,N
          A(K,J) = A(K,J)/TEMP1
        DO 190 I = 1,N
          IF (I - K) 170,190,170
        170 TEMP1 = -A(I,K)
          A(I,K) = 0.0
          DO 180 J = 1,N
            A(I,J) = A(I,J) + TEMP1*A(K,J)
        190 CONTINUE
        DO 200 K = 1,N
          NK = N - K
          L = L0C(NK+1)
          DO 200 I = 1,N
            TEMP1 = A(I,NK+1)
            A(I,NK+1) = A(I,L)
        200 A(I,L) = TEMP1
        NIX = 0
      210 RETURN
      END

```

SUBROUTINE INITIAL

As a result of the matrix operations performed in REGMAT, the SKI22, the XK2221, and the XK22L2 arrays for each region are passed to INITIAL. The XK1112 and XL1 arrays for each segment, resulting from the matrix procedures in SEGMAT, are also passed to INITIAL. The region end deflection matrices, DRE, which were formed in STRMAT or BCVECT are transmitted to INITIAL.

Following appropriate matrix operations upon these arrays, the force initial conditions, the FICS array, and the deflections initial conditions, the DICS array, are produced. These arrays combine to form the YICS matrix, which contains the true initial conditions for the structure to be analyzed.

The pertinent counters in the subroutine are:

NS = segment counter

NR = region counter

FORTRAN CODE

ENGINEERING SYMBOLS (REF. 1)

XK2221 MATRIX

$$\begin{bmatrix} \hat{K}_{22} \end{bmatrix}^{-1} \quad \begin{bmatrix} \hat{K}_{21} \end{bmatrix}$$

XK22L2 MATRIX

$$\begin{bmatrix} \hat{K}_{22} \end{bmatrix}^{-1} \quad \begin{bmatrix} \hat{L} \end{bmatrix}$$

DSE ARRAY

$$\{\Delta\}$$

XK1112 MATRIX

$$\begin{bmatrix} k_{ii} & | & k_{ij} \end{bmatrix}$$

ROTD MATRIX

$$[IDT]^T$$

DICS ARRAY

$$\{\delta(i)\}$$

XL1 ARRAY

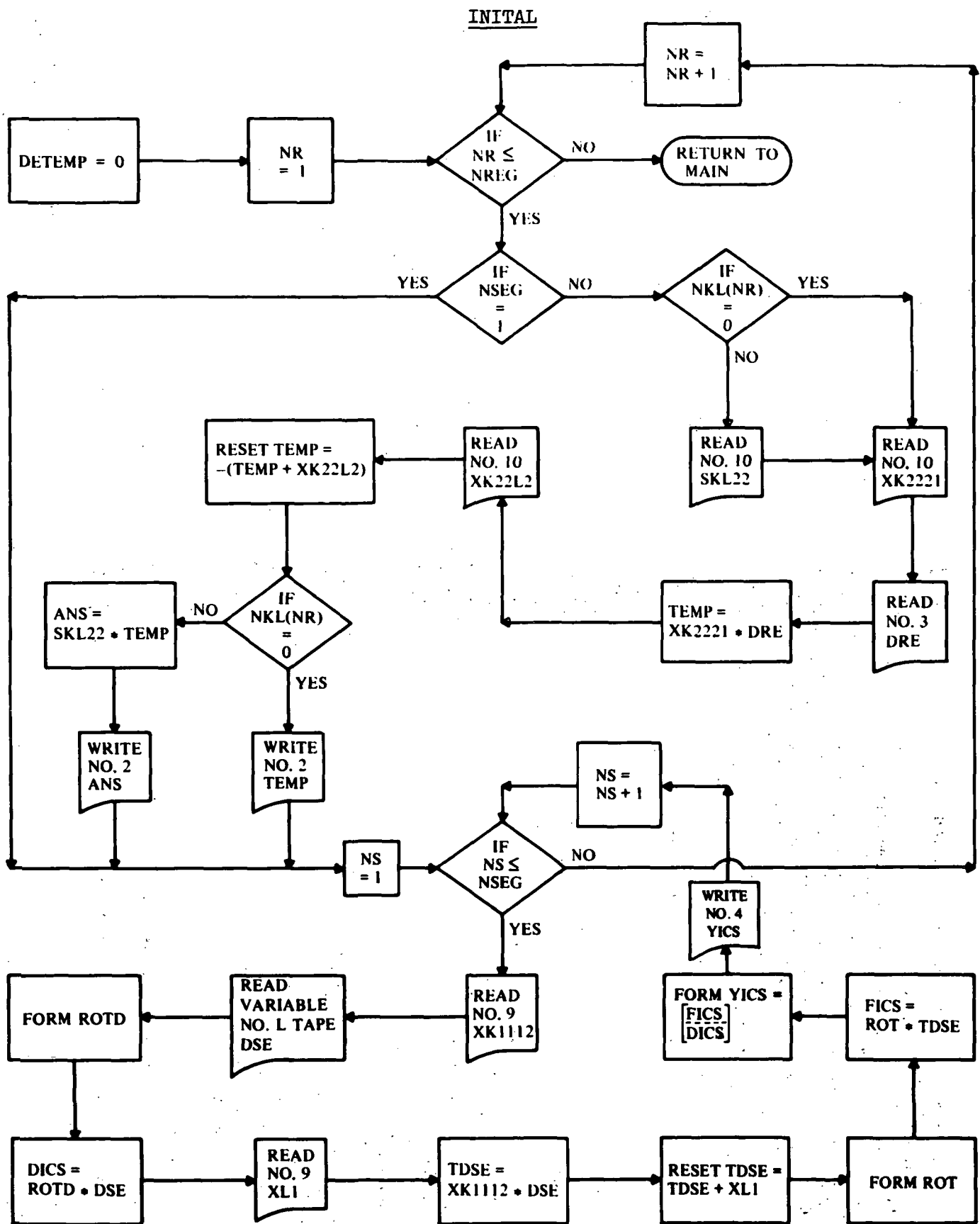
$$\{\ell(i)\}$$

ROT MATRIX

$$[IFT]^T$$

FICS ARRAY

$$\{f(i)\}$$



```

C ..... ROUTINE **D16      ** ABACUS UPDATED 07/24/72 .....
SUBROUTINE INITIAL
INTEGER SAVJTC, SAVSTP, Q, THICK
INTEGER XN1, XN
DOUBLE PRECISION SAVTIC, TIC, PHI, ST0P, REST0P, RTICK
COMMON TADUS(16), XMAT(110,10), STD(10), SADUS(30), RADUS(30)
COMMON XN, TEFREE, TIC, PHI, ST0P, REST0P, RTICK, G1, XNL(2), NH
COMMON NST(30), NKL(30), NXMAT(20), SAVJTC(30), SAVSTP(30), JRTIC(30)
COMMON JRST0P(30), NREG, NMPT, NRC, NSC, NIX, IERR0R, KGE0M, IGE0M, ISTTAB
COMMON KELVIN, IBEGIN, NPR0B, NSEG, NERR0R, Q, THICK, N0JS, NLINKS, NLCASE
COMMON NTSKL, NZ, NBCT, LINPUT, NTRKL, NPASS, XN1, KBC, NRINGS
DIMENSION XK222(112,8), DRE(8,2), TEMP(112,2), XK22L2(112,2)
DIMENSION XK112(4,8), DSE(8,2), R0TD(4,4), DTCS(4,2)
DIMENSION T0SE(8,2), YICS(8,2)
DIMENSION XLI(4,2), R0T(4,4), FICS(4,2), SKL22(112,112), ANS(112,2)
EQUIVALENCE (R0T(1),R0TD(1)), (TIC,TICK)
EQUIVALENCE (DSE(1),DRE(1)), (XK222(1),XK22L2(1))
EQUIVALENCE (SKL22(1),XK112(1)), (YICS(1),T0SE(1))
NH4 = 4
NH41 = NH4 + 1
NH8 = 8
NH81 = NH8 + 1
REWIND 2
REWIND 3
REWIND 4
REWIND 8
REWIND 9
REWIND 10
1 FORMAT(1H,8(E14.7,2X)/(3X,8(E14.7,2X)))
G0 100 NK=1,NREG
N0J = NST(NR) + NKL(NR) + 1
ISKL22 = 4*(N0J-2)
JSKL22 = 4*(N0J-2-NKL(NR))
NJTNH4=N0J*NH4
M8=4*(N0J-NKL(NR))-8
NSEG=NST(NR)
IF (NSEG.EQ.1) G0T0 703
IF (NKL(NR).EQ.0) G0T0 415
D0 425 I=1,JSKL22
425 READ(10) (SKL22(I,J),J=1,JSKL22)
415 READ(10) ((XK222(I,J),J=1,NH8),I=1,M8)
READ(10) (SAVJTC(1),SAVSTP(1),I=1,NSEG)
703 D0 91 K = 1,2
11 = 1
IF (K.EQ.2) 11=5
111 = 11+3
D0 91 I=1,111
91 READ(3) (DRE(I,J),J=1,NPR0B)
IF (NSEG.EQ.1) G0T0 999
D0 101 J=1,NPR0B
D0 101 I=1,M8
TEMP(I,J)=0.0
D0 101 K=1,NH8
TEMP(I,J)=TEMP(I,J)+XK222(I,K)*DRE(K,J)
101 CONTINUE
IF (NH.NE.0) G0T0 510
READ(10) ((XK22L2(I,J),J=1,NPR0B),I=1,M8)
G0T0 511
510 D0 512 I=1,M8

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DØ 512 J=1,NPRØB
512 XK22L2(I,J)=0.0
511 CONTINUE
DØ 102 J=1,NPRØB
DØ 102 I=1,M8
102 TEMP(I,J)=-(TEMP(I,J))+XK22L2(I,J)
IF(NKL(NR).EQ.0) GØ TØ 435
DØ 445 I = 1,ISKL22
DØ 445 J=1,NPRØB
ANS(I,J)=0.0
DØ 445 K = 1,JSKL22
445 ANS(I,J)=ANS(I,J)+SKL22(I,K)*TEMP(K,J)
435 DØ 391 N=1,NSEG
IF(N.EQ.1.ØR.N.EQ.NSEG).AND.SAVJTC(N).GT.SAVSTP(N)) GØ TØ 370
DØ 398 K=1,2
IF (N.NE.1.ØR.K.NE.1) GØTØ 393
DØ 394 I= 1,4
394 WRITE (2) (DRE(I,J),J=1,NPRØB)
GØ TØ 398
393 IF(N.EQ.NSEG.AND.K.EQ.2) GØTØ 395
IF (K.EQ.1) II = SAVJTC(N)*4-7
IF (K.EQ.2) II = SAVSTP(N)*4-7
III = II + 3
DØ 397 I=1,III
IF (NKL(NR).EQ.0) GØTØ 392
WRITE (2) (ANS(I,J),J=1,NPRØB)
GØTØ 397
392 WRITE (2) (TEMP(I,J),J=1,NPRØB)
397 CONTINUE
GØ TØ 398
395 DØ 396 I=5,8
396 WRITE (2) (DRE(I,J),J=1,NPRØB)
398 CONTINUE
GØ TØ 391
370 IF(N.EQ.NSEG) GØ TØ 380
IF(NKL(NR).EQ.0) GØ TØ 375
DØ 371 I=1,4
371 WRITE(2) (ANS(I,J),J=1,NPRØB)
GØ TØ 376
375 DØ 372 I=1,4
372 WRITE(2) (TEMP(I,J),J=1,NPRØB)
376 DØ 373 I=1,4
373 WRITE(2) (DRE(I,J),J=1,NPRØB)
GØ TØ 391
380 II =M8 -3
III = M8
DØ 381 I=5,8
381 WRITE(2) (DRE(I,J),J=1,NPRØB)
IF(NKL(NR).EQ.0) GØ TØ 385
DØ 382 I=1,III
382 WRITE(2) (ANS(I,J),J=1,NPRØB)
GØ TØ 391
385 DØ 383 I=1,III
383 WRITE(2) (TEMP(I,J),J=1,NPRØB)
391 CONTINUE
REWIND 2
999 DØ 201 NS=1,NSEG
READ (9) ((XK1112(I,J),J=1,NH8),I=1,NH4),IGEØM,G1
ISEG=0
NRI=NR-1
IF(NR1.EQ.0)IGØTØ8
1700620
1700630
1700640
1700650
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1700680
1700690
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1700990
1701000
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1701180
1701190
1701200

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D0 7 I=1,NR1
7 ISEG=ISEG+NST(I)
8 ISEG=ISEG+NS
TIC= SAVTIC(ISEG)
G0 T0 (21,22,23),IGE0M
21 SN = DSIN(TIC)
CS = DC0S(TIC)
G0 T0 25
22 SN = C0S(I1.570796-G1)
CS = SIN(I1.570796-G1)
G0 T0 25
23 SN = 1.0
CS = 0.0
25 CONTINUE
IF (INSEG.EQ.1) G0 T0 80
D0 78 I = 1,8
78 READ (2) (DSE(I,J),J=1,NPR08)
80 CONTINUE
D0 302 J=1,NH4
D0 302 I=1,NH4
302 R0TD(I,J)=0.0
D0 305 J=1,NH4,4
R0TD(I,J)=1.0
R0TD(J+1,J+2)=CS
R0TD(J+2,J+1)=-CS
R0TD(J+1,J+1)=-SN
R0TD(J+2,J+2)=-SN
305 R0TD(J+3,J+3)=1.0
D0 306 J=1,NPR08
D0 306 I=1,NH4
DICS(I,J)=0.0
D0 306 K=1,NH4
306 DICS(I,J)=DICS(I,J)+R0TD(I,K)*DSE(K,J)
D0 350 J=1,NPR08
D0 350 I=1,NH4
350 XL1(I,J) = 0.0
IF (NH.EQ.0) READ(9) ((XL1(I,J),J=1,NPR08),I=1,NH4)
D0 202 J=1,NPR08
D0 202 I=1,NH4
TDSE(I,J)=0.0
D0 202 K=1,NH8
202 TDSE(I,J)=TDSE(I,J)+XL112(I,K)*DSE(K,J)
D0 203 J=1,NPR08
D0 203 I=1,NH4
203 TDSE(I,J)=TDSE(I,J)+XL1(I,J)
D0 301 J=1,NH4
D0 301 I=1,NH4
301 R0TD(I,J)=0.0
D0 204 J=1,NH4,4
R0T(J,J)=-1.0
R0T(J+1,J+2)=-CS
R0T(J+2,J+1)=CS
R0T(J+1,J+1)=SN
R0T(J+2,J+2)=SN
204 R0T(J+3,J+3)=1.0
D0 205 J=1,NPR08
D0 205 I=1,NH4
FICS(I,J)=0.0
D0 205 K=1,NH4
205 FICS(I,J)=R0T(I,K)*TDSE(K,J)+FICS(I,J)
D0 402 J=1,NPR08

```

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1701210
1701220
1701230
1701240
1701250
1701260
1701270
1701280
1701290
1701300
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1701360
1701370
1701380
1701390
1701400
1701410
1701420
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1701500
1701510
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1701600
1701610
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1701800
1701810

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DO 402 I=1,NH4
  II=I+NH4
  YICS(I,J)=FICS(I,J)
402 YICS(II,J)=OICS(I,J)
201 WRITE(4) ((YICS(I,J),I=1,8),J=1,NPR08)
  REWIND 2
100 CONTINUE
  REWIND 1
  REWIND 4
  REWIND 8
  RETURN
  END

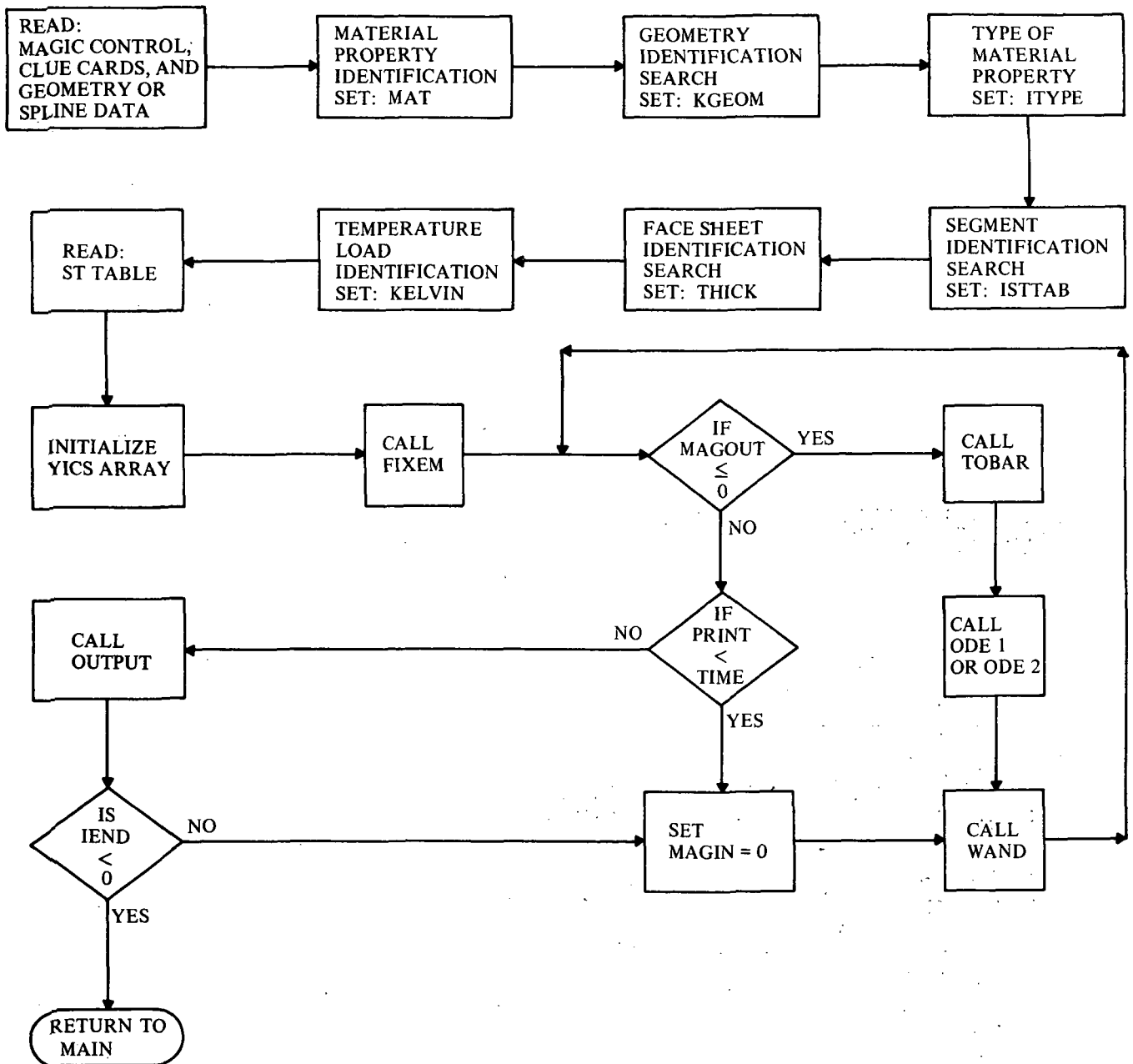
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SUBROUTINE LEBEGE

The subroutine link LEBEGE receives the YICS array for each segment from INITIAL via Tape #4. The subroutine FIXEM is called to integrate the differential equations of each segment, under true load conditions. FIXEM is identical to subroutine SETUP, while WAND corresponds to subroutine MAGIC and only consideration of the OVERLAY structure dictates the change in names. The subroutines TOBAR, TEMOEG, PLYCO, and PLYNE are similarly equivalent to ROBOT, GEOMET, PLICO, and PLINE discussed previously.

The results of the final integration sequence are the forces and deflections at the beginning, intermediate, and end points of each segment. In the first pass, first cycle, the prestress and predeformation states are printed from this routine. In other passes the U, V, W eigenvectors are printed, providing convergence has been reached.

LEBEGE



```

C ..... ROUTINE **D17 ** ABACUS UPDATED 07/24/72 .....
SUBROUTINE LEBEGE
  INTEGER XN
  DOUBLE PRECISION SAVTIC, TIC, PHI, STØP, RESTØP, RTICK
  DOUBLE PRECISION DTAU, DIFF, STEP, DELTA, TIME, DTIME
  DOUBLE PRECISION YNEW, YPREO
  COMMON STØRY(16), XMAT(110,10), STD(110), SADUS(30), RADUS(30)
  COMMON TADUS(30), UADUS(30), SAVTIC(900)
  COMMON XN, TEFREE, TIC, PHI, STØP, RESTØP, RTICK, G1, XNL(2), NH
  COMMON NST(30), NKL(30), NXMAT(20), SAVJTC(30), SAVSTP(30), JRTIC(30)
  COMMON JRSTØP(30), NREG, NMPT, NRC, NSC, NIX, IERRØR, KGEØM, IGEØM, ISTTAB
  COMMON KELVIN, IBEØIN, NPROB, NSEG, NERRØR, Q, THICK, MØJS, NLINKS, NLCASE
  COMMON NTKL, NZ, NBCT, LINPUT, NTRKL, NPASS, XN1, KBC, NRINGS
  COMMON /NAME/ FACE(4), STRGØ(7), THERM(4), MATER(3), SEGTab(12)
  COMMON /ARING/ NRING(28)
  COMMON /SNILPS/ ANG, PSI(100), RAD(100), CUR1(100), CUR2(100),
1    DR1DP(100), Z1(14), R1(14), NRZIN
  COMMON /MAGIO/ KNT
  COMMON /LASTEQ/ YPREDI(16), YDØT(16), YASAVE(16),
2    YANTH, YAMTH, YAMPT, YANPT, YØPH, YØPH, YØTH, YAJPH,
3    S, SN, CS, SNSQ, CSSQ, TAN, SEC, CN, X1CS, X1SN, TN,
4    X1Ø, X1ØSQ, X1SNØ, X1CSØ, X1SNØ, X1Ø, CS1Ø,
5    RØSQ, XNSQ, BETA, R1, R2, S1, R1DØT, R1SQ,
6    XNTH, XNTPH, XMTTH, XMTPH, XFTHLD, XFPHLD, XFZELD,
7    XNTHLD, XMPHLD, ETHET(2), EPHI(2), XGPT(2), ALPHTH(2), ALPHPH(2),
8    XNUTP, XNUPT, XC11, XC22, XC15, XD33, XD22, XD21, XD12,
9    XN11, XN12, XK21, XK22, XK33, XD11,
A    M, L, SITIN, SITØT, SIPIN, SIPØT, TPTIN, TPTØT,
B    ZBRIN, ZBRØUT, SCRIPI, SCRIPI, SIFIN, SIFØT, TZEPI, TZETH
C    , XNPHI, BETTA, ZETTA, SAVY(8), XC16
  DIMENSION TPAV(5), RWØ(8)
  DIMENSION LST(13), YDEV(16), YICS(16), YNEW(16)
  DIMENSION XKF(128), TØDEL(16), FWDØL(16), YCØRR(16)
  DIMENSION ST(72,31), XLAYER(10)
  DIMENSION XSAVY(3,2)
  EQUIVALENCE (XMTTH, XMTETH), (XMTPH, XMTPEPH), (XNTH, XNTEPH),
1    (XNTPH, XNTEPH)
  EQUIVALENCE (XNPHI, XNPI)
  EQUIVALENCE (YNEW(1), XKF(1))
  EQUIVALENCE (XSAVY(1,1), SAVY(1))
  REWIND 1
600 FØRMAT(1H, 8(E14.7,2X)/(3X,8(E14.7,2X)))
  KSC = 0
  JAM = 1
  JNSC = 0
  DØ 451 I=1, NREG
451 KSC = KSC + NST(I)
902 LSC = 0
  LSC = LSC + 1
  XNTH = 0.0
  XNTPH = 0.0
  XMTTH = 0.0
  XMTPH = 0.0
  NSC = LSC
  JNSC = JNSC + 1
  IF (JNSC - LE, NST(JAM)) GØ TØ 1727
  NRNG = NRING(JAM)
  IF (NRNG - EQ, 0) GØ TØ 1900

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1800210
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1800650
1800660
1800670

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DØ 1901 I=1,NRNG
1901 READ(1) DUMLNK
1900 CONTINUE
  NNSKL = NKL(JAM)
  IF (NNSKL.EQ.0) GØ TØ 1724
  DØ 1725 I=1,NNSKL
1725 READ(1) DUMLNK
1724 CONTINUE
  JAM=JAM+1
  JNSC=1
1727 CONTINUE
  READ(1) RGØ,ANG,STØRY
  READ(1) DTAU,DIFF,STEP,DELTA
  IF (RGØ.EQ.14.0) GØ TØ 182
  READ(1)
    G1,G2,G3
  GØ TØ 183
182 READ(1) NRZIN,(Z(I),I=1,NRZIN)
183 CONTINUE
  READ(1) TYPE,HLAYR,SHEET,INTERP,RANKIN,TEFREE,NP
  DIFF =1.0E-04
  EPSIL =1.0E-05
  ERR = 1.0 E-07
  I = RGØ
  WRITE(6,1726)
1726 FORMAT(1H1)
  IF(JNSC.EQ.1) WRITE(6,606) JAM,NST(JAM),NKL(JAM)
606 FORMAT(/'58X,13HREGION NUMBER,13/35X,10HTHERE ARE ,12,14H SEGMENT
  1S AND ,12,35H KINEMATIC LINKS WITHIN THIS REGION)
  WRITE(6,651) JNSC,I ,(STØRY(I),I=1,16)
651 FORMAT(/'13X,15HSEGMENT NUMBER ,12,5X,13HSEGMENT CØDE ,12,5X,
  116A4)
C MATERIAL PRØPØRTY IDENTIFICATION
  DØ 501 I=1,NMPT
  IF (HLAYR-STD(I)) 501,502,501
502 MAT=I
  GØTØ 503
501 CONTINUE
  GØTØ 8036
503 CONTINUE
C GEØMETRY IDENTIFICATION SEARCH
  DØ 504 I=1,7
  IF(RGØ-STRGØ(I)) 504,505,504
504 CONTINUE
  GØTØ 8086
505 KGEØM=I
  IGEØM = 0
  IF (KGEØM.EQ.1.ØR.KGEØM.EQ.2.ØR.KGEØM.EQ.5.ØR.KGEØM.EQ.6) IGEØM =1
  IF (KGEØM.EQ.3) IGEØM=2
  IF (KGEØM.EQ.4) IGEØM=3
  IF ( KGEØM.EQ.7 ) IGEØM = 1
  DØ 506 I=1,3
  IF(TYPE-WATER(I))506,507,506
506 CONTINUE
  GØTØ 8087
507 ITYPE=I
  DØ 510 I=1,12
  IF(INTERP-SEGTAB(I))510,511,510
510 CONTINUE
  GØ TØ 8088
511 ISTTAB=I
  DØ 508 I=1,4

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1800680
1800690
1800700

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1801210
1801220
1801230


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72 CONTINUE
  IF (LST(JT).EQ.0) GO TO 660
  KZ = K + LST(JT) - 1
  K = KZ + 1
660 CONTINUE
  71 K = K + L - LST(JT)
  IF (NLC.EQ.1.AND.LST(1).EQ.0) NRW = K - 1
  JJ=JJJ+1
  JJ=JJ+5
17 MM=MM+1
590 CONTINUE
  READ(1) IS,SAVJTC(15),SAVSTP(15),STORY
  NSAVE = NRW
  JJ=NLCASE*6
  LT=0
  DO 15 J=1,JJ
15 LT=LT+LST(J)
  NTOTAL=LT+NSAVE
  NEQNS=8*NPR08
  TIC = ST(1,1)
  ST0P = ST(1,NP)
  READ(4) (YICS(I),I=1,NEQNS)
  NCYC=0
  NSAVE=NR0W
  IEND=0
  PRINT=TIC
  DTA=DTAU
  DTAU=0.0
  IF (NH.EQ.0) WRITE(6,656)
656 FORMAT(//5X,-PHI OR S,-13X,-NTHETA,-11X,-NPHI,-11X,-OMEGATH-)
  IF (NH.EQ.0.AND.NLCASE.EQ.2) WRITE(6,657)
657 FORMAT(11H,80X,-NTHETA,-11X,-NPHI,-11X,-OMEGATH-)
  IF (NH.NE.0) WRITE(6,671)
671 FORMAT(//27X,-V E C T Ø R 1-37X,-V E C T Ø R 2-
  1//3X,-PHI ØR S,-10X,-U,-14X,-V,-14X,-W,-9X,-ØMEGA THETA-8X,
  2-U,-14X,-V,-14X,-W,-9X,-ØMEGA THETA-/)
  IF (NH.EQ.0) WRITE(6,661)
661 FORMAT(11X)
  IF (NH.NE.0.AND.KBC.EQ.0) READ(13) SAVY
59 CALL FIXEM (MAGIN,MAG0UT,TIC,STEP,NEQNS,DTAU,EPSIL,DELTA,ERR,TIME,
  1 DTIME,YICS,YPRD,YCØRR,YDØT,YNEW,YDEV,FNDEL,TBDEL)
  GO TO 61
60 CALL WANDIMAGIN,MAG0UT,TIC,STEP,NEQNS,DTAU,EPSIL,DELTA,ERR,TIME,
  1 DTIME,YICS,YPRD,YCØRR,YDØT,YNEW,YDEV,FNDEL,TBDEL)
61 IF(MAG0UT.LE.0) GO TO 25
  IF (NH.EQ.0.AND.KBC.EQ.0) WRITE(13) SAVY
  IF(TIME.GT.STØP) GO TO 62
  IF(TIME.LT.STØP) GO TO 63
64 IEND=-1
  GO TO 67
62 IF(TIME.LE.(STØP+DIFF)) GO TO 64
  GO TO 8001
63 IF((STØP-DIFF).LE.TIME) GO TO 64
  IF((TIME+DTIME).GT.STØP) GO TO 65
  IF(PRINT.GT.TIME) GO TO 66
  PRINT=TIME+DTA
67 IF (NH.EQ.0) WRITE(6,1333) TIME,((IXSAVY(J1,K1),J1=1,3),K1=1,NLCASE)
1333 FORMAT(11X,1PE16.7,2(5X,1P3E16.7))
  IF (NH.NE.0) WRITE(6,1334) TIME,RMØ
1334 FORMAT(11X,1PE13.7,2(1X,1P3E15.7,1PE13.51)
6X50 IF(IEND.GT.0) GO TO 8002

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IF(IEND.LT.0).GOTO 150
66 MAGIN=0
GOTO 60
65 OTIME=STOP-TIME
DELTA=0.0
GOTO 67
75 NCYC=NCYC+1
MAGIN=-1
GOTO 60
25 PHI=TIME
ARG=PHI
IF (NH.NE.0.AND.KKNT.EQ.4.AND.KBC.EQ.0) READ(13) SAVY
LL=NP+1
DO 51 I=1,NP
IF(ARG-ST(1,I)) 52,55,51
52 IF(I-1) 55,55,54
51 CONTINUE
I=NP
GOTO 55
54 DO 57 IK=2,NTOTAL
57 ST(IK,LL)=ST(IK,I-1)+(ST(IK,I)-ST(IK,I-1))*(ARG-ST(1,I-1))/(ST(1,I)-ST(1,I-1))
GOTO 80
55 DO 58 IK=2,NTOTAL
58 ST(IK,LL)=ST(IK,I)
80 CONTINUE
C THE UPDATED INTERPOLATED VALUES OF THE MATERIAL PROPERTY COEFFIC
C IENTS ARE FOUND IN THE XMAT TABLE AND STORED IN THE XLAYER ARRAY
L=(MAT-1)*2+1
II=NXMAT(L)
III=NXMAT(L+1)
LL=NP+1
L=NR0W + 1
IF(KELVIN.NE.1)GOTO 81
IF(THICK.NE.1)GOTO 83
81 L00P=1
IL0W=1
HIGH = 1
IF(KELVIN.NE.1)GOTO 85
82 CONTINUE
TMPAV(IL0W)=(ST(L,LL)+ ST(L+1,LL)+ ST(L+2,LL) + ST(L+3,LL))/4.0
GOTO 85
83 L00P = 2
IL0W = 1
HIGH = 2
TMPAV(IL0W)= (ST(L,LL)+ ST(L+1,LL))/2.0
TMPAV(HIGH)=(ST(L+2,LL) + ST(L+3,LL))/2.0
M=1
GOTO (91,92,93,93),KELVIN
91 ARG= TMPAV(IL)
GOTO 94
93 CONTINUE
ARG= ST(NR0W+1,LL)
TMPAV(1) = ARG
94 DO 104 I = 2,10
IF (ARG-XMAT(II,I)) 121,123,104
121 IF (I-2) 8007,8007,124
104 CONTINUE
GOTO 8067
123 L=II+1
1802450
1802460
1802470
1802480
1802490
1802500
1802510
1802520
1802530
1802540
1802550
1802560
1802611
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107 L00P= 3
   IL0W = 3
   IHIGH= 3
   G0 T0 82
108 IF(ITYPE.EQ.3.AND. ISTAB .GE. 3)G0 T0 109
   G0 T0 118
109 L00P= 4
   IL0W = 4
   IHIGH = 4
   CPH = ST(3,LL)
   IF(ISTAB.GE. 10.AND. ISTTAB.LE. 12)CPH = ST(6,LL)
   IF(CPH .LE.0)G0 T0 284
   TPAV(4) = ST(L,LL)
   G0 T0 85
284 TPAV(4) =ST(L+3,LL)
   G0 T0 85
281 L00P=5
   IL0W=5
   IHIGH=5
   CTH = ST(3,LL)
   IF(ISTAB .GE. 10 .AND. ISTTAB .LE. 12)CTH = ST(7,LL)
   IF(CTH .LE. 0)G0 T0 116
   TPAV(5) = ST(L,LL)
   G0 T0 85
116 TPAV(5) = ST(L+3,LL)
   G0 T0 85
117 CONTINUE
   ETHET(2) = ETHET(1)
   ALPHH(2)=ALPHH(1)
   ALPHH(2)=ALPHH(1)
   XGPT(2) = XGPT(1)
   EPHI(2) = EPHI(1)
118 CONTINUE
   CALL T0BAR (ST,KLUE2,NROW,NRW,LL,ER,ES,EL,E2,HI,H0,T,TII,T00,TIK,
   1 T0K,DEGRES,G2,G3,TIME)
   IF (INIX.NE.0) G0 T0 9999
   LL=NP+1
   IF(XK11.EQ.0.0) G0T0 8101
   IF(ITYPE.EQ.3.AND.XK12.EQ.0.0) G0 T0 8102
   IF(ITYPE.EQ.3.AND.XK21.EQ.0.0) G0 T0 8103
   IF(XK22.EQ.0.0) G0T0 8104
   IF(XK33.EQ.0.0) G0T0 8105
   IF(XD11.EQ.0.0) G0T0 8106
   IF(ITYPE.EQ.3.AND.XD12.EQ.0.0) G0 T0 8107
   IF(ITYPE.EQ.3.AND.XD21.EQ.0.0) G0 T0 8108
   IF(XD22.EQ.0.0) G0T0 8109
   IF(XD33.EQ.0.0) G0T0 8110
   NL=0
   NLCSE=NLCASE
   IF(NH.EQ.0) NLCSE=1
   XFPHL1=0.0
   XFZEL1=0.0
   XFPHL2=0.0
   XFZEL2=0.0
   XNPH1 = 0.0
   JF = NPR08
   K = NK0W
   D0 7 N=1,JF
   I = (N-1)*8 + 1
   IF(KBC.NE.0) G0 T0 255
   IF(NH.EQ.0) G0 T0 350

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1803670
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1803910
1803920
1803930
1803940
1803950
1803960
1803970
1803980
1803990
1804000
1804080
1804090
1804020
1804030
1804040
1804050
1804060
1804070
1804080
1804090
1804100
1804110
1804120
1804130
1804140

1804150
1804160
1804170
1804180
1804190

```

K=NRØW
NL=0
350 DØ 250 JKL=1,NLCSE
NL=NL+1
XFTHLD=0.0
XFPHLD=0.0
XFZELD=0.0
XMTHLD=0.0
XMPHLD=0.0
IR=NL*6-5
IF (LST(IR),NE.0) K=K+LST(IR)
IF (LST(IR+1),EQ.0) GØTØ 44
K=K+1
XFTHLD=ST(K,LL)
44 IF (LST(IR+2),EQ.0) GØTØ 45
K=K+1
XFPHLD=ST(K,LL)
45 IF (LST(IR+3),EQ.0) GØTØ 46
K=K+1
XFZELD=ST(K,LL)
46 IF (LST(IR+4),EQ.0) GØTØ 47
K=K+1
XMTHLD=ST(K,LL)
47 IF (LST(IR+5),EQ.0) GØTØ 48
K=K+1
XMPHLD=ST(K,LL)
48 CØNTINUE
IF (JKL,EQ.2) GØ TØ 251
XFPHL1=XFPHLD
XFZEL1=XFZELD
251 XFPHL2=XFPHLD
XFZEL2=XFZELD
250 CØNTINUE
255 CØNTINUE
IF (1STTAB,GE.3.AND.1STTAB.LE.9) GØ TØ 4002
CALL ØDE1(XFPHL1,XFZEL1,XFPHL2,XFZEL2)
GØ TØ 77
77 IF (NH,NE.0) GØ TØ 8
NN = (M-1)*3+1
SAVY(NN) = YANTH
SAVY(NN+1) = YPRED(I+1)
SAVY(NN+2) = YPRED(I+7)
GØ TØ (177,178,179),IGEØM
177 SAVY(M+6) = XIRØ*(XN*YPRED(I+4)+YPRED(I+5)*CS-YPRED(I+6)*SN)
GØ TØ 7
178 SAVY(M+6) = (1.0/(S*CS))*(XN*YPRED(I+4)+CS*YPRED(I+5)-SN*
1 YPRED(I+6))
GØ TØ 7
179 SAVY(M+6) = XIRØ*(XN*YPRED(I+4)-YPRED(I+6))
GØ TØ 7
8 N=1
IF (M,EQ.2) N=5
RWØ(N)=YPRED(I+4)
RWØ(N+1)=YPRED(I+5)
RWØ(N+2)=YPRED(I+6)
RWØ(N+3)=YPRED(I+7)
7 CØNTINUE
GØTØ 75
8001 IERRØR=8001
NERRØR = 11

```

1804200
1804210
1804220
1804230
1804240
1804250
1804270
1804280
1804290
1804300
1804310
1804320
1804330
1804340
1804350
1804360
1804370
1804380
1804390
1804400
1804410
1804420
1804430
1804440

1804450
1804470
1804490
1804500
1804510
1804520
1804530

1804540

1804590
1804600
1804610
1804620

8002 GØTØ 8888
 IERRØR=8002
 NERRØR = 12
 GØTØ 8888
 8007 IERRØR=8007
 NERRØR = 15
 GØTØ 8888
 8008 IERRØR = 8008
 NERRØR = 10
 GØTØ 8888
 8031 IERRØR=8031
 NERRØR = 9
 GØTØ 8888
 8036 IERRØR=8036
 NERRØR = 2
 GØTØ 8888
 8086 IERRØR=8086
 NERRØR = 3
 GØTØ 8888
 8087 IERRØR=8087
 NERRØR = 4
 GØTØ 8888
 8088 IERRØR=8088
 NERRØR = 27
 GØTØ 8888
 8089 IERRØR=8089
 NERRØR = 5
 GØTØ 8888
 8090 IERRØR=8090
 NERRØR = 6
 GØTØ 8888
 8067 IERRØR= 8067
 NERRØR = 16
 GØTØ 8888
 8101 IERRØR = 8101
 NERRØR = 17
 GØTØ 8888
 8102 IERRØR = 8102
 NERRØR = 18
 GØTØ 8888
 8103 IERRØR = 8103
 NERRØR = 19
 GØTØ 8888
 8104 IERRØR = 8104
 NERRØR = 20
 GØTØ 8888
 8105 IERRØR = 8105
 NERRØR = 21
 GØTØ 8888
 8106 IERRØR = 8106
 NERRØR = 22
 GØTØ 8888
 8107 IERRØR = 8107
 NERRØR = 23
 GØTØ 8888
 8108 IERRØR = 8108
 NERRØR = 24
 GØTØ 8888
 8109 IERRØR = 8109
 NERRØR = 25
 GØTØ 8888

1804630
 1804640
 1804650
 1804660
 1804670
 1804680
 1804690
 1804700
 1804710
 1804720
 1804730
 1804740
 1804750
 1804760
 1804770
 1804780
 1804790
 1804800
 1804810
 1804820
 1804830
 1804840
 1804850
 1804860
 1804870
 1804880
 1804890
 1804900
 1804910
 1804920
 1804930
 1804940
 1804950
 1804960
 1804970
 1804980
 1804990
 1805000
 1805010
 1805020
 1805030
 1805040
 1805050
 1805060
 1805070
 1805080
 1805090
 1805100
 1805110
 1805120
 1805130
 1805140
 1805150
 1805160
 1805170
 1805180
 1805190
 1805200
 1805210
 1805220
 1805230

8110 ERROR = 8110
NERRR = 26
8888 NIX=1
GO TO 9999
150 IF (LSC.LI.KSC) GO TO 902
9999 RETURN
END

1805240
1805250
1805260
1805270
1805280
1805340
1805350

```

C ..... ROUTINE **018 ** ABACUS UPDATED 07/07/72 .....
SUBROUTINE FIXEM (MAGIN,MAGOUT,TIC,STEP,NEQNS,DTAU,
1 EPSIL,DELTA,ERR,TIME,DTIME,YICS,YPRD,
2 YCRRR,YDGT,YNEW,YDEV,FWDEL,TBDEL)
C RUNGE KUTTA MAGIC (REVISED) SINGLE PRECISION
DIMENSION YICS(1),YPRD(1),YCRRR(1),YDGT(1),YNEW(1),
1 YDEV(1),FWDEL(1),TBDEL(1)
DIMENSION C(3),D(3)
COMMON /MAGIQ/ KKNT
DOUBLE PRECISION YNEW,YPRD
DOUBLE PRECISION TIC,STEP,DTAU,DELTA,TIME,DTIME
DATA C,D / .5,.5,1.0,.5,.0,.5/
MSET=1
TIME = TIC
TAU = TIC
IF (DELTA)200,201,200
200 DTIME = 0.0078125
GO TO 225
201 DTIME = STEP
225 DO 102 I = 1,NEQNS
YDEV(I) = 0.0
YPRD(I) = YICS(I)
YCRRR(I) = YICS(I)
102 YNEW(I) = YICS(I)
MAGOUT = -2
GO TO 264
555 CONTINUE
ENTRY HAND (MAGIN,MAGOUT,TIC,STEP,NEQNS,DTAU,EPSIL,DELTA,ERR,
1 TIME,DTIME,YICS,YPRD,YCRRR,YDGT,YNEW,YDEV,FWDEL,
2 TBDEL)
5556 CONTINUE
MSET=2
IF (MAGOUT) 305,101,101
101 IF (MAGIN) 21, 27, 14
27 K = 0
202 YNEW(I) = YPRD(I)
21 K = K + 1
KKNT = K
210 DO 2 I = 1,NEQNS
GO TO (9,6,7,4,1),K
9 FWDEL(I) = YDGT(I)
GO TO 105
6 TBDEL(I) = YDGT(I)
GO TO 105
7 TBDEL(I) = TBDEL(I) + YDGT(I)
105 YPRD(I) = YNEW(I) + C(K)*DTIME*YDGT(I)
GO TO (2,2,400),K
400 YCRRR(I) = YPRD(I)
2 CONTINUE
TIME = TIME + D(K)*DTIME
99 MAGOUT = 0.0
264 RETURN
4 DO 8 I = 1,NEQNS
YPRD(I) = YNEW(I) + DTIME*(FWDEL(I) + 2.*TBDEL(I) + YDGT(I))/6.
8 YDEV(I) = YCRRR(I) - YPRD(I)
GO TO 99
11 IF (DELTA)80, 5,80
80 DO 13 I = 1,NEQNS
IF (EPSIL*ABS(YCRRR(I)) + ERR - ABS(YDEV(I))) 14,13,13

```

```

13 CONTINUE
  IF (SIGB)15,15,205
205 SIGB = 0.0
  GO TO 5
15 SIGC = 0.0
  DO 207 I = 1,NEQNS
    IF (ERR /100.+ DELTA*ABS(YCORR(I)) - ABS(YDEV(I))) 5,207,207
207 CONTINUE
    DTIME = 2.*DTIME
    5 DO 208 I = 1,NEQNS
208 YCORR(I) = YPRED(I)
209 IF (DTAU) 19,30,19
19 IF (TAU - TIME)20,20,27
20 TAU = TAU + DTAU
30 MAGOUT = 2
  GO TO 264
14 DTIME = DTIME/2.0
25 IF (K-3148,26,26)
26 TIME = TIME - DTIME - DTIME
  GO TO 47
48 TIME = TIME - DTIME
47 SIGB = +2.
  DO 209 I = 1,NEQNS
209 YDOT(I) = FWDDEL(I)
212 K = 0
  GO TO 21
  END
1900570
1900580
1900590
1900600
1900610
1900620
1900630
1900640
1900650
1900660
1900670
1900680
1900690
1900700
1900710
1900720
1900730
1900740
1900750
1900760
1900770
1900780
1900790
1900800
1900810
1900820
1900830

```

```

C ..... ROUTINE ** T0B0R ** ABACUS UPDATED 07/07/72 .....
SUBROUTINE T0BAR (ST,KLUE2,NR0W,NR,LL,ER,ES,E1,E2,H1,H0,T,T11,
1 T00,TIK,T0K,DEGRES,G2,G3,TIME)
INTEGER SAVJTC,SAVSTP,Q,THICK
INTEGER XN1,XN2,XN
REAL*4 I2
DOUBLE PRECISION SAVTIC,TIC,PHI,ST0P,REST0P,RTICK
DOUBLE PRECISION YPRED,TIME
COMMON ST0RY(I6),XMAT(110,10),STD(10),SADUS(30),RADIUS(30)
COMMON TADUS(30),UADUS(30),SAVTIC(900)
COMMON XN,TEREE,TIC,PHI,ST0P,REST0P,RTICK,G1,XN1(2),NH
COMMON NST(30),NKL(30),NXMAT(20),SAVJTC(30),SAVSTP(30),JRTIC(30)
COMMON JST0(30),NREG,NRPT,NRC,NSC,NIX,IERR0R,KGE0M,IGE0M,ISTTAB
COMMON KELVIN,IBEGIN,NPR0B,NSEG,NERR0R,Q,THICK,N0JS,NLINKS,NLCASE
COMMON NTSK1,NZ,NBCT,LINPUT,NTRKL,NPASS,XN1,KBC,NRINGS
COMMON /LASTEQ/ YPRED(I6),YD0T(I6),YASAVE(I6),
1 YANTH,YAMTH,YAMPT,YANPT,Y0PH,YA0PH,YAQTH,YAJPH,
2 S,SN,CS,SNSQ,CSSQ,TAN,SEC,CN,XICS,XISN,IN,
3 XIR0,XIR0SQ,XISNR0,XICSR0,CNIR0,SNIR0,CSIR0,
4 XIR1,XIR2,CSIR1,CSIR2,SNIR1,XIRISQ,R2SQ,R0,BESQ,
5 R0SQ,XNSQ,BETA,R1,R2,S1,RID0T,RLSQ,
6 XNTH,XNTPH,XMTPH,XFTHLD,XFPHLD,XFZELO,
7 XMTHLD,XMPLD,ETHET(2),EPHI(2),XGPT(2),ALPHTH(2),ALPHPH(2),
8 XNUTP,XNUPT,XC11,XC22,XC15,XD33,XD22,XD21,XD12,
9 XK11,XK12,XK21,XK22,XK33,XD11,
A M,I,SI,TIN,SI0UT,SI0IN,SI0UT,TPTIN,TPT0UT,
B ,XNPHI,BEITA,ZETTA,ZETTA,SAVY(8),XC16
C COMMON /SNILPS/ ANG,PSI(100),RAD(100),CUR1(100),CUR2(100),
1 DRIDP(100),Z(114),RI(14),NRZIN
DIMENSION ST(72,31)
DATA A/-A -/
IF (KBC.EQ.0) G0 T0 500
L = 1
IF (NLCASE.EQ.1) G0 T0 800
L = 3
SAVY(4) = ST(NR0W-1,LL)
SAVY(5) = ST(NR0W,LL)
SAVY(6) = 0.0
800 SAVY(1) = ST(NR0W-L,LL)
L = L-1
SAVY(2) = ST(NR0W-L,LL)
SAVY(3) = 0.0
500 CONTINUE
G0T0 (771,772,773,774,775,776,70771),KGE0M
GEOMETRY FOR ELIPSE(G3=0FFSET DISTANCE )
771 A=G1
BE=G2
BETA = BE
BESQ=RE**2
ASQ=A**2
SN = DSIN(PHI)
CS = DCOS(PHI)
SNSQ = SN**2
CSSQ = CS**2
R2 = A*SQRT(1.0/(SNSQ+BESQ*CSSQ))
R2SQ = R2**2
K0=R2*SN
R1=R2*R2SQ*BESQ/ASQ
BESQ=BE**2

```



```

R1DØT=0.0
IF (KGEØM.EQ.1.AND.BETA.NE.1.0.AND.SN.NE.0.0)R1DØT=3.0*(R2*BETA/
1A) **2*(CS/SNSQ)*(R1*SN-RØ)
IF (SN.EQ. 0.0)GØ TØ 779
R2 = R2-G3/SN
R2SQ = R2**2
RØ = RØ-G3
GØ TØ 7775
779 IF (G3 .EQ. 0.0)GØ TØ 7775
RØ = -G3
GØ TØ 7775
GEØMETRY FØR ØGIVE
C 772 R1=G1
C=G2
SN = DSIN(PHI)
CS = DCØS(PHI)
IF (SN.EQ.0.0) GØTØ 777
R2=R1-C/SN
GØTØ 778
777 R2 = 1.0
778 RØ = R1*SN-C
R1DØT=0.0
GØTØ 7775
GEØMETRY FØR CØNE
C 773 SN= SIN(G1)
S=PHI
S1=1.0/S
R2=CS*SN*PHI
RØ=PHI*CS
R1DØT=0.0
GØTØ 7775
GEØMETRY FØR CYLINDER
C 774 RØ = G1
SN=1.0
CS=1.0
R1DØT=0.0
GØTØ 7775
MODIFIED ELLIPSE
C 775 XNEXP=G1
A =G2
XN1=1.0+XNEXP
XN2=1.0/XN1
XN3=XN1+1.0
XN4=XN3+1.0
XN5=XN4/XN1
SN = DSIN(PHI)
CS = DCØS(PHI)
R2= A*(2.0/(1.0+SN**XN1))**XN2
R1=(A/2.0)*(R2/A)**XN3
RØ=R2*SN
R1DØT=-XN3*A*(SN**XNEXP*CS/4.0)*(2.0/(1.0+SN**XN1))**XN5
GØTØ 7775
GENERAL GEØMETRY
C 776 SN = DSIN(PHI)
CS = DCØS(PHI)
TAN = SN / CS
SEC = 1.0 / CS
IF (TIME.EQ.TIC) CALL TEMØEG
ARG = PHI

```

```

D0 204 J=1,100
PH0 = PSI(J)
IF (ANG.EQ.A) IF (ARG-PH0) 221,223,204
IF (PH0-ARG) 221,223,204
221 IF (J-1) 8502,8502,224
204 CONTINUE
C0 T0 8503
223 R0 = RAD(J)
R1 = CUR1(J)
R2 = CUR2(J)
R100T = DRIDP(J)
C0 T0 7775
8502 NERR0R = 41
C0 T0 8888
8503 NERR0R = 42
8888 NIX = 1
C0 T0 8889
224 SUB1 = ARG-PSI(J-1)
SUB2 = PSI(J)-PSI(J-1)
R0 = RAD(J-1)+(RAD(J)-RAD(J-1))*SUB1/SUB2
R1 = CUR1(J-1)+(CUR1(J)-CUR1(J-1))*SUB1/SUB2
R2 = CUR2(J-1)+(CUR2(J)-CUR2(J-1))*SUB1/SUB2
R100T = DRIDP(J-1)+(DRIDP(J)-DRIDP(J-1))*SUB1/SUB2
C0 T0 7775
C TS0TENS0ID GEOMETRY
7077 CONTINUE
SN = DSIN(PHI)
CS = DCOS(PHI)
A = G1
R2 = A / SORT(SN)
R1 = 0.5 * R2
R0 = R2 * SN
R100T = - ((A**2)*0.5)*(R1*CS)/R0**2
7775 IAN=SN/CS
DEGRES = 0.0
IF (IGE0M.EQ.1) DEGRES = PHI * 57.29578
R0SQ = R0**2
XNSQ=XN**2
CN=CS*SN
X1CS=1.0/CS
TN=SN/CS
X1R0=1.0/R0
X1R0SQ=1.0/R0**2
X1CSR0=1.0/(CS*R0)
CNIR0=CN/R0
SNIR0=SN/R0
CSIR0=CS/R0
SNS0=SN**2
CSSQ=CS**2
IF (KGE0M.EQ.4.0R.KGE0M.EQ.3) G0T0 79
R1SQ = R1**2
R2SQ = R2**2
X1SN=1.0/SN
X1SNR0=1.0/(SN*R0)
X1R1=1.0/R1
X1R2=1.0/R2
CSIR1=CS/R1
CSIR2=CS/R2
SNIR1=SN/R1
X1R1SQ=1.0/R1**2
79 XNTH=0.0

```



```

C      RANKIN=THINH MEANS INTERPOLATE, BUT DO NOT COMPUTE NTEMP, MTEMP
C
C
711 CONTINUE
    XK11=ST(2,LL)
    XK12=ST(3,LL)
    XK22 = ST(4,LL)
    XK33 = ST(5,LL)
    XD11 = ST(6,LL)
    XD12 = ST(7,LL)
    XD22 = ST(8,LL)
    XD33 = ST(9,LL)
    XC11 = ST(10,LL)
    XC22 = ST(11,LL)
    XC15 = ST(12,LL)
    XC16 = ST(13,LL)
    XK21 = XK12
    XD21 = XD12
    GO TO 103

40 CONTINUE
    TEMP3= (1.0-XNUPT * XNUTP)
    PERM= TEMP3
    E1= (ETHET(1)+ EPHI(1))/2.
    E2= (ETHET(2)+ EPHI(2))/2.
    ES1= E1+E2
    GO TO (42,47,49,41),THICK
41 GO TO (103,42,103,42,47,49,42,47,49,42,47,49),ISTTAB
C
C
SINGLE SHEET
42 TEMP1= ETHET(1) * HI
    TEMP2= TEMP1 * HI**2
    XK11= TEMP1/TEMP3
    XD11= TEMP2/(12.0* TEMP3)
    TEMP1= EPHI(1)* HI
    TEMP2= TEMP1*HI**2
    XK22= TEMP1/TEMP3
    XD22= TEMP2/(12.0* TEMP3)
    XK33= XGPT(1)* HI
    XD33= XK33*HI**2/12.0
    GO TO 55
C
C
EQUAL SHEETS
47 EPSUM= EPHI(1)+ EPHI(2)
    ETSUM= ETHET(1)+ ETHET(2)
    XK11= ETSUM * HI/PERM
    XK22= EPSUM * HI/PERM
    XK33= HI*(XGPT(1)+ XGPT(2))
    ZBRIN = (HI*(E1+3.0*E2)+2.0*E2*T)/(2.0*ES1)
    ZBR0UT = (HI*(E2+3.0*E1)+2.0*E1*T)/(2.0*ES1)
    ZBHIN= (ZBRIN- HI/2.0)**2
    ZBH0UT=(ZBR0UT-HI/2.0)**2
    XD33= (HI**3*(XGPT(1)+XGPT(2)))/12.0+ HI*(XGPT(1)* ZBHIN
1      + XGPT(2)* ZBH0UT)
    XD11=(XK11* HI**2)/12.+ HI*( ETHET(1) * ZBHIN + ETHET(2)*ZBH0UT)
    I/PERM
    XD22=(XK22* HI**2)/12.+ HI*( ETHET(1) * ZBHIN + ETHET(2)* ZBH0UT)
    I/PERM
    GO TO 55

```

C UNEQUAL FACE SHEETS
 C
 C
 49 CONTINUE
 ZBRIN=((E1*HI**2)+(E2*H0**2)+(2.0*E2*H0*HI)+(2.0*E2*H0*T))/
 1 (2.0*(E1*HI+E2*H0))
 /BR0UT=((E1*HI**2)+(E2*H0**2)+(2.0*E1*H0*HI)+(2.0*E1*HI*T))/
 1 (2.0*(E1*HI+E2*H0))
 /BHIN=(ZBRIN-HI/2.0)**2
 /BHOUT=(ZBR0UT-H0/2.0)**2
 XK11=(ETHET(1)*HI+ETHET(2)*H0)/PERM
 XK22=(EPHI(1)*HI+EPHI(2)*H0)/PERM
 XK33=(XGPT(1)*HI+XGPT(2)*H0
 XD33=(XGPT(1)*HI**3+XGPT(2)*H0**3)/12.+HI*(XGPT(1)*ZBHIN)+
 1 XGPT(2)*ZBHOUT*H0
 D11=(ETHET(1)*HI**3+ETHET(2)*H0**3)/12.
 XD11=(D11+(HI*ETHET(1)*ZBHIN)+(H0*ETHET(2)*ZBHOUT))/PERM
 D22=(EPHI(1)*HI**3+EPHI(2)*H0**3)/12.
 XD22=(D22+(HI*EPHI(1)*ZBHIN)+(H0*EPHI(2)*ZBHOUT))/PERM
 DETERMINE COMPLETE CONSTANTS DEPENDENT ON REINFORCEMENT CLUE
 C
 C
 C
 55 CONTINUE
 IF(ISTAB.EQ.2)GO TO 103
 EASPH=ER*ATH/STH
 EASPH=ES*APH/SPH
 EISPH=F5*XIPH/SPH
 EISTH=ER*XITH/STH
 GO TO (58,60,100),KLU2
 C
 C
 C
 58 CONTINUE
 XK12=XK11*XNUTP
 XK11=XK11+EASTH
 XK22=XK22+EASPH
 XC11=EASTH*CTH
 XC22=EASPH*CPH
 XD22=-XD22-EISPH
 XD33=XD33+GJPH/(4.0*SPH)+GJTH/(4.0*STH)
 XD12=-XD11*XNUTP
 XD11=-XD11-EISTH
 XK21=XK12
 XD21=XD12
 GO TO 103
 C
 C
 C
 60 CONTINUE
 SINB=SIN(BETTA)
 COSB=COS(BETTA)
 SN2T04=2*(SINB**4)
 D=.STH*(COSB*SINB)
 ED=ER*ATH/D
 SINB2=SINB**2
 HL=2.0*(ABS(ZETTA)-ABS(CTH))
 I2=(ATH**3.)/((3*HL**2)
 95 XC22=2.0*CTH*COSB**3*ED
 XC15=2.0*CTH*COSB*SINB2*ED
 XC16=XC15
 GR1=ER*12/(2.0*(1.0+XNUTP)*D)
 XC11=CTH*SN2T04/COSB*ED
 2603040
 2603050
 2603060
 2603070
 2603080
 2603090
 2603100
 2603110
 2603120
 2603130
 2603140
 2603150
 2603160
 2603170
 2603180
 2603190
 2603200
 2603210
 2603220
 2603230
 2603240
 2603250
 2603260
 2603270
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ED1 = ER*XI1H/D
SN4T02 = 4.*SINB2
XD22 = -XD22-2.0*C0SB**3*EDI-SN4T02*C0SB*GRI
TB = 2.0* BETTA
XD33 = XD33+((4.0*C0S(TB))*
1*2*GRI)/ C0SB) + (2.0*C0SB*SINB2*EDI)
XD12 = -XD11*XNUTP-(2.0*C0SB
1*SINB2*EDI)-(SN4T02*C0SB*GRI )
XK12= XK11*XNUTP + (2.0*C0SB*SINB2*ED)
XK22=XK22+(2*C0SB**3*ED)
XK33=XK33+(2*C0SB*SINB2*ED)
XK11=XK11+(SN2T04*ED/C0SB)
XD11 = -XD11-SN2T04*EDI/C0SB-(
1 SN4T02*C0SB*GRI)
XK21 = XK12
XD21 = XD12
G0 T0 103
C
C
C
100 CONTINUE
SNB =SIN(BETTA)
CSB =C0S(BETTA)
TBETTA= 2.0*BETTA
CS2B= C0S(TBETTA)
0NEC2B=(1.0+ CS2B)/2.
SCB2 =(SNB-CS2B*SNB + 2.)/(2.0*CSB)
SN2B =SIN(TBETTA) /2.
XK12=XK11*XNUTP + (EASTH*SNB*0NEC2B/CSB)
XK11=XK11+ EASTH*SCB2
XK22=XK22+ EASTH*(CSB/SNB*0NEC2B)
XK33=XK33+ EASTH* SN2B
XC11= (EASTH*CTH* SCB2 )
XC15=EASTH*CTH*( SNB* 0NEC2B/CSB )
XC16=EASTH*CTH*SN2B
XC22= EASTH*CTH* (CSB/SNB * 0NEC2B)
XD12=-XD11*XNUTP- E1STH*(SNB*0NEC2B/CSB)
XD11=-XD11- E1STH*SCB2
XD22 = -XD22-E1STH*(CSB/SNB*0NEC2B)
XD33= XD33+ E1STH*SN2B
XK21 = XK12
XD21 = XD12
C
C
C
103 CONTINUE
G0T0 (716,714,715,714),KELVIN
716
T11 = ST(NRW+1,LL)
T1K = ST(NRW+2,LL)
T0K = ST(NRW+3,LL)
T00 = ST(NRW+4,LL)
G0 T0 717
715
T11 = ST(NRW+1,LL)
T1K = T11
T0K = T11
T00 = T11
C
717 TEMP11= ALPHTH(1)+ XNUTP * ALPHPH(1)
TEMP12= ALPHTH(2)+ XNUTP * ALPHPH(2)
TEMP21= ALPHPH(1)+ XNUTP * ALPHTH(1)

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TEMP22= ALPHPHI(2)+ XNUPT * ALPHTH(2)
TEMP3 = 1-XNUPT*XNUTP
TEMP4 = HI/4.0
ETHK1= ETHET(1)*TEMP11/TEMP3
ETHK2 = ETHET(2)*TEMP12/TEMP3
TEMP5 = HI**2/24.0
TEMP61= TII+ TIK-2* TEFREE
TEMP62= T00+ T0K-2* TEFREE
TEMP71= 2.0* TII +TIK-3*TEFREE
TEMP72= 2.0* T00 +T0K-3*TEFREE
EPHK1 = EPHI(1)*TEMP21/TEMP3
EPHK2 = EPHI(2)*TEMP22/TEMP3
C0 T0 (H11.812,813,814),THICK

811 XNTH= ETHK1 * TEMP4 * (TEMP61+ TEMP62)
XNTPH= EPHK1 * TEMP4 * (TEMP61 + TEMP62)
XNTH= ETHK1 * TEMP5 * (TEMP71- TEMP72)
XNTPH= EPHK1 * TEMP5 * (TEMP71 - TEMP72)
C0 T0 714

812 TI = (HI*(E2-E1)+2.0*E2*T)/(2.0*(E1+E2))
T0 = (HI*(E1-E2)+2.0*E1*T)/(2.0*(E1+E2))
TEMP8= HI/2.0
XNTH= ETHK1 * TEMP8*TEMP61 + ETHK2 * TEMP8*
TEMP62
XNTPH= EPHK1 * TEMP8*TEMP61 + EPHK2 * TEMP8*
TEMP62
XNTH=(ETHK1 * TEMP8 * (HI*TEMP71/3.0+ TI*TEMP61)) - (ETHK2 *
TEMP8*(HI*TEMP72/3.0+T0*TEMP62))
XNTPH=(EPHK1 * TEMP8 * (HI*TEMP71/3.0+ TI*TEMP61)) - (EPHK2 *
TEMP8*(HI*TEMP72/3.0+T0*TEMP62))
C0 T0 714

813 FI = (E2*H0**2-E1*H1**2+2.0*E2*H0*T)/(2.0*(E1*H1+E2*H0))
T0 = (E1*H1**2-E2*H0**2+2.0*E1*H1*T)/(2.0*(E1*H1+E2*H0))
XNTH= ETHK1*0.5*(HI*TEMP61)+ETHK2*0.5*(H0*TEMP62)
XNTPH= EPHK1*0.5*(HI*TEMP61)+ EPHK2*0.5*(H0*TEMP62)
XNTH= ETHK1*0.5*(HI**2*TEMP71/3.0+TI*HI*TEMP61)-ETHK2*0.5*(H0
**2*TEMP72/3.+ T0*H0*TEMP62)
XNTPH= EPHK1*0.5*(HI**2*TEMP71/3.0+TI*HI*TEMP61)-EPHK2*0.5*(H0
**2*TEMP72/3.+ T0*H0*TEMP62)
C0 T0 714

814 TEMP10=(((-XK11*X0D11)**.5)/(48.0**5)
TEMP11 = ((-XK22*X0D21)**.5)/(48.0**5)
XNTH = (XK11/4.0 *TEMP11)* TEMP61 + (XK11/4.0*TEMP12) * TEMP62
XNTPH = (XK22/4.0 *TEMP21)* TEMP61 + (XK22/4.0*TEMP22) * TEMP62
XNTH= TEMP10*(TEMP11*TEMP71 - TEMP12* TEMP72)
XNTPH= TEMP11 *(TEMP21*TEMP71 - TEMP22* TEMP72)
714 CONTINUE
8889 RETURN
END

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C ..... ROUTINE ** TEMØG ** ABACUS UPDATED 07/07/72 .....
C SUBROUTINE TEMØG
C THIS SUBROUTINE CALCULATES THE GEOMETRY FOR A SHELL SEGMENT.
C THE INPUT VARIABLES ARE . . .
C RI(1) -- DISTANCE FROM AXIS OF REV. TO POINTS.
C ON SHELL MERIDIAN.
C ZI(1) -- DISTANCE ALONG AXIS OF REV. TO THE
C INTERSECTION OF THE CORRESPONDING RI(1) AND
C THE AXIS OF REV.
C NRZIN -- NUMBER OF (RI,ZI) PAIRS READ AS INPUT.
C
C COMMON /SNILPS/ ANG,PSI(100),RAD(100),CUR1(100),CUR2(100),
C DRDP(100),ZI(14),RI(14),NRZIN
C DIMENSION CI(14,13),DRDZ(14),SØUT(14),S(101),RADØ(100)
C
C FUN(ANG) = SORT(1.0 + ARG**2)
C
C RADØ = 3.1415926/180.0
C DATA 8/-8 -/
C AMULT = 1.0
C IF (ANG.EQ.8) AMULT = -1.0
C
C PASS SPLINE CURVE THROUGH INPUT POINTS ON SHELL MERIDIAN, AND
C COMPUTE DR/DZ AT THESE POINTS.
C
C CALL PLYCØ (ZI,RI,NRZIN,CI)
C NDELZ = NRZIN - 1
C DO 60 I=1,NRZIN
C CALL PLYNE (ZI,RI,NRZIN,CI,ZI(1),FAKEL,DRDZ(1),FAKE2)
C 60 CONTINUE
C
C COMPUTE MERIDIONAL ARC LENGTH TO INTERPOLATED POINTS BY
C NUMERICAL INTEGRATION (SIMPSON'S RULE). SINCE SIMPSON'S RULE
C REQUIRES AN EVEN NUMBER OF PARTITIONS, INTERPOLATE A POINT
C MIDWAY BETWEEN EACH PAIR OF POINTS USING SUBROUTINE PLINE.
C
C SØUT(1) = 0.
C DO 70 I=1,NDELZ
C DZ2=(ZI(I+1)-ZI(1))/2.0
C DZ6=DZ2/3.0
C CALL PLYNE (ZI,RI,NRZIN,CI,ZI(1)+DZ2,FAKEL,DRDZM,FAKE2)
C SØUT(I+1) = SØUT(1) + DZ6*(FUN(DRDZ(1)) + 4.0*FUN(DRDZM) +
C FUN(DRDZ(I+1)))
C 70 CONTINUE
C
C USE SPLINE TO REPRESENT RI(1) AS A FUNCTION OF SØUT(1). THEN USE
C SPLINE TO INTERPOLATE RADØ AND CORRESPONDING DERIVATIVES. FROM
C THESE, COMPUTE THE TWO PRINCIPAL RADII OF CURVATURE,
C CUR1 = 1/RI
C CUR2 = 1/R2
C
C CLDH1 = SØUT(NRZIN)/99.0
C CALL PLYC2 (SØUT,RI,NRZIN,CI)
C DO 110 I=1,100
C S(I) = FLØAT(I-1)*ØLDHI
C CALL PLYNE (SØUT,RI,NRZIN,CI,S(1),RAD(1),RADØ(1),RADØ2)
C IF (ABS(RADØ(1))-ØT-1.0) RADØ(1)=1.0
C FACTØR = SORT(1.0-RADØ(1)**2)
C CUR1(1) = -RADØ2/FACTØR
C CUR2(1) = FACTØR/RAD(1)

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3000800
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110 CONTINUE
  DO 180 J=1,100
    COSPSI = AMULT*RADD(J)
    PSI(J) = ARCOS(COSPSI)
    SINPSI = -AMULT*RAD(J)*CUR2(J)
    IF (ANG.EQ.B) GO TO 179
    PSI(J) = 2.0*3.1415926-PSI(J)
179 CONTINUE
    CUR1(J) = -AMULT/CUR1(J)
    CUR2(J) = -AMULT/CUR2(J)
    IF (J.EQ.1) GO TO 180
    I = 1
    IF (J.EQ.2) GO TO 181
    I = 2
181 IF (ANG.EQ.B) GO TO 190
    DR1OP(J-I) = (CUR1(J)-CUR1(J-I))/(PSI(J)-PSI(J-I))
    GO TO 180
190 DR1OP(J-I) = (CUR1(J)-CUR1(J-I))/(PSI(J-I)-PSI(J))
180 CONTINUE
    DR1DP(100) = DR1OP(99)
    DO 42 J=1,100
      DR1OP(J) = DR1DP(J)*0.1
42 CONTINUE
  RETURN
END

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C ..... ROUTINE ** PLYC0 ** ABAQUS UPDATED 05/20/72 .....
C SUBROUTINE PLYC0 (X,Y,M,C)
C SUBROUTINE TO DETERMINE C(1,K),C(2,K),C(3,K) AND C(4,K).
C DIMENSION X(14),Y(14),A(14,3),B(14),Z(14)
C DIMENSION D(13),P(13),E(13),C(4,13)
C MM = M-1
C D0 10 K=1,MM
C   D(K) = X(K+1) - X(K)
C   P(K) = D(K)/6.0
C 10 E(K) = (Y(K+1)-Y(K))/D(K)
C D0 20 K=2,MM
C   B(K) = E(K) - E(K-1)
C   A(1,2) = -1.0-D(1)/D(2)
C   A(1,3) = D(1)/D(2)
C   A(2,3) = P(2)-P(1)*A(1,3)
C   A(2,2) = 2.0*(P(1)+P(2)) - P(1)*A(1,2)
C   A(2,3) = A(2,3)/A(2,2)
C   B(2) = B(2)/A(2,2)
C D0 30 K=3,MM
C   A(K,2) = 2.0*(P(K-1)+P(K))-P(K-1)*A(K-1,3)
C   B(K) = B(K)-P(K-1)*B(K-1)
C   A(K,3) = P(K)/A(K,2)
C 30 B(K) = B(K)/A(K,2)
C   O = D(M-2)/D(M-1)
C   A(M,1) = 1.0+O*(M-2,3)
C   A(M,2) = -O*(M,1)*A(M-1,3)
C   B(M) = B(M-2)-A(M,1)*B(M-1)
C   Z(M) = B(M)/A(M,2)
C MN = M-2
C D0 40 I=1,MN
C   K = M-I
C 40 Z(K) = B(K)-A(K,3)*Z(K+1)
C   Z(1) = -A(1,2)*Z(2)-A(1,3)*Z(3)
C D0 50 K=1,MM
C   Q = 1.0/(6.0*D(K))
C   C(1,K) = Z(K)*Q
C   C(2,K) = Z(K+1)*Q
C   C(3,K) = Y(K)/D(K)-Z(K)*P(K)
C 50 C(4,K) = Y(K+1)/D(K)-Z(K+1)*P(K)
C RETURN
C END

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C ..... ROUTINE ** PLYNE ** ABACUS UPDATED 05/20/72 .....
C SUBROUTINE PLYNE (X,Y,M,C,XINT,YINT,DYDX,D2YDX2)
C SUBROUTINE FOR SPLINE FIT INTERPOLATION IN THE TABLE OF VALUES
C (X1,Y1) TO (XM,YM), WHERE M MAY BE AS LARGE AS 100, HERE THE
C CONSTANTS C(1,K),C(2,K),C(3,K) AND C(4,K) ARE ALREADY COMPUTED
C AND STORED.
C SUBROUTINE ALSO COMPUTES DY/DX AND D2Y/DX2 AT XINT.
C DIMENSION X(14),Y(14),C(4,13)
C IF (XINT-X(1)) 80,10,20
10 YINT = Y(1)
K=1
C0 TO 70
20 K = 1
30 IF (XINT-X(K+1)) 60,40,50
40 YINT = Y(K+1)
C0 TO 70
50 K = K + 1
IF (M-K) 80,80,30
60 YINT = (X(K+1) - XINT)*(C(1,K)*(X(K+1)-XINT)**2+C(3,K))
YINT = YINT + (XINT-X(K))*(C(2,K)*(XINT-X(K))**2+C(4,K))
70 DYDX=-3.0*(C(1,K)*(X(K+1)-XINT)**2-C(2,K)*(XINT-X(K))**2)
1 -C(3,K)+C(4,K)
D2YDX2=6.0*(C(1,K)*(X(K+1)-XINT)+C(2,K)*(XINT-X(K)))
RETURN
80 WRITE (6,90)
90 FORMAT (31H OUT OF RANGE FOR INTERPOLATION)
RETURN
END

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3100210
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3100250
3100260
3100270

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SUBROUTINES ODE1 AND ODE2

Subroutine LEBEGE calls either ODE1 or ODE2, as necessary, and various geometric and trigonometric clues, as well as the predicted values of the variables for the differential equations, are passed to this subprogram via label common area LASTEQ.

The equations in ODE1 and ODE2 are identical to those in subroutines DIF1 and DIFF2 respectively, with the addition of the auxiliary equations for YAQPH, and YAQTH. Subroutines ODE1 and ODE2 perform the final integration for each segment in the structure utilizing the initial conditions previously obtained, and return these values to LEBEGE via label common area LASTEQ.

The ODE1, ODE2 flow charts are identical to the DIF1, DIFF2 flow charts, respectively.

FORTRAN CODE	ENGINEERING SYMBOLS (REF. 1)
YANPT	$N_{\phi\theta}$
YAQPH	Q_{ϕ}
YAQTH	Q_{θ}
YAOPH	Ω_{ϕ}

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C ..... ROUTINE **D19 ** ABACUS UPDATED 07/07/72 .....
SUBROUTINE DDEL(XFPHL1,XFZEL1,XFPHL2,XFZEL2)
INTEGER SAVJTC,SAVSTP,Q,THICK
INTEGER XN1,XN
DOUBLE PRECISION SAVTIC,TIC,PHI,STØP,RESTØP,RTICK
DOUBLE PRECISION YPRED
COMMON STØRY(16),XMAT(110,10),STD(110),SADUS(30),RADIUS(30)
COMMON TADUS(30),UADUS(30),SAVTIC(900)
COMMON XN,TIC,PHI,STØP,RESTØP,RTICK,G1,XNL(2),NH
COMMON NST(30),NKL(30),NXMAT(20),SAVJTC(30),SAVSTP(30),JRTIC(30)
COMMON JRSTØP(30),NREG,NMPT,NRC,NSC,NIX,IERRØR,KGEØM,IGEM,ISTTAB
COMMON KBEGIN,NPRØB,NSEG,NERRØR,Q,THICK,NØJS,NLINKS,NLCASE
COMMON NTSKL,NZ,NBCT,LINPOT,NTRKL,NPASS,XNL,KBC,NRINGS
COMMON /LASTEQ/ YPRED(16),YDØT(16),YASAVE(16),
1 YANTH,YAMTH,YAMPT,YANPT,YABPH,YAQPH,YAQTH,YAJPH,
2 S,SN,CS,SNQS,CSSQ,TAN,SEC,CN,XICS,XISN,TN,
3 XIRØ,XIRØSQ,XISNRØ,XICSRØ,CNIRØ,SNIRØ,CSIRØ,
4 XIR1,XIR2,CSIR1,CSIR2,SNIR1,XIRISQ,R2SQ,RØ,BESQ,
5 RØSQ,XNSQ,BETA,R1,R2,S1,RIDØT,RISQ,
6 XNTH,XNTPH,XMTTH,XMTPH,XFTHLD,XFPHLD,XFZELD,
7 XNTHLD,XMPHLD,ETHET(2),EPI(2),XGPI(2),ALPHTH(2),ALPHPH(2),
8 XNUTP,XNUPT,XC11,XC22,XC15,XD33,XD22,XD21,XD12,
9 XK11,XK12,XK21,XK22,XK33,XD11,
A M,I,SITIN,SITØT,SIPIN,SIPØT,TPTIN,TPTØT,
B ZBRIN,ZBRØT,SCRIPA,SCRIP1,SIFIN,SIFØT,TZEPH,TZETH
C ,XNPHI,BETTA,ZETTA,SAVY(8),XC16
EQUIVALENCE (XNL(1),X1),(XNL(2),X2)
K = 0
IF (KBC-EQ.0-AND-NH-EQ.0) K = 1
IF (ISTTAB-EQ.1) GØ TØ 7786
IF (ISTTAB-GE.101GØ TØ 7786
C THE FØLLØWING EQUATIONS ARE THE -THICK- SET
GØ TØ (151,152,153),IGEMØ
C EQUATIONS FØR SHELLS ØF REVØLUTION ( PHI CØØRDINATE )
151 YANTH = XNUPT*YPRED(I+1)+(XK11-XNUPT**2*XK22)*(XN*YPRED(I+4)+
1 YPRED(I+5)*CS-YPRED(I+6)*SN)*XIRØ*(XNUPT*XNTPH-
2 XNTH)
YAMTH = XNUPT*YPRED(I+3)-(XØ11-XNUPT**2*XØ22)*XIRØ*(XN*
1 YPRED(I+4)*SN-XNSQ*YPRED(I+6))+YPRED(I+7)*CS)+K*
2 (XNUPT*XNTPH-XNTH)
YØPH = XN*YPRED(I+6)*XIRØ-YPRED(I+4)*SNIRØ
YAMPT = (-1.0/(RØ/XØ33))+XNSQ*XIRØ/XK33))*(-2.0*XN*
1 YPRED(I+7)+YPRED(I+4)*(CSIR1-CNIRØ)+XN*YPRED(I+5)*
2 (SNIRØ+XIR1)+2.0*XN*YPRED(I+6)*CSIRØ+YPRED(I+7)*SN/
3 XK33+SN*YØPH*(X1*SAVY(3)+X2*SAVY(6)))
YAJPH = YPRED(I+2)-YPRED(I+1)*(X1*SAVY(3)+X2*SAVY(6))
1 -YPRED(I+7)*(X1*SAVY(2)+X2*SAVY(5))
YANPT = YPRED(I)+YAMPT*SNIRØ
YDØT(I+4) = R1*(YPRED(I+4)*CSIRØ+XN*YPRED(I+5)*XIRØ+YPRED(I)/XK33+
1 YAMPT*SNIRØ/XK33)+R1*YØPH*(X1*SAVY(3)+X2*SAVY(6))
YDØT(I) = R1*(-2.0*YPRED(I)*CSIRØ+XN*YANTH*XIRØ-XN*YAMTH*SN*
1 XIRØSQ-YAMPT*CSIRØ*(XIR1-SNIRØ))-R1*(X1*XFTHLD+XMPHLD*
2 SNIRØ)-(YDØT(I+4)*(X1*XFPHL1+X2*XFPHL2)+R1*YØPH*
3 (X1*XFZEL1+X2*XFZEL2))-R1*SNIRØ*(YØPH*(X1*SAVY(1)+
4 X2*SAVY(4))-YANPT*(X1*SAVY(3)+X2*SAVY(6)))
YDØT(I+5) = R1*(YPRED(I+6)*XIR1+(1.0/(XK22-XNUTP**2*XK11))*
1 (YPRED(I+1)-XNUTP*YANTH+K*(XNTPH-XNUTP*XNTH)))
2 -R1*YPRED(I+7)*(X1*SAVY(3)+X2*SAVY(6))
EPSITH = XIRØ*(XN*YPRED(I+4)+YPRED(I+5)*CS-YPRED(I+6)*SN)
EPSIPH = XIR1*(YDØT(I+5)-YPRED(I+6))+YPRED(I+7)*(X1*SAVY(3)+

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2000650
1 YD0T(I+1) = R1*(CSIR0*(YANTH-YPRD(I+1))-XN*XIR0*(YPRD(I)+
2000660 YAMPT*(SN*XIR0+XIR1))*YPRD(I+2)*XIR1)-R1*K*XFPHD
2000670 -R1*((EPSITH+EPSIPH)*(X1*XFPHL1+X2*XFPHL2))-YPRD(I+7)*
2000680 (X1*XFZEL1+X2*XFZEL2))
2000690
YD0T(I+2) = R1*(-YPRD(I+2)*GSR0-YANTH*SNIR0-YPRD(I+1)*XIR1
2000700 +XNSQ*YANTH*XIR0SQ-2.0*XN*YAMPT*CS*XIR0SQ)+R1*K*
2000710 (XN*XMPLD*XIR0-XFZELD)-R1*(EPSITH+EPSIPH)*X1*
2000720 XFZEL1+X2*XFZEL2)+YPRD(I+7)*(X1*XFPHL1+X2*XFPHL2))
2000730
4 -R1*XIR0*XN*(YAMPT*(X1*SAVY(3)+X2*SAVY(6))-YAMPH*
2000740 (X1*SAVY(1)+X2*SAVY(4)))
2000750
YD0T(I+3) = R1*(YAMTH*CSIR0-YPRD(I+3)*CSIR0-2.0*XN*YAMPT*XIR0+
2000760 YAJPH+K*XMTHLD)
2000770
YD0T(I+6) = R1*(YPRD(I+7)-YPRD(I+5)*XIR1)
2000780
YD0T(I+7) = R1*(1.0/(XD22-XNUTP**2*XD11))*(-YPRD(I+3)+XNUTP*
2000790 YAMTH-K*(XMTPH-XNUTP*XMTH))
2000800
2000810
2000820
2000830
2000840
2000850
2000860
2000870
2000880
2000890
2000900
2000910
2000920
2000930
2000940
2000950
2000960
2000970
2000980
2000990
2001000
2001010
2001020
2001030
2001040
2001050
2001060
2001070
2001080
2001090
2001100
2001110
2001120
2001130
2001140
2001150
2001160
2001170
2001180
2001190
2001200
2001210
2001220
2001230
2001240
2001250

X2*SAVY(6))
1 YD0T(I+1) = R1*(CSIR0*(YANTH-YPRD(I+1))-XN*XIR0*(YPRD(I)+
YAMPT*(SN*XIR0+XIR1))*YPRD(I+2)*XIR1)-R1*K*XFPHD
-R1*((EPSITH+EPSIPH)*(X1*XFPHL1+X2*XFPHL2))-YPRD(I+7)*
(X1*XFZEL1+X2*XFZEL2))
YD0T(I+2) = R1*(-YPRD(I+2)*GSR0-YANTH*SNIR0-YPRD(I+1)*XIR1
+XNSQ*YANTH*XIR0SQ-2.0*XN*YAMPT*CS*XIR0SQ)+R1*K*
(XN*XMPLD*XIR0-XFZELD)-R1*(EPSITH+EPSIPH)*X1*
XFZEL1+X2*XFZEL2)+YPRD(I+7)*(X1*XFPHL1+X2*XFPHL2))
-R1*XIR0*XN*(YAMPT*(X1*SAVY(3)+X2*SAVY(6))-YAMPH*
(X1*SAVY(1)+X2*SAVY(4)))
YD0T(I+3) = R1*(YAMTH*CSIR0-YPRD(I+3)*CSIR0-2.0*XN*YAMPT*XIR0+
YAJPH+K*XMTHLD)
YD0T(I+6) = R1*(YPRD(I+7)-YPRD(I+5)*XIR1)
YD0T(I+7) = R1*(1.0/(XD22-XNUTP**2*XD11))*(-YPRD(I+3)+XNUTP*
YAMTH-K*(XMTPH-XNUTP*XMTH))
G0T0 9005
EQUATIONS FOR C0NE
152 YANTH=XNUTP*YPRD(I+1)+(XK11-XNUTP**2*XK22)*(X1CS/S)*(XN*YPRD(I+4
)+YPRD(I+5)*CS-YPRD(I+6)*SN)+K*(XNUTP*XMTPH-XNTH)
YAMTH=XNUTP*YPRD(I+3)-(1.0/S)*X1CS*(X011-XNUTP**2*XD22)*(1.0/S)*
X1CS*(XN*YPRD(I+4)*SN-XNSQ*YPRD(I+6))+YPRD(I+7)*CS)-
K*(XMTH-XNUTP*XMTPH)
YABPH = XN*YPRD(I+6)*X1CS/S-YPRD(I+4)*TAN/S
YAMPT=(-1.0/(S*CS/XD33)+(SN*TAN/(XK33*S)))*(-2.0*XN*YPRD(I+7)-
YPRD(I+4)*SN/S*XN*YPRD(I+5)*TAN/S+2.0*XN*YPRD(I+6)/S*YPRD
(I)*SN/XK33+SN*YABPH*(X1*SAVY(3)+X2*SAVY(6)))
YAJPH = YPRD(I+2)-YPRD(I+1)*(X1*SAVY(3)+X2*SAVY(6))
-YPRD(I+7)*(X1*SAVY(2)+X2*SAVY(5))
YANPT = YPRD(I)*YAMPT*TAN/S
YD0T(I+4)=(1.0/S)*(YPRD(I+4)-XN*YPRD(I+5)*X1CS+YAMPT*TAN/XK33)
+YPRD(I)/XK33+YABPH*(X1*SAVY(3)+X2*SAVY(6))
YD0T(I) = -2.0*YPRD(I)/S*XN*YANTH*X1CS/S-XN*YANTH*SN*X1CS**2/S**2
+YAMPT*TAN/S**2-K*(XFTHLD+XMPLD*TAN/S)-(YD0T(I+4)*
(X1*XFPHL1+X2*XFPHL2)+YABPH*(X1*XFZEL1+X2*XFZEL2))-
TAN/S*(YABPH*(X1*SAVY(1)+X2*SAVY(4))-YANPT*(X1*SAVY(3)
+X2*SAVY(6)))
YD0T(I+5) = (1.0/(XK22-XNUTP**2*XK11))*(YPRD(I+1)-XNUTP*YANTH+
K*(XMTPH-XNUTP*XMTH))-YPRD(I+7)*(X1*SAVY(3)+X2*
SAVY(6))
EPSITH = (1.0/(S*CS))*(XN*YPRD(I+4)+CS*YPRD(I+5))-SN*
YPRD(I+6))
EPSIPH = YD0T(I+5)+YPRD(I+7)*(X1*SAVY(3)+X2*SAVY(6))
YD0T(I+1)= -YPRD(I+1)/S+YANTH/S-XN*YPRD(I)/(S*CS)-XN*YAMPT*SN/
(S**2*CS**2)-K*XFPHD-(EPSITH+EPSIPH)*(X1*XFPHL1+X2*
XFPHL2)+YPRD(I+7)*(X1*XFZEL1+X2*XFZEL2)
YD0T(I+2) = -YPRD(I+2)/S-YANTH*TAN/S+XNSQ*YAMTH/(S**2*CS**2)
-2.0*XN*YAMPT/(S**2*CS)+K*(XN*XMPLD*X1CS/S-XFZELD)
-(EPSITH+EPSIPH)*(X1*XFZEL1+X2*XFZEL2)-YPRD(I+7)*
(X1*XFPHL1+X2*XFPHL2)-X1CS/S*XN*(YAMPT*(X1*SAVY(3)+
X2*SAVY(6))-YABPH*(X1*SAVY(1)+X2*SAVY(4)))
YD0T(I+3)= YAMTH/S-YPRD(I+3)/S-2.0*XN*YAMPT/(S*CS)+YAJPH+XMTHLD
*K
YD0T(I+6)=YPRD(I+7)
YD0T(I+7)=(1.0/(XD22-XNUTP**2*XD11))*(-YPRD(I+3)+XNUTP*YAMTH-
K*(XMTPH-XNUTP*XMTH))
G0 T0 9005
EQUATIONS FOR CYLINDER
153 YANTH=XNUTP*YPRD(I+1)+(XK11-XNUTP**2*XK22)*(X1R0*(XN*YPRD(I+4)-
YPRD(I+6)))+K*(XNUTP*XMTPH-XNTH)
YAMTH=XNUTP*YPRD(I+3)-(X1R0*(X011-XNUTP**2*XD22))*(X1R0*(XN*YPRD

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1  (I+4)-XNSQ*YPRED(I+6)))+(XNUPT*XMTTH-XMTTH) 2001260
YABPH = XIR0*(XN*YPRED(I+6))-YPRED(I+4)) 2001270
YAMPT=(-1.0/(X033)+(XIR0/XK33)))*(-2.0*XN*YPRED(I+7)+XN*XIR0* 2001280
YPRED(I+5)+YPRED(I)/XK33+YABPH*(X1*SAVY(3)+X2* 2001290
SAVY(6))) 2001300
YAJPH = YPRED(I+2)-YPRED(I+1)*(X1*SAVY(3)+X2*SAVY(6)) 2001310
-YPRED(I+7)*(X1*SAVY(2)+X2*SAVY(5)) 2001320
YANPT = YPRED(I+1)+YAMPT*XIR0 2001330
YD0T(I+4)=XN*YPRED(I+5)+XIR0*YPRED(I)/XK33+YAMPT*XIR0/XK33 2001340
+YABPH*(X1*SAVY(3)+X2*SAVY(6)) 2001350
YD0T(I) = XN*YANTH*XIR0-XN*YANTH*XIR0SQ-K*(XFTHLD*XMPHLD*XIR0) 2001360
-(YD0T(I+4)*(X1*XFPHL1+X2*XFPHL2)+YABPH*(X1*XFZEL1+ 2001370
X2*XFZEL2))-XIR0*(YABPH*(X1*SAVY(1)+X2*SAVY(4))-YANPT* 2001380
(X1*SAVY(3)+X2*SAVY(6))) 2001390
YD0T(I+5) = (1.0/(XK22-XNUTP**2*XK11))*(YPRED(I+1)-XNUTP*YANTH+ 2001400
K*(XNTHP-XNUTP*XNTH))-YPRED(I+7)*(X1*SAVY(3)+X2* 2001410
SAVY(6)) 2001420
EPSITH = XIR0*(XN*YPRED(I+4))-YPRED(I+6)) 2001430
EPSIPH = YD0T(I+5)+YPRED(I+7)*(X1*SAVY(3)+X2*SAVY(6)) 2001440
YD0T(I+1) = -XN*XIR0*YPRED(I)-XN*YAMPT*XIR0SQ-K*XFPHLD-(EPSITH+ 2001450
EPSIPH)*(X1*XFPHL1+X2*XFPHL2)+YPRED(I+7)*(X1*XFZEL1+ 2001460
X2*XFZEL2) 2001470
YD0T(I+2) = -YANTH*XIR0+XNSQ*YANTH*XIR0SQ-K*(XN*XMPHLD*XIR0- 2001480
XFZELD)-(EPSITH+EPSIPH)*(X1*XFZEL1+X2*XFZEL2)- 2001490
YPRED(I+7)*(X1*XFPHL1+X2*XFPHL2)-XIR0*XN*(YANPT* 2001500
(X1*SAVY(3)+X2*SAVY(6))-YABPH*(X1*SAVY(1)+X2*SAVY(4))) 2001510
YD0T(I+3) = -2.0*XN*YAMPT*XIR0+YAJPH+K*XMTHL 2001520
YD0T(I+6)=YPRED(I+7) 2001530
YD0T(I+7) = (1.0/(XK22-XNUTP**2*XK11))*(-YPRED(I+3)+XNUTP*YANTH+ 2001540
K*(XNUTP*XMTTH-XMTPH)) 2001550
G0 T0 9005 2001560
7786 G0 T0 (4771,4772,4773),ICE0M 2001570
C THE FOLLOWING EQUATIONS ARE THE -STIO- SET 2001580
C EQUATIONS FOR SHELLS OF REVOLUTION ( PHI C00RDINATE ) 2001590
4771 YANTH = XK12*(1.0/(XK22+XK22**2/XD22)))+(YPRED(I+1)+K*XNTPH+ 2001600
(XK22/XD22)*(YPRED(I+3)+K*XMTPH))-K*XNTH+(XIR0*XK11- 2001610
XK12*XK21*XIR0*(1.0/ 2001620
(XK22+XK22**2/XD22)))+(XN*YPRED(I+4)+YPRED(I+5)*CS-YPRED(I+ 2001630
6)*SN)-(XC11+XK12*XK22*XD21/XD22*(1.0/(XK22+XK22**2/XD22))) 2001640
*(XIR0**2*(XN*YPRED(I+4)*SN-XN**2*YPRED(I+6))+YPRED(I+7)*CS* 2001650
XIR0) 2001660
YAMTH = -XD12*(XK22/(XK22**2+XK22*XD22))*(YPRED(I+1)+K*XNTPH) 2001670
-K*XMTTH+XD12*(XK22/(XK22**2+XK22*XD22))*(YPRED(I+3)+ 2001680
K*XMTPH)+(XC11* 2001690
XIR0+XD12*XK21*XIR0*(XK22/(XK22**2+XK22*XD22)))+(XN*YPRED(I 2001700
I+4)+YPRED(I+5)*CS-YPRED(I+6)*SN)+(XD11-XD12*XK22*XD21/( 2001710
XC22**2+XK22*XD22))*(XIR0SQ*(XN*YPRED(I+4)*SN-XNSQ*YPRED 2001720
(I+6))+YPRED(I+7)*CS*XIR0) 2001730
YABPH = XN*YPRED(I+6)*XIR0-YPRED(I+4)*SNIR0 2001740
YAMPT = (-1.0/(X033)+(XNSQ*XIR0/XK33)))*(-2.0*XN* 2001750
YPRED(I+7)+YPRED(I+4)*(CSIR1-CNIR0)+XN*YPRED(I+5)* 2001760
(SNIR0+XIR1)+2.0*XN*YPRED(I+6)*CSIR0+YPRED(I)*SN/ 2001770
XK33+SN*YABPH*(X1*SAVY(3)+X2*SAVY(6))) 2001780
YAJPH = YPRED(I+2)-YPRED(I+1)*(X1*SAVY(3)+X2*SAVY(6)) 2001790
-YPRED(I+7)*(X1*SAVY(2)+X2*SAVY(5)) 2001800
YANPT = YPRED(I+1)+YAMPT*SNIR0 2001810
YD0T(I+4) = R1*(YPRED(I+4)*CSIR0+XN*YPRED(I+5)*XIR0+YPRED(I)/XK33+ 2001820
YAMPT*SNIR0/XK33)+R1*YABPH*(X1*SAVY(3)+X2*SAVY(6)) 2001830
YD0T(I) = R1*(-2.0*YPRED(I+3)*CSIR0+XN*YANTH*XIR0-XN*YANTH*SN+ 2001840
XIR0SQ-YAMPT*CSIR0*(XIR1-SNIR0))-R1*K*(XFTHLD+XMPHLD* 2001850
SNIR0)-(YD0T(I+4)*(X1*XFPHL1+X2*XFPHL2)+R1*YABPH*

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3      (X1*XFZEL1+X2*XFZEL2))-R1*SNIR0*(YA0PH*(X1*SAVY(1)+
4      X2*SAVY(4)))-YANPT*(X1*SAVY(3)+X2*SAVY(6))
YD0T(I+5) = R1*(YPRD(I+6)*XIR1-YPRD(I+7)*(X1*SAVY(3)+X2*SAVY(6))
+1.0/(XK22+XK22**2/XD22))*(YPRD(I+1)*K*XTNTPH+XK22/
X021*(YPRD(I+3)+K*XTNTPH)-XK21*XIR0*(XN*
2001910
YPRD(I+4)+YPRD(I+5)*CS-YPRD(I+6)*SN)-(XK22*X021/XD22
2001920
)*(XIR0SQ*(XN*YPRD(I+4)*SN-XNSQ*YPRD(I+6))+YPRD(I+7)
2001930
*CS*XIR0)))
EPSITH = XIR0*(XN*YPRD(I+4)+YPRD(I+5)*CS-YPRD(I+6)*SN)
2001950
EPSIPH = XIR1*(YD0T(I+5)-YPRD(I+6))+YPRD(I+7)*(X1*SAVY(3)+
2001960
X2*SAVY(6))
2001970
YD0T(I+1) = R1*(CSIR0*(YANTH-YPRD(I+1))-XN*XIR0*(YPRD(I)+
YANPT*(SN*XIR0+XIR1)+YPRD(I+2)*XIR1)-R1*K*XFPHLD
2001980
-R1*(EPSITH+EPSIPH)*(X1*XFPHL1+X2*XFPHL2))-YPRD(I+7)*
2002000
(X1*XFZEL1+X2*XFZEL2))
YD0T(I+2) = R1*(-YPRD(I+2)*CSIR0-YANTH*SNIR0-YPRD(I+1)*XIR1
2002010
+XNSQ*YANTH*XIR0SQ-2.0*XN*YAMPT*CS*XIR0SQ)+R1*K*
2002020
(XN*XMPHLD*XIR0-XFZELD)-R1*(EPSITH+EPSIPH)*(X1*
2002030
XFZEL1+X2*XFZEL2)+YPRD(I+7)*(X1*XFPHL1+X2*XFPHL2))
2002040
-R1*XIR0*XN*(YANPT*(X1*SAVY(3)+X2*SAVY(6))-YA0PH*
2002050
(X1*SAVY(1)+X2*SAVY(4)))
2002060
YD0T(I+3) = R1*(YAMTH*CSIR0-YPRD(I+3)*CSIR0-2.0*XN*YAMPT*XIR0+
2002070
YAJPH+K*XTNTPH)
2002080
YD0T(I+6) = R1*(YPRD(I+7)-YPRD(I+5)*XIR1)
2002090
YD0T(I+7) = R1*(-XK22/(XK22**2+XK22*XD22))*(YPRD(I+1)*K*XTNTPH-
2002100
(XK21/
2002110
R0))*(XN*YPRD(I+4)+YPRD(I+5)*CS-YPRD(I+6)*SN))
2002120
+XK22/(XK22**2+XK22*XD22))*(YPRD(I+3)+K*XTNTPH)-(XK22*
2002130
X021/(XK22**2+XK22*XD22))*(XIR0SQ*(XN*YPRD(I+4)*SN-XNSQ
2002140
*YPRD(I+6))+YPRD(I+7)*CS*XIR0))
2002150
G0 T0 9005
C
EQUATIONS FOR C0NE
4772 YANTH = XK12*(1.0/(XK22+XK22**2/XD22))*(YPRD(I+1)*K*XTNTPH+
(XK22/XD22)*(YPRD(I+3)+K*XTNTPH))-K*XTNTH+(1.0/(CS*S))
1      *(XK11-XK12*XK21)*
2002160
2      1.0/(XK22+XK22**2/XD22))*(XN*YPRD(I+4)+YPRD(I+5)*CS-
2002170
YPRD(I+6)*SN)-(XK11+XK12*X021/XK22/XD22)*(1.0/(XK22+XK22*
2002180
*2/XD22))*(1.0/(S**2*CS**2))*(XN*YPRD(I+4)*SN-XNSQ*YPRD
2002190
(I+6))+YPRD(I+7)/S)
2002200
YANTH = -X012*(XK22/(XK22**2+XK22*XD22))*(YPRD(I+1)*K*XTNTPH)
2002210
-K*XTNTH+X012*(XK22/(XK22**2+XK22*XD22))*(YPRD(I+3)+
2002220
K*XTNTPH)+(XK11/
2002230
(S*CS)*X012*XK21/(S*CS))*(XK22/(XK22**2+XK22*XD22))*(XN*
2002240
YPRD(I+4)+YPRD(I+5)*CS-YPRD(I+6)*SN)+(X011-XD12*XK22*
2002250
X021/(XK22**2+XK22*XD22))*(1.0/(S*CS)**2)*(XN*YPRD(I+4)*
2002260
SN-XNSQ*YPRD(I+6))+YPRD(I+7)/S)
2002270
YA0PH = XN*YPRD(I+6)*XICS/S-YPRD(I+4)*TAN/S
2002280
YAMPT=(-1.0/(S*CS/XD33)+(SN*TN/(XK33*S)))*(-2.0*XN*YPRD(I+7)-
2002290
YPRD(I+4)*SN/S+XN*YPRD(I+5)*TN/S+2.0*XN*YPRD(I+6)/S+YPRD
2002300
(I+1)*SN/XK33+SN*YA0PH*(X1*SAVY(3)+X2*SAVY(6)))
2002310
YAJPH = YPRD(I+7)*(X1*SAVY(1)+X2*SAVY(5))
2002320
-YPRD(I+2)*(X1*SAVY(12)+X2*SAVY(51))
2002330
YANPT = YPRD(I+1)+YAMPT*TAN/S
2002340
YD0T(I+4)=(1.0/S)*(YPRD(I+4)+XN*YPRD(I+5)*XICS+YAMPT*TN/XK33)
2002350
+YPRD(I+1)/XK33+YA0PH*(X1*SAVY(3)+X2*SAVY(6))
2002360
YD0T(I) = -2.0*YPRD(I+1)/S+XN*YANTH*XICS/S-XN*YANTH*SN*XICS**2/S**2
2002370
+YAMPT*TAN/S**2-K*(XFTHLD+XMPHLD*TAN/S)-(YD0T(I+4)*
2002380
(X1*XFPHL1+X2*XFPHL2))+YA0PH*(X1*XFZEL1+X2*XFZEL2))-
2002390
TAN/S*(YA0PH*(X1*SAVY(1)+X2*SAVY(4))-YANPT*(X1*SAVY(3)
2002400
+X2*SAVY(6)))
2002410
YD0T(I+5) = -YPRD(I+7)*(X1*SAVY(3)+X2*SAVY(6)))+(1.0/(XK22+XK22**2
2002420
2002430
2002440
2002450
2002460
2002470

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1  (X0221)*(YPRED(I+1)+K*XNTPH+(XC22/X022))*(YPRED(I+3)) 2002480
1  +K*XNTPH)-(XK21/(S*CS))*(XN*YPRED(I+4)+YPRED(I 2002490
1  I+5)*CS-YPRED(I+6)*SN-(XC22*X021/X022)*(I+1.0/(S**2*CS** 2002500
2  2))*(XN*YPRED(I+6)*SN-XN*SQ*YPRED(I+6))+YPRED(I+7)/S)) 2002510
1  EPSITH = (I+1.0/(S*CS))*(XN*YPRED(I+4)+CS*YPRED(I+5)-SN* 2002520
1  YPRED(I+6)) 2002530
1  EPSIPH = YD0T(I+5)+YPRED(I+7)*(X1*SAVY(3)+X2*SAVY(6)) 2002540
1  YD0T(I+1) = -YPRED(I+1)/S+YANTH/S-XN*YPRED(I)/(S*CS)-XN*YAMPT*SN/ 2002550
1  (S**2*CS**2)-K*XFPHLD-(EPSITH+EPSIPH)*(X1*XFPHL1+X2* 2002560
2  XFPHL2)+YPRED(I+7)*(X1*XFZEL1+X2*XFZEL2) 2002570
1  YD0T(I+2) = -YPRED(I+2)/S-YANTH*TAN/S+XNSQ*YAMTH/(S**2*CS**2) 2002580
1  -2.0*XN*YAMPT/(S**2*CS)+K*(XN*XMPHLD+XICS/S-XFZELD) 2002590
2  -EPSITH+EPSIPH)*(X1*XFZEL1+X2*XFZEL2)-YPRED(I+7)* 2002600
3  (X1*XFPHL1+X2*XFPHL2)-XICS/S*XN*(YAMPT*(X1*SAVY(3)+ 2002610
4  X2*SAVY(6))-YABPH*(X1*SAVY(1)+X2*SAVY(4))) 2002620
1  YD0T(I+3) = YAMTH/S-YPRED(I+3)/S-2.0*XN*YAMPT/(S*CS)+YAJPH+XMTHLD 2002630
1  *K 2002640
1  YD0T(I+6)=YPRED(I+7) 2002650
1  YD0T(I+7) = -(XC22/(XC22**2+XK22*X022))*(YPRED(I+1)+K*XNTPH-XK21* 2002660
1  (XN* 2002670
1  YPRED(I+4)+YPRED(I+5)*CS-YPRED(I+6)*SN)/(S*CS)) 2002680
2  +(XK22/(XC22**2+XK22*X022))*(YPRED(I+3)+K*XNTPH)-(XK22* 2002690
1  X021 2002700
3  /(XC22**2+XK22*X022))*(I+1.0/(S*CS)**2)*(XN*YPRED(I+4)*SN 2002710
4  -XN**2*YPRED(I+6))+YPRED(I+7)/S) 2002720
1  2002730
1  2002740
1  2002750
1  2002760
1  2002770
1  2002780
1  2002790
1  2002800
1  2002810
1  2002820
1  2002830
1  2002840
1  2002850
1  2002860
1  2002870
1  2002880
1  2002890
1  2002900
1  2002910
1  2002920
1  2002930
1  2002940
1  2002950
1  2002960
1  2002970
1  2002980
1  2002990
1  2003000
1  2003010
1  2003020
1  2003030
1  2003040
1  2003050
1  2003060
1  2003070
1  2003080

```

G0 T0 9005
 EQUATIONS FOR CYLINDER
 4773 YANTH

```

2      X2*XFZEL2)
YD0T(I+2) = -YANTH*X1R0+XNSQ*YAMTH*X1R0SQ+K*(XN*XMPHLD*X1R0-
1      XFZEL0)-(EPSITH+EPSIPH)*(X1*XFZEL1+X2*XFZEL2)-
2      YPRED(I+7)*(X1*XFPHL1+X2*XFPHL2)-X1R0*XN*(YAMPT*
3      (X1*SAVY(3)+X2*SAVY(6))-YA0PH*(X1*SAVY(1)+X2*SAVY(4)))
YD0T(I+3) = -2.0*XN*YAMPT*X1R0+YAJPH+K*XNTHLD
YD0T(I+6)=YPRED(I+7)
YD0T(I+7) = -(XC22/(XC22**2+XK22*X022))*(YPRED(I+1)+K*XNTPH-XK21*
1      X1R0*(
1      XN*YPRED(I+4)-YPRED(I+6)))+(XK22/(XC22**2+XK22*X022))*(
2      YPRED(I+3)+K*XNTPH)-(XK22*X021/(XC22**2+XK22*X022))*(
3      X1R0SQ*(XN*YPRED(I+4)-XNSQ*YPRED(I+6)))
9005  IY =8*(M-1)+1
YASAVE(IY) = YANTH
YASAVE(IY+1)=YAMTH
YASAVE(IY+2)=YAMPT
YASAVE(IY+3)=YANPT
YASAVE(IY+4)=YA0PH
YASAVE(IY+7) = YAJPH
RETURN
END

```

2003090
2003100
2003110
2003120
2003130
2003140
2003150
2003160
2003170
2003180
2003190
2003200
2003210
2003220
2003230
2003240
2003250
2003260
2003270
2003280
2003290

2100000

C ***** ** ABACUS UPDATED 07/07/72 *****

2100030

ROUTINE **D20 SUBROUTINE BDE2(XFPHL1,XFZEL1,XFPHL2,XFZEL2)

2100040

INTEGER SAVJTC,SAVSTP,Q,THICK

2100050

DOUBLE PRECISION SAVTIC,TIC,PHI,ST0P,REST0P,RTICK

2100060

DOUBLE PRECISION YPRE

2100070

COMMON ST0RY(16),XMAT(110,10),STD(10),RADUS(30),RADIUS(30)

2100080

COMMON XN,TERR,TIC,PHI,ST0P,REST0P,RTICK,CL,XNL(2),NH

2100090

COMMON NST(30),NKL(30),XNMT(20),SAVJTC(30),SAVSTP(30),JRTIC(30)

2100100

COMMON JRST0P(30),NREG,NMPT,NRC,NSC,NIX,IERR0R,KGE0M,IGE0M,ISTAB

2100110

COMMON KELVIN,IBEGIN,NPR0B,NSEG,NERR0R,Q,THICK,N0JS,NLINKS,NLCASE

2100120

COMMON NTSKL,NZ,NBCT,LINPUT,NTRKL,NPASS,XN1,KBC,NRINGS

2100130

COMMON /LASTEQ/ YPRE(16),YD0T(16),YASAVE(16)

2100140

1 YANTH,YANTH,YAMPT,YAMPT,YANPT,YA0PH,YA0PH,YA0TH,YA0PH,

2 S,SN,CS,SNSQ,CSQ,TAN,SEC,CN,X1CS,X1SN,TN,

3 XIR0,XIR0SQ,X1SNR0,X1CSNR0,CNIR0,SNIR0,CSIR0,

4 XIR1,XIR2,CSIR1,CSIR2,SNIR1,XIRISQ,R2SQ,R0,BESQ,

5 R0SQ,XNSQ,BETA,R1,R2,Z1,RID0T,RISQ,

6 XNTH,XNTPH,XMTTH,XMTPH,XFTHLD,XFPHLD,XFZELD,

7 XNTHLD,XMPHLD,ETHET(2),EPHI(2),XGPT(2),ALPHTH(2),ALPHPH(2),

8 XNUT,XNUPT,XC11,XC22,XC15,XD33,XD22,XD21,XD12,

9 XK11,XK12,XK21,XK22,XK33,X011,

A M,I,SITIN,SIT0T,SIPIN,SIP0T,TPTIN,TPT0T,

B ZBRIN,ZBR0T,SCRIP0,SCRIP1,SIFIN,SIF0T,TZEPH,TZETH

C XNPHI,BETTA,ZETTA,SAVY(8),XC16

2100250

EQUIVALENCE (XNL(1),X1),(XNL(2),X2)

2100260

K = 0

2100270

IF (KBC.EQ.0.AND.NH.EQ.0) K = 1

2100280

G0 T0 (7341,7342,7343),IGE0M

2100340

THE FOLLOWING EQUATIONS ARE THE -RWAF- SET

2100350

EQUATIONS FOR SHELLS OF REVOLUTION (PHI COORDINATE)

2100360

7341 YANTH = (YPRE(1+1)+K*XNTPH)*(XC15*XC22+XD22*XK12)/(XK22*XD22+

2100370

1 XC22**2)-K*XNTH+(XK12*XC22-XK22*XC15)*(YPRE(1+3)+K*XMTPH)/

2100380

2 (XC22*XC22+XD22*XD22)+XIR0*(XN*YPRE(1+4)+YPRE(1+5)*CS-

2100390

3 YPRE(1+6)*SN)*(XK11+(XC15*(XC15*XC22-2.0*XK12*XC22)+

2100400

4 XD22)/(XK22*XD22+XC22*XC22))+(XIR0SQ*(XN*YPRE(1+4)*SN-XNSQ

2100410

5 *YPRE(1+6))+XIR0*YPRE(1+7)*CS)*(-XC11+(XC15*XC15*XC22+

2100420

6 XC15*(XK12*XD22+XK22*XD12)-XK12*XD12*XC22)/(XK22*XD22+XC22*XC22)

2100430

YAMTH = (YPRE(1+3)+K*XMTPH)*(XC15*XC22+XD22*XD12)/(XK22*XD22+

2100440

1 XC22*XC22)+YPRE(1+1)+K*XNTPH)*(XC15*XC15-XD12*XC22)/(XK22*XD22+

2100450

2 XC22**2)-K*XNTH+(XIR0SQ*(XN*YPRE(1+4)*SN-XNSQ*YPRE(1+6))+

2100460

3 XIR0*YPRE(1+7)*CS)*(XC11-(XD12*XD12*XC22+XC15*(2.0*XC22*XD12-

2100470

3 XC15*

2100480

4 XD22)/(XC22*XC22+XD22*XD22))+XIR0*(XN*YPRE(1+4)+YPRE(1+5)*CS-

2100490

5 YPRE(1+6)*SN)*(XC11-(XD12*XD12*XC22+XD12-XC15*(XC15*XC22+XD12*XC22+

2100500

6 XD22*XD12))/(XC22*XC22+XD22*XD22))

2100510

YA0PH = XN*YPRE(1+6)*XIR0-YPRE(1+4)*SNIR0

2100520

YAMPT = (1.0/(XC16*SN*XIR0-XK33-SN*XIR0*(XD33*SN/(R0-XC16))))

2100530

1 *((XC33*XD33-XC16**2)*XIR0*(-2.0*XN*YPRE(1+7)+YPRE(1+4)*

2100540

2 (CS*XIR1-CNIR0)+XN*YPRE(1+5)*(XIR1+SNIR0)+2.0*XN*YPRE

2100550

3 (1+6)*CS*XIR0)+YA0PH*SN*(X1*SAVY(3)+X2*SAVY(6))+YPRE(1+*

2100560

4 (XD33*SN*XIR0-XC16))

2100570

YA0PH = YPRE(1+2)-YPRE(1+1)*(X1*SAVY(3)+X2*SAVY(6))

2100580

-YPRE(1+7)*(X1*SAVY(2)+X2*SAVY(5))

2100590

YANPT = YPRE(1+1)+YAMPT*SNIR0

2100600

YD0T(1+4) = R1*(YPRE(1+4)*CS*XIR0+YA0PH*(X1*SAVY(3)+X2*SAVY(6))

2100610

+XN*YPRE(1+5)*XIR0+(1.0/(XK33-

2100620

1 XC16**2/XD33))*(YPRE(1+1)+YAMPT*(SN*XIR0-XC16/XD33))

2100630

1 YD0T(1) = R1*(-2.0*YPRE(1+1)*CSIR0+XN*YANTH*XIR0-XN*YAMTH*SN*

2100640

```

1 X1R0SQ-YAMPT*CS1R0*(X1R1-SN1R0))-R1*K*(XFTHLD+XMPHLD* 2100650
2 SN1R0)-(YD0T(I+4)*(X1*XFPHL1+X2*XFPHL2)+X1*YABPH* 2100660
3 (X1*XFZEL1+X2*XFZEL2))-R1*SN1R0*(YABPH*(X1*SAVY(1)+ 2100670
4 X2*SAVY(4))-YAMPT*(X1*SAVY(3)+X2*SAVY(6))) 2100680
5 YD0T(I+5) = YPRE(I+6)-R1*YPRE(I+7)*(X1*SAVY(3)+X2*SAVY(6))+R1* 2100690
1 (X022*(YPRE(I+1)+K*XNTPH)+X022*(YPRE(I+3)+K*XMTPH)- 2100700
2 X1R0*(XN*YPRE(I+4)+YPRE(I+5)*CS-YPRE(I+6)*SN)* 2100710
3 (XK12*X022+XC15*X022)-(X1R0SQ*(XN*YPRE(I+4)-XNSQ* 2100720
4 YPRE(I+6))+X1R0*YPRE(I+7)*CS)*(X022*X012-XC15*X022) 2100730
5 /(X022*X022+X022**2) 2100740
EPSITH = X1R0*(XN*YPRE(I+4)+YPRE(I+5)*CS-YPRE(I+6)*SN) 2100750
EPSIPH = X1R1*(YD0T(I+5)-YPRE(I+6))+YPRE(I+7)*(X1*SAVY(3)+ 2100760
X2*SAVY(6)) 2100770
1 YD0T(I+1) = R1*(CS1R0*(YANTH-YPRE(I+1))-XN*X1R0*(YPRE(I+1)+ 2100780
YAMPT*(SN*X1R0+X1R1))+YPRE(I+2)*X1R1)-R1*K*XFPHLD 2100790
2 -R1*(EPSITH+EPSIPH)*(X1*XFPHL1+X2*XFPHL2)-YPRE(I+7)* 2100800
3 (X1*XFZEL1+X2*XFZEL2)) 2100810
1 YD0T(I+2) = R1*(-YPRE(I+2)*CS1R0-YANTH*SN1R0-YPRE(I+1)*X1R1 2100820
+XNSQ*YANTH*X1R0SQ-2.0*XN*YAMPT*CS*X1R0SQ)+R1*K* 2100830
2 (XN*XMPHLD*X1R0-XFZEL0)-R1*(EPSITH+EPSIPH)*(X1* 2100840
3 XFZEL1+X2*XFZEL2)+YPRE(I+7)*(X1*XFPHL1+X2*XFPHL2)) 2100850
4 -R1*X1R0*XN*(YAMPT*(X1*SAVY(3)+X2*SAVY(6))-YABPH* 2100860
5 (X1*SAVY(1)+X2*SAVY(4))) 2100870
1 YD0T(I+3) = R1*(YAMTH*CS1R0-YPRE(I+3)*CS1R0-2.0*XN*YAMPT*X1R0+ 2100880
YABPH+K*XNTHLD) 2100890
1 YD0T(I+6) = R1*(YPRE(I+7)-YPRE(I+5)*X1R1) 2100900
YD0T(I+7) = R1*(XK22*(YPRE(I+3)+K*XMTPH)-X022*(YPRE(I+1)+K* 2100910
XNTH)+X1R0 2100920
1 (XN*YPRE(I+4)+YPRE(I+5)*CS-YPRE(I+6)*SN)*(XK12*X022-XK22*X015) 2100930
2 -(X1R0SQ*(XN*YPRE(I+4)*SN-XNSQ*YPRE(I+6))+X1R0*YPRE(I+7)*CS)* 2100940
3 (X015*X022+XK22*X012))/(X022**2+XK22*X022) 2100950
G0 T0 9005 2100960
C EQUATIONS FOR CONE 2100970
7342 YANTH = (YPRE(I+1)+K*XNTH)*(XK12*X022-XK22*X015)*(X015*X022+X022*XK12)/(XK22*X022+ 2100980
1 X022**2)-K*XNTH*(XK12*X022-XK22*X015)*(YPRE(I+3)+K*XMTPH)/ 2100990
2 (X022*X022-XK22*X022)+(XN*YPRE(I+4)+YPRE(I+5)*CS-YPRE(I+6) 2101000
3 *SN)/(S*CS)*(XK11+X015*(XK15*XK22-2.0*XK12*X022)-XK12*XK12* 2101010
4 X022)/(XK22*X022+XK22*X022))+((XN*YPRE(I+4)*SN-XNSQ* 2101020
5 YPRE(I+6))/(S*S*CS)+YPRE(I+7)/S)*(-X011+(XK15*X015*X022+ 2101030
6 X015*(XK12*X022+XK22*X012)-XK12*X012*X022)/(XK22*X022+X022*XK22)) 2101040
YAMTH = (YPRE(I+3)+K*XNTH)*(X015*X022+XK22*X012)/(XK22*X022+ 2101050
1 X022**2)+(YPRE(I+1)+K*XNTH)*(X022*X015-X012*X022)/(X022*XK22+ 2101060
2 X022**2)-K*XNTH*(X022*X015-X012*X022)/(X022*XK22+ 2101070
3 SN)+YPRE(I+7)/S*(X011-(X012*X012*XK22+X015*(2.0*X022*X012-XC15* 2101080
4 X022))/(X022*X022+XK22*X022))+1.0/(S*CS)*(XN*YPRE(I+4)+ 2101090
5 YPRE(I+5)*CS- 2101100
6 YPRE(I+6)*SN)*(X011+(X012*X022+XK12-XC15*(X015*X022+X012*XK22+ 2101110
X022*XK12))/(X022*X022+XK22*X022)) 2101120
YABPH = XN*YPRE(I+6)*X015/S-YPRE(I+4)*TAN/S 2101130
1 YAMPT = (X016*TAN/S-XK33-(TAN/S)*(X033*TAN/S-XC16))*((-1))*((XK33* 2101140
X033-XC16**2)/(1.0/(S*CS)))*(-2.0*XN*YPRE(I+7)-YPRE(I+4)* 2101150
SN/S)+XN*YPRE(I+5)*TAN/S+2.0*XN*YPRE(I+6)/S)+YABPH*SN* 2101160
3 (X1*SAVY(3)+X2*SAVY(6))+YPRE(I+7)*(X033*TAN/S-XC16)) 2101170
1 YAJPH = YPRE(I+2)-YPRE(I+1)*(X1*SAVY(3)+X2*SAVY(6)) 2101180
-YPRE(I+7)*(X1*SAVY(2)+X2*SAVY(5)) 2101190
2101200
1 YAMPT = YPRE(I+1)+YAMPT*TAN/S 2101210
YD0T(I+4) = YPRE(I+4)/S+YABPH*(X1*SAVY(3)+X2*SAVY(6))+XN* 2101220
YPRE(I+5)/(S*CS)+1.0/(XK33-XC16**2) 2101230
1 X033))*((YPRE(I+1)+YAMPT*(TAN/S-XC16/X033)) 2101240
1 YD0T(I) = -2.0*YPRE(I)/S+XN*YANTH*X015/S-XN*YANTH*SN*X015**2/S**2 2101250
+YAMPT*TAN/S**2-K*(XFTHLD+XMPHLD*TAN/S)-(YD0T(I+4))*

```

C EQUATIONS FOR CONE

```

2      (X1*XFPHL1+X2*XFPHL2)+YA0PH*(X1*XFZEL1+X2*XFZEL2))-
3      TAN/S*(YA0PH*(X1*SAVY(1)+X2*SAVY(4))-YANPT*(X1*SAVY(3)
4      +X2*SAVY(6)))
5      YD0T(I+5) = -YPRED(I+7)*(X1*SAVY(3)+X2*SAVY(6))+(X022*(YPRED(I+1)
6      +K*XMTPH)+XC22*(YPRED(I+3)+K*XMTPH)-(XK12*
7      XD22+XC15*XC22)*(1.0/(S*CS)+X1*XMTPH+X2*XFZEL2))-
8      CS*YPRED(I+6)*SN)-(XC22*XD12-XC15*XD22)*(X1*SAVY(3)+
9      YPRED(I+6)+XN*YPRED(I+4)*SN)/(X1*SAVY(3)+X2*XFZEL2))-
10     /((XK22*XD22+XC22*XC22))
11     EPSITH = (1.0/(S*CS))*(XN*YPRED(I+4)+CS*YPRED(I+5))-SN*
12     YPRED(I+6))
13     EPSIPH = YD0T(I+5)+YPRED(I+7)*(X1*SAVY(3)+X2*SAVY(6))
14     YD0T(I+1) = -YPRED(I+1)/S+YANTH/S-XN*YPRED(I+1)/(S*CS)-XN*YAMPT*SN/
15     (S*CS+X2*XC22)-K*XFPHL2-(EPSITH+EPSIPH)*(X1*XFPHL1+X2*
16     XFPHL2)+YPRED(I+7)*(X1*XFZEL1+X2*XFZEL2)
17     YD0T(I+2) = -YPRED(I+2)/S-YANTH*TAN/S+XNSQ*YAMTH/(S*CS+X2*XC22)
18     -2.0*XN*YAMPT/(S*CS+X2*XC22)+K*(XN*XMTPH+X1*CS/X2*XFZEL2)
19     -(EPSITH+EPSIPH)*(X1*XFZEL1+X2*XFZEL2))-YPRED(I+7)*
20     (X1*XFPHL1+X2*XFPHL2)-X1*CS/X2*XFZEL2)+XN*YAMPT*(X1*SAVY(3)+
21     X2*SAVY(6))-YA0PH*(X1*SAVY(1)+X2*SAVY(4))
22     YD0T(I+3) = YAMTH/S-YPRED(I+3)/S-2.0*XN*YAMPT/(S*CS)+YAJPH+XMTGLD
23     *K
24     YD0T(I+6) = YPRED(I+7)
25     YD0T(I+7) = (XK22*(YPRED(I+3)+K*XMTPH)-XC22*(YPRED(I+1)+K*XMTPH)+
26     (XK12*XC22-XK22*XC15)*(1.0/(S*CS)+XN*YPRED(I+4))+
27     YPRED(I+5)*CS-YPRED(I+6)*SN)-(XC15*XC22+XK22*XD12)*
28     (-XNSQ*YPRED(I+6)+XN*YPRED(I+4)*SN)/(S*CS+X2*XC22)+
29     YPRED(I+7)/S)/(XK22*XD22+XC22*XC22)
30     G0 T0 9005
31     EQUATIONS FOR CYLINDER
32     7343 YANTH = (YPRED(I+1)+K*XMTPH)*(XC15*XC22+X022*XC12)/(XK22*XD22+
33     XC22*XC22)-K*XMTPH+(XK12*XC22-XK22*XC15)*(YPRED(I+3)+K*XMTPH)/
34     (XC22*XC22+XK22*XD22)+X1R0*(XN*YPRED(I+4))-
35     YPRED(I+6))*(XK11+(XC15*(XC15*XC22-2.0*XK12*XC22)-XK12*XC12*
36     XD22)/(XK22*XD22+XC22*XC22))+X1R0SQ*(XN*YPRED(I+4))-XNSQ
37     *YPRED(I+6))
38     XC15*(XK12*XD22+XK22*XD12)-XK12*XD12*XC22)/(XK22*XD22+XC22*XC22))
39     YAMTH = (YPRED(I+3)+K*XMTPH)*(XC15*XC22+XK22*XD12)/(XK22*XD22+
40     XC22*XC22)-K*XMTPH+X1R0SQ*(XN*YPRED(I+4))-XNSQ*YPRED(I+6))
41     *XD11-(XD12*XD12+XK22*XC15*XC22+XK22*XD12)-XC15*
42     XD22)/(XC22*XC22+XK22*XD22)+X1R0*(XN*YPRED(I+4))-
43     YPRED(I+6))*(XC11+(XD12*XC22+XK12-XC15*(XC15*XC22+XD12*XC22+
44     XD22*XC12))/(XC22*XC22+XK22*XD22))
45     YA0PH = X1R0*(XN*YPRED(I+6))-YPRED(I+4))
46     YAMPT = (1/(XC16*X1R0-XK33-X1R0*(XD33*X1R0-XC16)))*(XK33*XD33-XC16
47     *X1R0*(-2.0*XN*YPRED(I+7)+XN*X1R0*YPRED(I+5))+YA0PH*
48     (X1*SAVY(3)+X2*SAVY(6))+YPRED(I+1)*(XD33*X1R0-XC16))
49     = YPRED(I+2)-YPRED(I+1)*(X1*SAVY(3)+X2*SAVY(6))
50     -YPRED(I+7)*(X1*SAVY(2)+X2*SAVY(5))
51     YAJPH = YPRED(I+1)+YAMPT*X1R0
52     YD0T(I+4) = (YA0PH*(X1*SAVY(3)+X2*SAVY(6))+XN*YPRED(I+5)/R0)+
53     (1.0/(XK33-XC16*XD33))*(YPRED(I+1)+
54     YAMPT*(X1R0-XC16/X033))
55     YD0T(I) = XN*YANTH*X1R0-XN*YAMTH*X1R0SQ-K*(XFTHLD+XMPHLD*X1R0)
56     -(YD0T(I+4)*(X1*XFPHL1+X2*XFPHL2)+YA0PH*(X1*XFZEL1+
57     X2*XFZEL2))-X1R0*(YA0PH*(X1*SAVY(1)+X2*SAVY(4))-YANPT*
58     (X1*SAVY(3)+X2*SAVY(6)))
59     YD0T(I+5) = -YPRED(I+7)*(X1*SAVY(3)+X2*SAVY(6))+X022*(YPRED(I+1)
60     +K*XMTPH)+XC22*(YPRED(I+3)+K*XMTPH)-X1R0*
61     (XN*YPRED(I+4))-YPRED(I+6))*(XK12*XD22+XC15*XC22)-X1R0SQ*(XN*YPRED

```

```

2(I+4)-XNSQ*YPRD(I+6))*(XC22*XD12-XC15*X022))/(XK22*X022+XC22**2)
EPSITH = XIR0*(XN*YPRD(I+4)-YPRD(I+6))
EPSIPH = YD0T(I+5)+YPRD(I+7)*(X1*SAYV(3)+X2*SAYV(6))
-YD0T(I+1) = -XN*XIR0*YPRD(I)-XN*YAMPT*XIR0SQ-K*XFPHLD-(EPSITH+
1 EPSIPH)*(X1*XFPHL1+X2*XFPHL2)+YPRD(I+7)*(X1*XFZEL1+
2 X2*XFZEL2)
YD0T(I+2) = -YANTH*XIR0*XNSQ*YAMTH*XIR0SQ+K*(XN*XMPHLD*XIR0-
1 XFZELD)-(EPSITH+EPSIPH)*(X1*XFZEL1+X2*XFZEL2)-
2 YPRD(I+7)*(X1*XFPHL1+X2*XFPHL2)-XIR0*XN*(YANPT+
3 (X1*SAYV(3)+X2*SAYV(6))-YA0PH*(X1*SAYV(1)+X2*SAYV(4)))
YD0T(I+3) = -2.0*XN*YAMPT*XIR0+YAJPH*K*XMTHLD
YD0T(I+6)=YPRD(I+7)
YD0T(I+7) = (XK22*(YPRD(I+3)+K*XNTPH)-XC22*(YPRD(I+1)+K*XNTPH)
1 +XIR0*
2 1(XN*YPRD(I+4)-YPRD(I+6))*(XK12*XC22-XK22*XC15)-XIR0SQ*(XN*YPRD
2(I+4)-XNSQ*YPRD(I+6))*(XC15*XC22+XK22*XD12))/(XC22**2+XK22*XD22)
9005 IV=8*(M-1)+1
YASAVE(IY) = YANTH
YASAVE(IY+1)=YANTH
YASAVE(IY+2)=YANPT
YASAVE(IY+3)=YANPT
YASAVE(IY+4)=YA0PH
YASAVE(IY+7) = YAJPH
RETURN
END

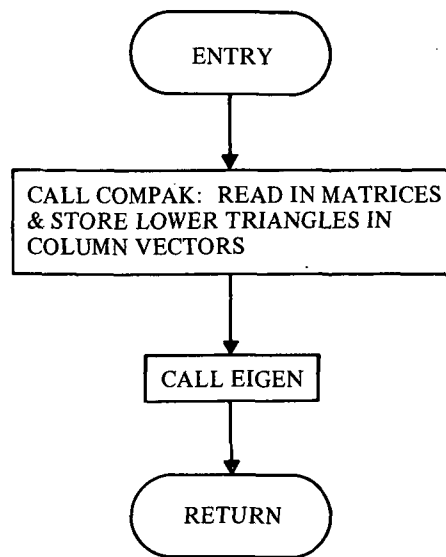
```

SUBROUTINE EIGVAL

This is the controlling routine for the program eigenvalue calculation loop. The necessary matrices for the calculations are passed to COMPAK, and thence to routine EIGEN. The controlling routine EIGVAL will provide intermediate matrix print as desired.

Subroutine COMPAK: This routine reads rows of a two-dimensional array from a storage unit into core and then stores them into a column vector.

EIGVAL



```

C ..... ROUTINE ** EIGVAL ** ABACUS UPDATED 07/24/72 .....
SUBROUTINE EIGVAL (CONV,EIG,N,IBEGIN,QVEC)
DIMENSION A(8400),B(8300),Q(1024),QVEC(128,1)
REWIND 4
KEND 11
CALL COMPACT (4,N,A)
CALL COMPACT (11,N,B)
INDEX = (N*N+N)/2
IF (IBEGIN.EQ.0) GO TO 50
M = 1
WRITE(6,21)
21 FORMAT(1H1,- LIVE LOAD PRESTRESS STIFFNESS MATRIX-)
DO 20 J=1,N
K = M+J-1
WRITE(6,22) J,(A(I),I=M,K)
22 FORMAT(15,1P8E15.6/(5X,1P8E15.6))
20 M = K+1
M = 1
WRITE(6,31)
31 FORMAT(1H1,- DEAD LOAD PRESTRESS OR BASE STIFFNESS MATRIX-)
DO 30 J=1,N
K = M+J-1
WRITE(6,22) J,(B(I),I=M,K)
30 M = K+1
50 CONTINUE
DO 10 J=1,INDEX
10 A(J) = -(A(J)-B(J))
CALL EIGEN(A,B,CONV,Q,EIG,QVEC)
RETURN
END
3400000
3400010
3400030
3400031
3400040
3400050
3400060
3400070
3400080
3400090
3400110
3400120
3400130
3400140
3400150
3400160
3400170
3400190
3400200
3400210
3400220
3400230
3400240
3400250
3400290
3400300

```

```

C ..... ROUTINE ** COMPAK ** ABACUS UPDATED 05/20/72 .....
SUBROUTINE COMPAK (NTAPE,IR0M,C)
  DIMENSION C(1),X(128)
  M = 1
  DO 10 J=1,IR0M
    READ(NTAPE) (X(I),I=1,IR0M)
    DO 20 L=1,J
      C(M) = X(L)
      20 M = M+1
  10 CONTINUE
  RETURN
  END

```

```

3500000
3500010
3500020
3500030
3500040
3500050
3500060
3500070
3500080
3500090
3500100
3500110

```

SUBROUTINE EIGEN

EIGEN is the main eigenvalue and eigenvector calculation routine. Printout of the eigenvalues and appropriate eigenvectors is provided by this routine. First EIGEN prepares the matrices for eigenvalue extraction, calling FUTILE, DAGGER, and SWITCH. Then the matrices are passed to SYMEIG, which obtains the eigenvalues and specified vectors using the Householder technique.

Subroutine DAGGER: This routine performs the reduction of the two matrix eigenvalue problem to a standard eigenvalue problem.

Subroutine SYMEIG (Alternate entry point SYMVEC): This routine obtains the eigenvalues and vectors of a real, symmetric, matrix.

Subroutine TFORM: This routine performs the Householder similarity reduction of a real, symmetric matrix to tri-diagonal form.

Subroutine STURM: Performs the Sturm-sequence calculations of eigenvalues of a real, symmetric, tri-diagonal matrix.

Subroutine PREP (alternate entry point DET): Determines the number of roots greater or equal to a stipulated value.

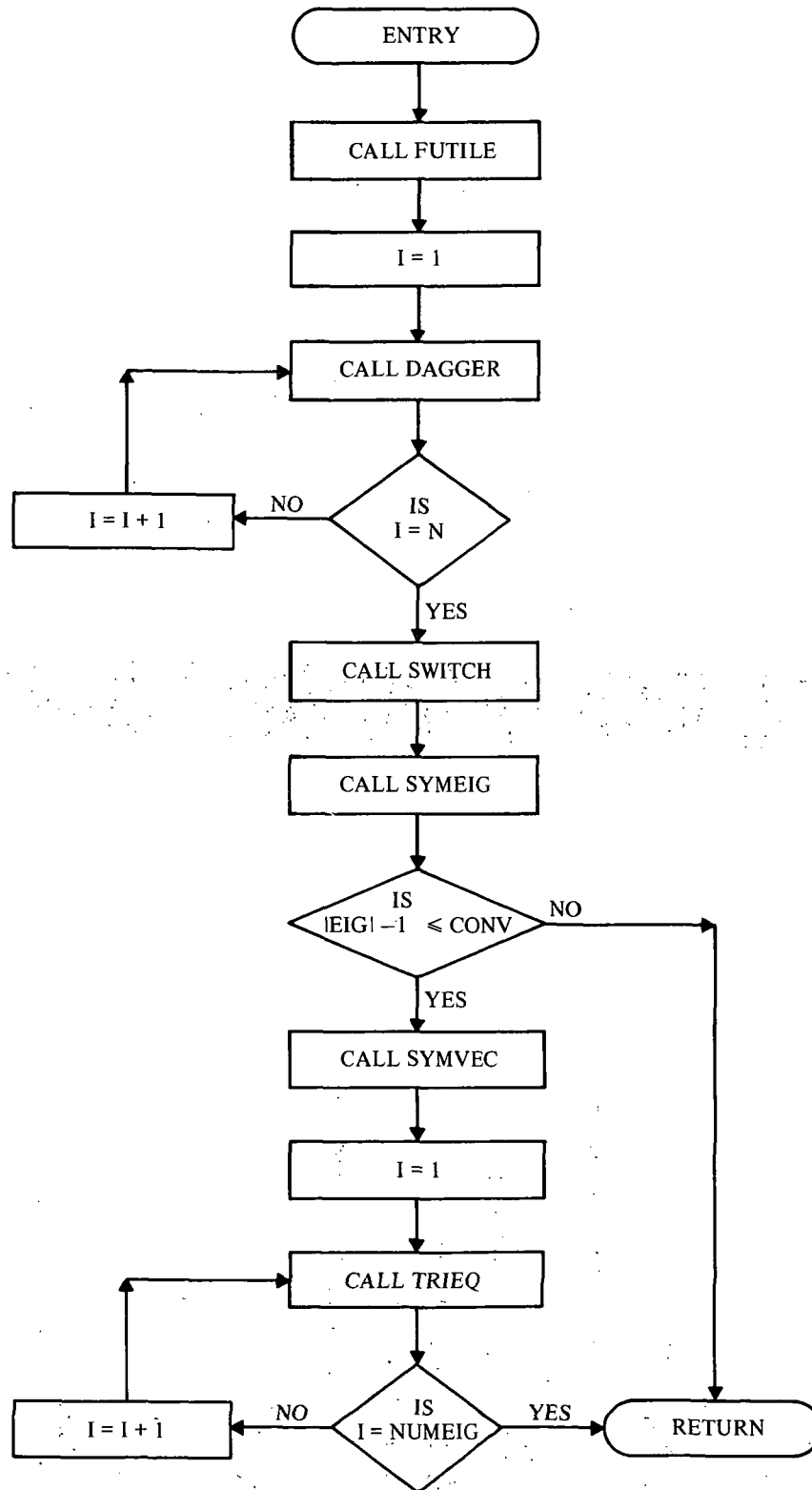
Subroutine QSVEC (alternate entry point QWIEL): Obtains eigenvectors of a tri-diagonal matrix and back transforms them to eigenvectors of the original real, symmetric matrix.

Subroutine RANDOM: Random number generator. This subroutine is an MSFC system subroutine and the listing is not included here. Most any random number generator may be substituted or the argument may be set to zero.

Subroutine ANDD: This routine "ands" or "ors" the corresponding bits of two given variables with each other.

Subroutine DOTPRO: Performs inner product accumulation using labeled common area INFO.

EIGEN



```

C *** ROUTINE ** EIGEN ** ABACUS UPDATED 07/19/72 *****
C SUBROUTINE EIGEN(M,A,B,C,NV,Q,ETG,QVEC)
C SOLVE THE EIGENVALUE PROBLEM
C
C      (A)(X)=(C)B(QA)(Q)(X)
C
C      DIMENSION A(1),Q(1),B(1)
C      DIMENSION C(128),QVEC(128,1)
C      COMMON /WINTER/INDIC8
C      COMMON /BAND/M,L
C      REWIND 4
C      INDIC8=-1
C      M=N
C      L=1
C      TOL = 0.1E-7
C      NUMEIG = N
C      INDEX=(N*N-N)/2+1
C      INDEX1=INDEX-1
C      NIX = 0
C
C FORM CHOLSKY DECOMPOSITION OF B MATRIX
C
C      CALL FUTILE (B,N,NIX)
C      IF(NIX)2,3,4
C      2 WRITE(6,41)
C      41 FORMAT(' B IS NOT POSITIVE DEFINITE-')
C      RETURN
C      4 WRITE(6,42)
C      42 FORMAT(' OVERFLOW IN FUTURE-')
C
C      L-MATRIX STORED IN B
C
C FORM A-MATRIX COLUMN INVERSES - STORE IN Q
C
C      3 IOFF=1
C      DO 10 I=1,N
C      J2 = IOFF+I-1
C      K = 1
C      DO 1 J=IOFF,J2
C      Q(K) = B(J)
C      1 K = K+1
C      WRITE(4) (Q(J),J=1,I)
C      IOFF = IOFF+I
C      X=-Q(I)
C      Q(I)=-1.
C      DO 20 J=1,I
C      20 Q(J)=Q(J)/X
C      10 CALL DAGGER(A,N,Q,I,A(INDEX))
C
C STORE (L)(A)(L-TRANSPOSE) IN A FORM SUITABLE FOR SYMEIG
C WHERE L IS THE INVERSE OF THE CHOLSKY MATRIX
C
C      CALL SWITCH(A,N)
C      CALL SYMEIG(A,N,1,NUMEIG,Q,TOL)
C      DO 300 I=1,NUMEIG
C      300 C(I) = 1.0/Q(I)
C      WRITE(6,56) (C(I),I=1,NUMEIG)
C      56 FORMAT('////- EIGENVALUES-/(1P8E15.6)')
C

```

```

C      EIGENVALUES ARE IN Q
C
      EIG = C(1)
      IF (ABS(ABS(EIG)-1.0).GT.C0NV) GO TO 99
      NUMEIG=2
      DO 30 I=1,NUMEIG
      CALL SYMVEC (A(INDEX),I,1,N)
      IN=INDEX1*N
      WRITE(4)(A(IND),IND=INDEX,IN)
30 CONTINUE
      REMIND 4
      I0FF=1
      DO 40 I=1,N
      J2=I0FF+I-1
      READ(4)(A(I),J=I0FF,J2)
40 I0FF=I0FF+1
      DO 50 I=1,NUMEIG
      READ(4)(Q(I),J=1,N)
      CALL TRIEQ (A,Q)
      WRITE(6,57)I,Q(IJ),IJ=1,N)
57 FORMAT(/- EIGENVECTOR-,I4/(1P8E15.6))
      DO 70 IJ=1,N
70 QVEC(IJ,I)=Q(IJ)
50 CONTINUE
99 RETURN
      END
3600610
3600620
3600630
3600640

3600670

3600720
3600730
3600740
3600750
3600760
3600780

3600790
3600800
3600810

3600820
3600830
3600840

```

```

C ..... RØUTINE ** DAGGER ** ABACUS UPDATED 07/19/72 .....
SUBROUTINE DAGGER(A,M,P,K0,Q)
DIMENSION A(1),P(1),Q(1)
EQUIVALENCE (SUM,SUM)
K = K0
K1 = K + 1
L = 1
LL = 0
INDEX = 1
DØ 130 I = 2,K1
LJ = INDEX
SUM = 0.
DØ 90 J = 1,L
SUM = SUM + A(LJ)*P(J)
90 LJ = LJ + 1
IF (K - LJ) 100,120,100
100 LL = LL + L
LJ = LL + L
DØ 110 J = 1,K
SUM = SUM + A(LJ)*P(J)
110 LJ = LJ + J
120 Q(I-1) = SUM
INDEX = INDEX + L
130 L = I
SUM = 0.
DØ 140 I = 1,K
SUM = SUM + P(I)*Q(I)
A(LL+1) = Q(I)
140 LL = LL + 1
A(LL) = SUM
IF (M - K) 150, 200, 150
150 DØ 190 L = K1,M
LJ = LL+L-K
SUM = 0.
DØ 180 J = 1,K
SUM = SUM + P(J)*A(JL)
180 JL = JL + 1
LL = LL + L - 1
190 A(LL) = SUM
200 CONTINUE
RETURN
END

```

```

4500000
4500010
4500020
4500030
4500040
4500050
4500060
4500070
4500080
4500090
4500100
4500110
4500120
4500130
4500140
4500150
4500160
4500170
4500180
4500190
4500200
4500210
4500220
4500230
4500240
4500250
4500260
4500270
4500280
4500290
4500300
4500310
4500320
4500330
4500340
4500350
4500360
4500370
4500380
4500390
4500400
4500410

```



```

C ..... ROUTINE ** SYMEIG ** ABACUS UPDATED 05/20/72 .....
C SUBROUTINE SYMEIG(M,INDEX,NUMBR,R,TOL)
C MASTER ROUTINE FOR EIGENVALUES AND (OPTIONALLY) EIGENVECTORS OF A
C REAL SYMMETRIC MATRIX STORED TRIANGULARLY IN CORE. THE HOUSEHOLDER
C REDUCTION TO TRIANGULAR FORM (SUBROUTINE TF0RM) IS FOLLOWED BY A
C BISECTION TECHNIQUE (SUBROUTINE STURM) FOR THE ROOTS AND THEN IN-
C VERSE ITERATION (SUBROUTINE TRIVEC) FOR THE VECTORS.
C
C MEANING OF THE PARAMETERS.
C A - THE TRIANGULAR ARRAY CONTAINING THE MATRIX. DURING EXEC-
C CUTION THE ARRAY IS CHANGED.
C M - ORDER OF A.
C INDEX - INDEX OF FIRST EIGENVALUE REQUIRED.
C NUMBR - NUMBER OF EIGENVALUES REQUIRED.
C R - REAL ARRAY FOR THE ROOTS AND WORKING STORAGE. R MUST CON-
C TAIN AT LEAST 8*M WORDS AND START ON A D.P. BOUNDARY.
C TOL - TOLERANCE. IF B IS THE MAG. OF LARGEST ROOT, THE ROOTS
C WILL USUALLY HAVE ERRORS AS LARGE AS B*TOL.
C
C DIMENSION A(1),R(1)
C LD = 1 + M
C LQ = LD + M
C LS = LQ + M
C LP = LS + M
C LQ = LP + M
C LR = LQ + M
C CALL TF0RM(A,M,R(LD),R(LQ),R(LS),R(LP))
C EPS = AMINI(TOL,1.E-3)
C CALL STURM(M,INDEX,NUMBR,R(LD),R(LQ),R(LS),R(LP),R,EPS)
C RETURN
C ENTRY SYMVEC(X,LQW,KOUNT,MID)
C DIMENSION X(MID,1)
C CALL OSVEC(A,R(LD),R(LQ),R(LP),R(LQ),R(LQ),R(LR),R(LS),M)
C ROOT = R(LS-1)
C EPS = ROOT * 3.E-7
C K = LQW
C DO 200 I = 1,KOUNT
C ROOT = AMINI(ROOT-EPS,R(K))
C CALL OMIEL(ROOT,X(1,I))
C 200 K = K + 1
C RETURN
C END

```

```

C ..... ROUTINE ** TFØRM ** ABACUS UPDATED 05/20/72 .....
SUBROUTINE TFØRM(A,N,D,Ø,S,P)
DIMENSION A(1),D(1),Ø(1),S(1)
BL = 0.
HU = 0.
ØLD = 0.
D(1) = A(1)
KIK1 = 1
N1 = N - 1
DØ 230 K = 1,N1
KPI = K + 1
KK = KIK1
KKPI = KK + 1
NK = N - K
KN = KK + NK
KIK1 = KN + 1
SUM = 0.
DØ 100 KJ = KKPI,KN
100 SUM = SUM + A(KJ)*A(KJ)
S(K) = SUM
RHØ = Sqrt(SUM)
RAD = ØLD + RHØ
HL = AMINI(BL,D(K)-RAD)
HU = AMAXI(BU,D(K)+RAD)
IF (K - N1) 120,230,230
120 ØLD = RHØ
IF (A(KKPI)) 140,140,130
130 RHØ = -RHØ
140 Ø(K) = RHØ
IF (SUM) 150,230,150
150 A(KKPI) = A(KKPI) - RHØ
RHØ = 1. / (RHØ*A(KKPI))
A(KK) = RHØ
IJ = KK
DØ 160 J = KPI,N
IJ = IJ + 1
Ø(J) = A(IJ)
160 D(IJ) = 0.
II = KIK1
NI = NK
DØ 190 I = KPI,N
D(I) = D(I) + A(II)*Ø(II)
IJ = II
II = II + NI
NI = NI - 1
IF (NI) 170,190,170
170 X = Ø(II)
DØ 180 J = I,N1
IJ = IJ + 1
D(J+1) = D(J+1) + A(IJ)*X
180 D(I) = D(I) + A(IJ)*Ø(J+1)
190 D(I) = D(I) * RHØ
SUM = 0.
DØ 200 I = KPI,N
200 SUM = SUM + D(I)*Ø(I)
TAU = RHØ * SUM * .5
DØ 210 I = KPI,N
210 D(I) = D(I) + TAU*Ø(I)
II = KIK1
NI = NK

```

```

D0 220 I = KPI,N
RH0 = 0(I)
TAU = 0(I)
IJ = II
II = II + NI
NI = NI - 1
D0 220 J = I,N
A(IJ) = A(IJ) + RH0*0(J) + TAU*0(J)
220 IJ = IJ + 1
230 0(K+1) = A(KIK1)
0(N1) = A(KKP1)
0(N) = AMIN1(BL,DIN)-RH0
S(N) = AMAX1(BU,DIN)+RH0
RETURN
END

```

```

3900600
3900610
3900620
3900630
3900640
3900650
3900660
3900670
3900680
3900690
3900700
3900710
3900720
3900730
3900740

```

```

C ..... ROUTINE ** STURM ** ABACUS UPDATED 05/20/72 .....
SUBROUTINE STURM (N,LIM1,NUMB,D,OFFD,SEC,PFFD,SIGMA,EPS)
DIMENSION D(1),OFFD(1),SEC(1),SIGMA(1),PFFD(1)
DATA HALF / .5/
BL = OFFD(N)
BU = SEC(N)
LIM2 = LIM1 + NUMB - 1
CALL PREP (N,D,SEC,R00T,L0RD)
N1 = N - 1
IF (N1) 16,200,200
200 T0L = AMAX1(-BL,BU)
OFFD(N) = T0L
T0L = T0L * AMAX1(1.E-15,EPS)
D0 2 I = LIM1,LIM2
SIGMA(I) = BL
2 PFFD(I) = BU
L0RD = Q
L = LIM1 - 1
RUTE = 1.E20
G0 T0 3
300 D0 400 I = K,L
400 SIGMA(I) = R00T
3 K = L + 1
IF (K - LIM2) 4,4,16
4 RU = PFFD(K)
R00T = BU + HALF * (SIGMA(K) - BU)
IF (K - L) 5,7,5
5 D0 6 I = K,LIM2
IF (BU - PFFD(I)) 7,6,7
6 L = I
7 IF (ABS(R00T - RUTE) - T0L) 300,300,8
8 CALL DET (N,D,SEC,R00T,L0RD)
D0 11 I = K,L
IF (I - L0RD) 9,9,10
9 SIGMA(I) = R00T
G0 T0 11
10 PFFD(I) = R00T
11 CONTINUE
RUTE = R00T
G0 T0 4
16 RETURN
END

```

```

END OF FILE
C ..... ROUTINE ** PREP ** ABACUS UPDATED 05/20/72 .....
SUBROUTINE PREP (N,D,SEC,R00T,L0RD)
  DIMENSION D(1),SEC(1)
  EQUIVALENCE (RD2,RE2),(RD4,RE4)
  N1 = N - 1
  GO TO 200
  ENTRY DET (N,D,SEC,R00T,L0RD)
  R00 = R00T
  L0W = 0
  LAWD = 0
  100 RD2 = 0.00
  RD4 = 1.00
  DO 120 I = L0W,N1
    RD4 = D(I+1) - RD0 - RD2
    IF (RD4) 120,140,110
  110 LAWD = LAWD + 1
  120 RE2 = SEC(I+1) / RE4
  130 L0RD = LAWD
  GO TO 200
  140 LAWD = LAWD + 1
  IF (RE2) 150,160,150
  150 I = I + 1
  160 L0W = I + 1
  IF (L0W - N1) 100,100,130
  200 RETURN
  END

```

```

4100000
4100020
4100030
4100040
4100050

4100070
4100080
4100090
4100100
4100110
4100120
4100130
4100140
4100150
4100160
4100170
4100180
4100190
4100200
4100210
4100220
4100230
4100240
4100250

```

```

C ..... ROUTINE ** QSVEC ** ABACUS UPDATED 05/20/72 .....
C SUBROUTINE QSVEC(A,D,OFFD,P,Q,R,S,N)
C SYMMETRIC MATRIX EIGENVECTOR CALCULATION.
C GIVEN THE ENTRIES (D AND OFFD) OF THE HOUSEHOLDER TRI-DIAGONAL FORM B
C OF A REAL SYMMETRIC MATRIX A, AND GIVEN A G000 APPROXIMATE ROOT OF
C B (AND A) THIS FORTRAN 4 SUBROUTINE COMPUTES A UNIT EIGENVECTOR X
C OF B. THEN TRANSFORMS IT TO A UNIT VECTOR OF A, USING THE VECTORS W
C STORED IN THE A ARRAY.
C DIMENSION A(1),D(1),OFFD(1),P(1),Q(1),R(1),S(1),X(1)
C DOUBLE PRECISION SUM
C COMMON /INER/ SUM,M,IX,IA
C DATA FLAG/0777777777776/

C PART 1. PRELIMINARIES.
C
IX = 1
IA = 1
N1 = N - 1
N2 = N - 2
RETURN
ENTRY QWEL(R00T,X)
ASSIGN 170 TO KOUNT
TOL = 0.
DO 100 I = 1,N
P(I) = D(I) - R00T
Q(I) = OFFD(I)
R(I) = 0.
TOL = AMAX1(TOL,ABS(D(I)))
CALL RANDOM (XX)
100 X(I) = XX+.1
TOL = (TOL + 1.E-15) * 1.E-15

C PART 2. MATRIX DECOMPOSITION.
C
DO 150 I = 1,N1
T = ABS (P(I))
U = ABS (OFFD(I))
IF (T + U - TOL) 110,120,120
110 P(I) = TOL
T = P(I)
120 IF (T - U) 130,140,140
130 S(I) = P(I)/OFFD(I)
CALL ANDD (S(I),1,S(I),1)
TEMP = Q(I)
P(I) = OFFD(I)
Q(I) = P(I+1)
R(I) = Q(I+1)
P(I+1) = TEMP - S(I)*Q(I)
Q(I+1) = -S(I)*R(I)
GO TO 150
140 S(I) = OFFD(I)/P(I)
CALL ANDD (S(I),FLAG,S(I),0)
P(I+1) = P(I+1) - S(I)*Q(I)
150 CONTINUE
IF (ABS(P(N)) .LT. TOL) P(N) = TOL
GO TO 210

C PART 3. RIGHT SIDE MODIFICATION.
C
170 ASSIGN 330 TO KOUNT

```

```

DØ 200 I = 1,N1
CALL ANDD (S(I),1,TEMP,0)
IF (TEMP) 180,190,180
180 I = X(I)
X(I) = X(I+1)
X(I+1) = T - S(I)*X(I)
GØ TØ 200
190 X(I+1) = X(I+1) - S(I)*X(I)
200 CONTINUE
C
C PART 4. TRIANGULAR SYSTEM SOLUTION.
C
210 X(N) = X(N)/P(N)
X(N1) = (X(N1) - Q(N1)*X(N)) / P(N1)
DØ 220 I = 2,N1
K = N - I
220 X(K) = (X(K) - Q(K)*X(K+1) - R(K)*X(K+2)) / P(K)
C
C PART 5. SCALING TØ UNIT VECTOR.
C
230 SUM = 0.00
M = N
CALL DØTPRØ (X,X)
SCALAR = DSQRT(SUM)
DØ 250 I = 1,N
250 X(I) = X(I)/SCALAR
GØ TØ KØUNT, (170,330,370)
C
C PART 6. TRANSFORMATION BY ØRTHØGØNAL MATRICES.
C
330 L = (N*(N+1))/2 - 4
DØ 360 I = 1,N2
N1 = N - I
SUM = 0.00
M = I + 1
CALL DØTPRØ (X(N1),A(L))
SCALAR = A(L-I)*SUM
IJ = L
DØ 350 J=N1,N
X(J) = X(I) + SCALAR*A(IJ)
350 IJ = IJ + 1
360 L = L - I - 3
ASSIGN 370 TØ KØUNT
GØ TØ 230
370 RETURN
END

```

```

SUBROUTINE ANDD (X,Y,Z,IFLAG)
  LOGICAL UND,JA,NEIN
  REAL N0
  EQUIVALENCE (UND,E),(JA,SI),(NEIN,N0)
  1 SI = X
  N0 = Y
  UND = JA.AND.NEIN
  IF (IFLAG.EQ.1) UND = JA.OR.NEIN
  Z = E
  RETURN
END

```



```

C ..... ROUTINE ** D0TPR0 ** ABACUS UPDATED 05/20/72 .....
SUBROUTINE D0TPR0 (X,Y)
  DIMENSION X(1),Y(1)
  DOUBLE PRECISION S
  COMMON /INFO/ S,N,IX,IY
  IF (N) 120,120,100
100 JX = 1
   JY = 1
   DO 110 J = 1,N
     S = S + X(JX)*Y(JY)
     JX = JX + 1X
110 JY = JY + 1Y
120 RETURN
      END

```

```

3700000
3700010
3700020
3700030
3700040
3700050
3700060
3700070
3700080
3700090
3700100
3700110
3700120
3700140

```

SUBROUTINE DETERM

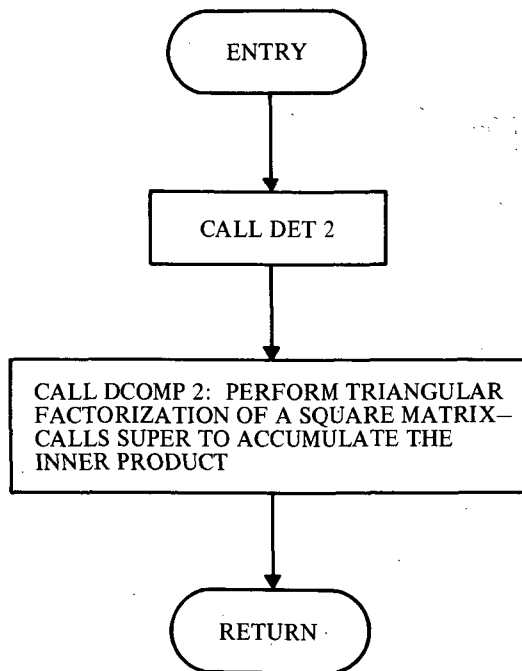
This is the controlling routine for the program determinant evaluation loop. The matrix in question is passed to DET2 where the determinant evaluation calculations occur.

Subroutine DET2: This routine computes the determinant of a square matrix. The actual determinant value is normalized to ± 1 .

Subroutine DCOMP2: This routine performs the triangular factorization of a square matrix.

Subroutine SUPER: This routine performs inner product accumulation.

DETERM



```

SUBROUTINE DETERM (NZ,MDET)
  DIMENSION A(128,128),T(256)
  REWIND 4
  DO 187 I=1,NZ
    187 READ(4) (A(I,J),J=1,NZ)
    CALL DET2 (A,NZ,128,T,NU,D)
    WRITE(6,80) D
    80 FORMAT(///20X,-DETERMINANT =-,F5.1)
    MDET = D
  REWIND 4
  RETURN
END

```



```

SUBROUTINE DCOMP2(A,M,MID,LEAD,ENT,NIX)
INTEGER*2 LEAD
TRIANGULAR DECOMPOSITION OF A SPARSE IN-CORE MATRIX.
DOUBLE PRECISION S
DIMENSION A(1), LEAD(1), ENT(1)
DATA MONE / -1 /
EQUIVALENCE (EL,L)
NIX = 0
EPS = 1.E-6
MPI = M + 1
MMID = M * MID
MM = MMID + M - MID
DO 130 I = 1,M
DO 100 IJ = I,MM,MID
IF (A(IJ)) 110,100,110
100 CONTINUE
IF LOOP FALLS THROUGH, ROW I IS ZERO AND A IS SINGULAR.
NIX = -(1000 + 1)
GO TO 999
110 LEAD(I) = (IJ - I) / MID + 1
LEAD(I) IS THE COLUMN INDEX OF 1ST NON-ZERO ENTRY OF ROW I.
G = 0.
DO 120 KJ = IJ,MM,MID
120 G = ABS( A(KJ) ) + G
130 ENT(I) = 16. / G
KB = 1
MK = M
LAST = 0
KK = 1
C MAJOR LOOP. COLUMN K OF A IS USED TO PRODUCE COLUMN K OF L AND
C U. ABOVE DIAGONAL, A ELEMENTS CONVERT TO U ELEMENTS. AFTER
C PIVOT SELECTION (USING PARTIAL PIVOTING WITH IMPLICIT ROW
C SCALING), THE U(K,K) AND L(I,K) ELEMENTS ARE COMPUTED. AN
C ATTEMPT IS MADE TO SUPPRESS TRIVIAL OPERATIONS BY SKIPPING THE
C LEADING ZERO TERMS IN EACH INNER PRODUCT. SUPER DOES THE INNER
C PRODUCT ACCUMULATION AND IS AVAILABLE IN FORTRAN AND (360)
C ASSEMBLY LANGUAGE.
DO 310 K=L,M
DO 140 JK = KB,MK
IF (A(JK)) 150,140,150
140 CONTINUE
IF LOOP FALLS THROUGH, COLUMN K IS ZERO AND A IS SINGULAR.
GO TO 998
150 LOK = JK
LW = JK - KB + 1
JK = MK
DO 160 J = 1,M
IF (A(JK)) 170,160,170
160 JK = JK + MONE
LOOP CAN-T FALL THROUGH.
170 LAST = MAX(1,MP1-J)
LASTK = KB + LAST - 1
FIRST K COLUMNS CONTAIN ALL ZEROS BELOW ROW LAST.
JK = LOK
LIMIT = 0
G = U.
DO 180 I = LW, LAST
G = AMAX1(G, ENT(I)*ABS(A(IK)))

```

```

180 IK = IK + 1
    TOL = G * EPS
    IK = LOMK
    TOP = 0.
    DO 230 I = LOM, LAST
        LEAST = LEAD(I)
        LEAST = MAXO(LEAST, LOM)
        CALL SUPER (A(I), A(KB), LEAST, LIMIT, MID, S)
        A(IK) = S + A(IK)
        IF(I - K) 200, 210, 210
    200 LIMIT = I
        GO TO 230
    210 G = ABS(A(IK)) * ENT(I)
    IF (TOP - G) 220, 230, 230
    220 TOP = G
        L = I
    230 IK = IK + 1
    IF (TOP - TOL) 998, 240, 240
    240 G = ENT(L)
        ENT(L) = ENT(K)
        ENT(K) = G
        IF (L - K) 250, 270, 250
    250 LEED = LEAD(K)
        KLEED = LEAD(L)
        LEED = MINO(LEED, KLEED)
        KLEED = (LEED - 1) * MID + K
        LJ = KLEED + L - K
    DO 260 KJ = KLEED, MM, MID
        TOP = A(KJ)
        A(KJ) = A(LJ)
        A(LJ) = TOP
    260 LJ = LJ + MID
        J = LEAD(L)
        LEAD(L) = LEAD(K)
        LEAD(K) = J
        NIX = 1 - NIX
    270 KK1 = KK + 1
        LEAD(M+K) = L
        IF (KK1 - LASTK) 280, 280, 300
    280 G = -A(KK)
    DO 290 IK = KK1, LASTK
    290 A(IK) = A(IK) / G
    300 KB = KB + MID
        MK = MK + MID
    310 KK = KB + K
        GO TO 999
    998 NIX = -K
    999 RETURN
        END

```

```

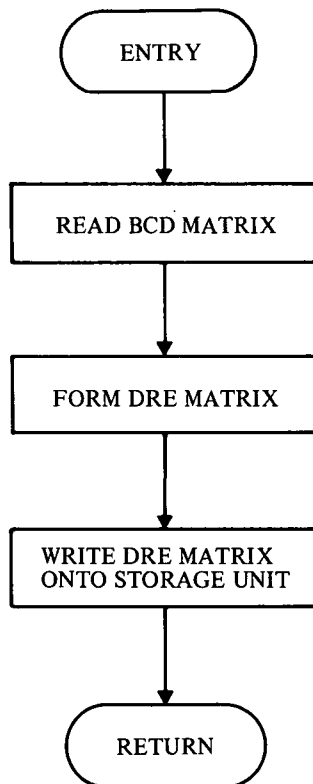
SUBROUTINE SUPER (X,Y,LEAST,LIMIT,MID,S)
DIMENSION X(1), Y(1)
DOUBLE PRECISION S
S = 0.000
IF (LEAST - LIMIT) 100,100,120
100 IX = (LEAST - 1) * MID + 1
DO 110 I = LEAST,LIMIT
S = S + X(IX)*Y(I)
110 IX = IX + MID
120 RETURN
END

```


SUBROUTINE BCVECT

This routine converts the eigenvector obtained during a converged eigenvalue pass into the form accepted by INITIAL. The calculations are identical to those in the latter part of STRMAT, and result in the DRE array.

BCVECT



```

66 ..... ROUTINE ** BCVECT ** ABACUS UPDATED 07/24/72 .....
SUBROUTINE BCVECT (NZ,QVEC,NØJS,JRTIC,JRSTØP,NREG)
DIMENSION QVEC(128,1),BCD(128,128),JRTIC(1),JRSTØP(1),DRE(128,2)
REWIND 3
REWIND 14
NJTNH4 = 4*NØJS
READ(14) ((BCD(I,J),J=1,NZ),I=1,NJTNH4)
DØ 800 L=1,2
CØ 800 J=1,NJTNH4
DRE(J,L)=0.
DØ 800 K=1,NZ
800 DRE(J,L)=DRE(J,L)+BCD(J,K)*QVEC(K,L)
DØ 71 NR=1,NREG
DØ 71 K=1,2
II = (JRTIC(NR)-1)*4+1
IF (K.EQ.2) II = JRSTØP(NR)*4-3
III = II+3
DØ 71 I=II,III
71 WRITE(3)(DRE(I,L),L=1,2)
REWIND 3
RETURN
END
4600000
4600010
4600030
4600040
4600050
4600060
4600070
4600090
4600110
4600120
4600130
4600140
4600150
4600160
4600180
4600190
4600200

```

SUBROUTINE ETRAP

This is an error trap routine which can be called by the MAIN routine at various stages of program execution. If the indicator NIX is not equal to zero, MAIN will call ETRAP and indicate the proper message to be printed.

```

C ..... ROUTINE *D22* ** ABACUS UPDATED 07/07/72 .....
SUBROUTINE ETRAP
  INTEGER SAVJTC, SAVSTP, Q, THICK
  INTEGER XN
  COMMON STOR(116), XMAT(110,10), STD(10), SADUS(30), RADUS(30)
  COMMON RADUS(30), UADUS(30), SAVTIC(900)
  COMMON XN, TEFREE, TIC, PHI, STOP, RESTOP, RTICK, G1, XNL(2), NH
  COMMON NST(30), NKL(30), NXMAT(20), SAVJTC(30), SAVSTP(30), JRTIC(30)
  COMMON JSTOP(30), NREG, NMPT, NRC, NSC, NIX, IERROR, KGEOM, ISTATB
  COMMON KELVIN, IBEGIN, NPRB, NSEG, NERROR, Q, THICK, NQJS, NLINKS, NLCASE
  COMMON NTSKL, NZ, NBCT, LINPUT, NTRKL, NPASS, XN1, KBC, NRINGS
  DOUBLE PRECISION SAVTIC, TIC, PHI, STOP, RESTOP, RTICK
  WRITE(6,1726)
1726 FORMAT(1H1)
  GO TO (8000,8036,8086,8087,8089,8090,8013,8009,8031,8008,8001,
1 8002,8003,8006,8007,8101,8102,8103,8104,8105,8106,
2 8107,8108,8109,8110,8088,110,8120,8841,8842,8777,8797,
3 8787),NERROR
8000 WRITE(6,1)
1 FORMAT(/ 4X,-ONE OF THE MATERIAL PROPERTY TABLES CANNOT BE IDENTI-
  FIED AS ISOT, ORTH, OR STIF.-/)
  GO TO 505
8036 WRITE(6,2)
2 FORMAT(/ 4X,-A MATERIAL PROPERTY TABLE NAME FOR A SEGMENT CANNOT
  BE FOUND IN THE TABLE LIST.-/)
  GO TO 505
8086 WRITE(6,3)
3 FORMAT(/ 4X,-THE TYPE OF GEOMETRY OF A SEGMENT CANNOT BE IDENTIFI-
  LIED AS ONE HANDLED BY THE PROGRAM.-/)
  GO TO 505
8087 WRITE(6,4)
4 FORMAT(/ 4X,-THE TYPE OF MATERIAL PROPERTY TABLE FOR A SEGMENT CA-
  NNOT BE IDENTIFIED AS ISOT, ORTH, OR STIF.-/)
  GO TO 505
8089 WRITE(6,5)
5 FORMAT(/ 4X,-THE WALL CONSTRUCTION OF A SEGMENT CANNOT BE IDENTIF-
  IED AS SING, EQUA, UNEQ, OR BLAN.-/)
  GO TO 505
8090 WRITE(6,6)
6 FORMAT(/ 4X,-THE TYPE OF TEMPERATURE INPUT FOR A SEGMENT CANNOT B-
  E IDENTIFIED AS THST, NQTH, THCN, OR THIN.-/)
  GO TO 505
8013 GO TO 505
8009 GO TO 505
8031 WRITE(6,9)
9 FORMAT(/ 4X,-THE LOAD INDICATOR CLUES CAN ONLY BE ZERO, BLANK, OR
  IE, OR FOUR.-/)
  GO TO 505
8008 WRITE(6,10)
10 FORMAT(/ 4X,-THE PROGRAM CAN EXECUTE ONLY ONE THERMAL LOAD PROBLE
  M PER DATA DECK.-/)
  GO TO 505
8001 WRITE(6,11)
11 FORMAT(/ 4X,-THE MAGIC CYCLE HAS GONE PAST STOP BY MORE THAN THE
  PERMITTED VALUE. CHECK TO SEE IF FIXED STEP SIZE IS TOO LARGE.-/)
  GO TO 505
8002 WRITE(6,12)
12 FORMAT(/ 4X,-THE RIEMAN VARIABLE, IEND, WHICH SIGNALS THE END OF
  A SEGMENT SHOULD ONLY BE ZERO OR NEGATIVE ONE.-/)
  GO TO 505
8003 GO TO 505
8006 GO TO 505

```

```

8007 WRITE(6,15)
15 FORMAT(/ 4X,-THE INTERPOLATED VALUE OF TEMPERATURE FOR THE MATERI
IAL PROPERTY TABLE IS LESS THAN THE SECOND TEMPERATURE VALUE.-/)
GO TO 505

8067 WRITE(6,16)
16 FORMAT(/ 4X,-THE INTERPOLATED VALUE OF TEMPERATURE FOR THE MATERI
IAL PROPERTY TABLE IS GREATER THAN THE LAST VALUE OF TEMPERATURE.-
2/)
GO TO 505

8101 WRITE(6,17)
17 FORMAT(/ 4X,-THE K11 STIFFNESS PARAMETER IS ZERO.-/)
GO TO 505

8102 WRITE(6,18)
18 FORMAT(/ 4X,-THE K12 STIFFNESS PARAMETER IS ZERO.-/)
GO TO 505

8103 WRITE(6,19)
19 FORMAT(/ 4X,-THE K21 STIFFNESS PARAMETER IS ZERO.-/)
GO TO 505

8104 WRITE(6,20)
20 FORMAT(/ 4X,-THE K22 STIFFNESS PARAMETER IS ZERO.-/)
GO TO 505

8105 WRITE(6,21)
21 FORMAT(/ 4X,-THE K33 STIFFNESS PARAMETER IS ZERO.-/)
GO TO 505

8106 WRITE(6,22)
22 FORMAT(/ 4X,-THE D11 STIFFNESS PARAMETER IS ZERO.-/)
GO TO 505

8107 WRITE(6,23)
23 FORMAT(/ 4X,-THE D12 STIFFNESS PARAMETER IS ZERO.-/)
GO TO 505

8108 WRITE(6,24)
24 FORMAT(/ 4X,-THE D21 STIFFNESS PARAMETER IS ZERO.-/)
GO TO 505

8109 WRITE(6,25)
25 FORMAT(/ 4X,-THE D22 STIFFNESS PARAMETER IS ZERO.-/)
GO TO 505

8110 WRITE(6,26)
26 FORMAT(/ 4X,-THE D33 STIFFNESS PARAMETER IS ZERO.-/)
GO TO 505

8088 WRITE(6,27)
27 FORMAT(/ 4X,-THE PROGRAM CANNOT DETERMINE WHETHER THE PROBLEM INP
UT IS THIC, RWA1, RWA2, RWA3, ST10, ST11, ST12, ST13, ISG1,
2ISG2, OR ISG3.-/)
110 GO TO 505

8120 WRITE(6,29)
29 FORMAT(/ 4X,-THE Y2 BLOCK IN THE SEGMENT MAGIC OUTPUT IS SINGULAR
1.-/)
GO TO 505

8841 WRITE(6,30)
30 FORMAT(/ 4X,-IN THE COMPUTATION OF THE REGION STIFFNESSES, THE K2
12 MATRIX WAS NOT POSITIVE DEFINITE.-/)
GO TO 505

8842 WRITE(6,31)
31 FORMAT(/ 4X,-IN THE COMPUTATION OF THE REGION LOADS, THE K22 MATR
IX WAS NOT POSITIVE DEFINITE.-/)
GO TO 505

8777 WRITE(6,32)
32 FORMAT(/ 4X,-IN THE COMPUTATION OF THE REDUCED FLEXIBILITY MATRIX
1, THE REDUCED STIFFNESS MATRIX IS SINGULAR.-/)
GO TO 505

8797 WRITE(6,33)

```

```

33 FORMAT/ 4X,-FOR KINEMATIC LINKS BETWEEN SEGMENTS, THE DEPENDENT
  JOINT NUMBER MUST BE GREATER THAN THE INDEPENDENT JOINT NUMBER.-/)
  GO TO 505
8787 WRITE(6,34)
34 FORMAT/ 4X,-THE NUMBER OF POINTS IN THE ST TABLE MUST BE BETWEEN
  1 2 AND 30.-/)
505 RETURN
  END

```

REFERENCES

1. Svalbonas, V., "Numerical Analysis of Stiffened Shells of Revolution - Vol. I: Theory", NASA CR-2273.



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